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Streamer propagation in the atmosphere of Titan and other N₂:CH₄ mixtures compared to N₂:O₂ mixtures

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Abstract

Streamers, thin, ionized plasma channels, form the early stages of lightning discharges. Here we approach the study of extraterrestrial lightning by studying the formation and propagation of streamer discharges in various nitrogen-methane and nitrogen-oxygen mixtures with levels of nitrogen from 20% to 98.4%. We present the friction force and breakdown fields $E_b$ in various $N_2$:O$_2$ (Earth-like) and $N_2$:CH$_4$ (Titan-like) mixtures. The strength of the friction force is larger in $N_2$:CH$_4$ mixtures whereas the breakdown field in mixtures with methane is half as large as in mixtures with oxygen.

1. Introduction

Lightning on Earth is a highly complex phenomenon involving physical processes on various spatial and temporal scales (Villanueva et al., 1994; Ebert et al., 2006; Ebert and Sentman, 2008; Luque and Ebert, 2012; Rakov, 2013; da Silva and Pasko, 2013) starting from electron avalanches and resulting in the formation of hot, conducting lightning leaders. The early stages of lightning discharges are formed by streamers, thin, ionized plasma channels (Loeb, 1939; Raether, 1939; Loeb and Meek, 1940; Morrow and Lowke, 1997; Ebert and Sentman, 2008; Luque et al., 2008; Liu et al., 2012; Qin and Pasko, 2014). Three necessary, yet not sufficient, conditions for the inception of streamers are the presence of initial free electrons with a sufficiently high density, a sufficiently high ambient electric field to accelerate electrons and an ambient gas as a source of new electrons to sustain the streamer discharge.

In our solar system, lightning activity has been detected on several planets. Whilst the occurrence of lightning on Venus is still a controversial question (Russell et al., 2007; Takahashi et al., 2008; Moineau et al., 2016; Pérez-Invernón et al., 2016; Takahashi et al., 2018), we possess clear evidences of lightning in the atmospheres of the gas and ice giants. Since Voyager 1, every probe that has approached Jupiter has imaged lightning flashes from its night side. Lightning has also been identified on Jupiter by its very-low frequency (VLF) radio signatures (Vasavada and Showman, 2005; Yair et al., 2008) and recently at 600 MHz by the Juno Microwave Radiometer (Brown et al., 2018). On Saturn, lightning has been recently detected optically and by its high-frequency (HF) radio signals (Dyudina et al., 2010, 2013), known as Saturn electrostatic discharges (SED) (Fischer et al., 2008). HF radio signals similar to those observed on Saturn have been detected by the Voyager 2 radio instrument at Uranus (Yair et al., 2008; Zarka and Pedersen, 1986). Lightning is also believed to take place at Neptune, based on the detection of lightning whistler like events observed during the encounter of Voyager 2 with this planet (Gurnett et al., 1990; Gibbard et al., 1999), and on Mars, in dust storms, based on the measurements of higher order moments of the electric field by a detector installed on NASA’s Deep Space Network (Renno et al., 2003; Ruf et al., 2009) and supported by simulations by Melnik and Parrot (1998). However, more recent measurements on Mars by Anderson et al. (2012) and by Gurnett et al. (2010) using the Allen Telescope and the radar receiver of Mars Express have not found any signatures of lightning discharges. Hence, it is still controversial whether lightning exists on Mars.

The existence of atmospheric electric discharges on these planets...
has been modelled by numerical simulations and tested by laboratory experiments. Using Monte Carlo simulations, Dwyer et al. (2006) simulated the runaway breakdown, which is the discharge initiation through high-energy electrons whose friction is significantly smaller than for low-energy electrons (Gurevich et al., 1992), in the atmospheres of Jupiter and Saturn. They found that the runaway breakdown field lowered by the presence of hydrometeors is ten times smaller than the conventional breakdown field and suggest that this might facilitate lightning inception on these planets.

Fulchignoni et al., 2005). Yet, a subsequent analysis of the provided data rather suggested that this resonance is an artifact of Titan's inhomogeneities. In Section 3 we discuss the temporal evolution of the discharge experiments in a gas resembling the composition on Titan

Dubrovin et al. (2010) investigated experimentally the inception and the motion of streamer discharges in CO2:N2 and H2:He as they are present in the atmospheres of Venus and Jupiter above the cloud layers at pressures between 25 and 200 mbar. They discovered that streamer discharges similar to sprites could exist in these atmospheres, yet fainter than on Earth. However, to the best of our knowledge, there have not been any simulations of streamer discharges and their inception in non-terrestrial gas compositions modelling the very early stages of lightning discharges.

Amongst the bodies of our solar system, not only planets, but also some of their moons shelter an atmosphere, such as Jupiter's satellite Europa with a pressure of 10^11 bar (Hall et al., 1995) or Saturn's moon Titan. Both satellites are suspected to host amino acids (Raulin, 2005; Loison et al., 2015) which are a necessary condition for the formation of life as we know it (Haldane, 1929; Oparin, 1938; Ward and Kirschvink, 2015). Waite Jr. et al. (2007) discussed that cosmic gamma-rays enter Titan's atmosphere and facilitate the formation of organic compounds, so-called Tholins. Its atmosphere mainly consists of carbonaceous methane and nitrogen which resembles the atmosphere of the primordial Earth also containing carbon monoxide, water, methane and nitrogenous ammonia. Miller (1953) and Miller and Urey (1959) mimicked lightning by performing spark discharges in the same gas mixture as of primordial Earth. They discovered that amino acids were formed in their set-up concluding that lightning could be one trigger for the formation of amino acids and molecules relevant for the formation of amino acids and nucleic acids.

First attempts to detect lightning on Titan were executed in 1980 when Voyager 1 flew by Saturn and Titan (Desch and Kaiser, 1990). Since the thickness of clouds and haze layers prevented the measurements of optical signatures, the search was extended towards spherics at radio wavelengths. However, no relevant data were recorded concluding that the maximum energy of a lightning flash on Titan would be approx. 1 MJ, approx. 1000 times weaker than for lightning flashes on Earth (Rakov and Uman, 2003).

In 2005, the Huygens Atmospheric Structure Instrument (HASI), designed to accurately measure atmospheric properties of Titan, measured a resonance at 36 Hz initially linked to the occurrence of lightning (Fulchignoni et al., 2005). Yet, a subsequent analysis of the provided data rather suggested that this resonance is an artifact of Titan’s interaction with Saturn’s magnetosphere (Béghin et al., 2009).

Successively, Cassini’s RPWS (Radio and Plasma Wave Science) instrument (Lammer et al., 2001; Fischer et al., 2007; Lorenz and Mitton, 2008; Fischer and Gurnett, 2011) tried to search for radio emissions as an indicator for lightning on Titan during, in total, 127 flybys. Again, during these missions, no positive results were found; however, the conclusion was not that lightning does not exist on Titan, but rather that, if lightning exists, it is too weak to be detected.

Despite the fact that lightning has not been observed directly by cameras on-board or indirectly by radio instruments during Cassini’s observations or during the descent of the Huygens probe, the atmospheric chemistry suggests the presence of electrical discharges in the atmosphere of Titan. Titan has a substantial atmosphere consisting predominantly of nitrogen and methane with trace amounts of hydrogen, hydrogen cyanide, ethane, propane, acetylene and other hydrocarbons and nitriles. The presence of the majority of these hydrocarbons and nitriles in the atmosphere of Titan has been explained in terms of photochemistry and charged-particle chemistry models with few exceptions. Perhaps the best known example is ethylene, which is more abundant in the upper atmosphere of Titan than photochemistry models would predict (Bar-Nun and Podolak, 1979; Borucki et al., 1988). Borucki et al. (1988) argued that the excess of ethylene in the upper Titan’s atmosphere could be explained by upward diffusion of ethylene produced in the lower parts of the atmosphere by lightning.

The post-Huygens era chemical model of Titan’s atmosphere by Lavvas et al. (2008) still underestimates the abundance of ethylene in the stratosphere compared to the measurements. Likewise, the presence of acetylene and hydrogen cyanide with the relatively high abundances of (1.9 ± 0.2) × 10^−6 and (1.5 ± 0.2) × 10^−7 (Taylor and Coutenisi, 1998), respectively, could also be explained by the lightning induced chemistry. On the contrary, more recent photochemical models (Vuitton et al., 2019) including isotopic photoabsorption and photodissociation for N2 as well as photodissociation branching ratios for CH4 and C2H2 simulates the density of organic species in Titan’s atmosphere without the need of lightning discharges.

Whereas Earth’s surface conductivity is approximately 10^−14 S m^−1 (Wählín, 1994), Molina-Cuberos et al. (2001) approximated Titan’s surface conductivity to range between 10^−15 S m^−1 and 10^−14 S m^−1, thus sufficiently large to allow the generation of cloud-to-ground lightning flashes. Tokano et al. give an extensive overview of available cloud convection and charging models as well as particle charging mechanisms (see Tokano et al., 2001 and references therein). They apply a one-dimensional time-dependent thundercloud model and state that negative space charges resulting from the attachment of electrons to clouds, can temporally create electric fields of up to 2 MV m^−1 which is sufficient to initiate 20 km long negative cloud-to-ground lightning.

We here strive to answer the question whether streamer discharges, the pre-cursors of lightning, exist in Titan’s atmosphere. Therefore, we perform Monte Carlo particle-in-cell simulations of electron avalanches in mixtures of N2:CH4 with different percentages of nitrogen in various electric fields and determine for which conditions the electron avalanches transition into streamer discharges. We also run simulations in N2:O2 mixtures with the same percentage of nitrogen and compare results for methane and for oxygen.

In Section 2 we briefly discuss the atmospheric profile of Titan and the set-up of our simulations. Additionally, we discuss the friction forces as well as the electric breakdown fields in different N2:O2 and N2:CH4 mixtures. In Section 3 we discuss the temporal evolution of the electron densities, the front velocities and the resulting electric field and compare results in mixtures with methane and with oxygen. We discuss when avalanche-to-streamer transitions are feasible and relate our results to the friction force and thus to the electron energy distribution. In Section 4 we summarize our results and discuss whether lightning is possible to occur on Titan. Finally, we give an outlook on future research activities.

2. Modelling and properties of Titan’s atmosphere

2.1. Set-up of the model

We simulate the development of electron avalanches and, if exist, of subsequent streamers with a 2.5D Monte Carlo particle-in-cell code with cylindrical symmetry with two spatial coordinates (r,z) and...
three coordinates \((v_x,v_y,v_z)\) in velocity space for each individual (super) electron (Chanrion and Neubert, 2008, 2010). We perform simulations in mixtures of \(\text{N}_2\text{O}_2\) and of \(\text{N}_2\text{CH}_4\) with different percentages \(\kappa\) of \(\text{N}_2\). Thus, Earth’s atmosphere is determined by \(\kappa = 0.8\) with its nitrogen-oxygen mixture and Titan’s atmosphere by \(\kappa = 0.984\) with its nitrogen-methane mixture. For a better comparison of the results in different gas mixtures, we use a gas density of \(2.9 \cdot 10^5 \text{m}^{-3}\) in all mixtures (see Section 2.2). As common for streamer discharges on Earth at distances such as the attachment to haze particles need a more extensive study after general avalanche and streamer characteristics in various \(\text{N}_2\text{O}_2\) and \(\text{N}_2\text{CH}_4\) have been discussed in the present paper.

The collision of electrons with nitrogen and oxygen molecules, cross sections as well as their implementation have already been studied carefully in various publications (e.g. Gurevich, 1961; Phelps and Pitchford, 1985; Crompton, 1994; Moss et al., 2006; Chanrion and Neubert, 2008; Dujko et al., 2011; Li et al., 2012; Köhn and Ebert, 2014, 2015). We review the collisions of electrons with methane molecules and the resulting friction force in Section 2.3.

Accounting for space charge effects, we solve the Poisson equation in the simulation domain with dimensions \((L_x,L_y,L_z) = (1.25,14,14)\) mm and with 150 grid points in \(r\) and 1200 grid points in \(z\)-direction (Kön et al., 2017). As boundary conditions, we use Neumann conditions \(\partial \phi/\partial r = 0\) for \(r = 0, L_x\), and Dirichlet conditions for the electric potential \(\phi(r,0) = 0\) and \(\phi(L_x,0) = \phi_{\text{amb}} = E_{\text{amb}} \cdot L_x\) where \(E_{\text{amb}}\) is the ambient electric field pointing downwards. We have performed simulations in ambient fields of 1.5, 2 and 3 times the classical breakdown field \(E_b\).

We initiate all simulations with a charge neutral electron-ion patch at the center of the simulation domain. The initial electron density is given by the Gaussian \(n_e(r,z,t=0) = n_{e,0} \exp\left(-(r^2 + (z-z_0)^2)/\lambda^2\right)\) with \(n_{e,0} = 10^20 \text{m}^{-3}\) as in Arrayás et al. (2002), Liu and Pasko (2004), and Köhn et al. (2017) and \(\lambda = 0.2\) mm centered at \(z_0 = 7\) mm. As in previous work, the initial electron energy is zero. As Li et al. (2007) have shown in a mixture of \(\text{N}_2\text{O}_2\) with \(\kappa = 0.8\), electron energies equilibrate towards similar energy distributions for different initial electron energies below 50 eV.

### 2.2. Titan’s atmospheric composition

An overview of the abundances of the constituents of Titan’s atmosphere is given in Niemann et al. (2005). Titan’s atmosphere is composed mainly of nitrogen and of methane where the percentage of methane varies from approx. 5% at ground up to approx. 1.4% at 140 km altitude. In order to perform reliable simulations, it is, however, not sufficient to know the gas composition, but we also need to specify the correct number density of ambient gas molecules. Lindal et al. (1983) and McKay et al. (1989) give an extended overview of Titan’s temperature and pressure profile as a function of altitude. Further measurements of the temperature and pressure were later performed by the Huygen’s Atmospheric Structure Instrument (HASI) descending towards Titan’s surface (Fulchignoni et al., 2005).

On Titan, clouds form between 20 km and 35 km altitude (Barth and Rafkin, 2007; Griffith et al., 2009) with the pressure varying between approximately 0.1 bar and 0.6 bar, the temperature varying between 70 K and 75 K and the level of methane varying between 1.6% and 2.0% (Müller-Wodarg et al., 2014). Hence, we here choose 1.6% of methane as well as \(p = 0.3\) bar and \(T = 75 K\) yielding a gas density of \(\rho_{\text{Titan}} = p/ (k_B T) \approx 2.9 \cdot 10^1 \text{m}^{-3}\) using the ideal gas law. On Earth a density of \(2.9 \cdot 10^3 \text{m}^{-3}\) corresponds to a pressure of approx. 1.2 bar at 300 K or approx. 1 bar at 250 K (equivalent to 10 km altitude).

### 2.3. Cross sections and friction forces for electrons in \(\text{N}_2\text{O}_2\) and \(\text{N}_2\text{CH}_4\) mixtures

Fig. 1a shows the cross sections \(\sigma_{ij}\) for different collision processes \(j\) of electrons at different species \(i\). As for oxygen, electrons scatter off methane elastically, excite, ionize or attach to it. The most frequent process below approximately 50 eV is elastic scattering followed by excitations (Šašić, O. et al., 2004). Since the ionization threshold energy is \(E_i \approx 12.6\) eV, the ionization cross section starts to increase for energies above and becomes predominant above approximately 50 eV.

However, due to the lack of reliable data, we do not have differential cross sections for elastic and inelastic collisions, including those for ionization. However, as we discuss below, most of the electrons in the \(\text{N}_2\text{CH}_4\) simulations have energies below 50 eV. For such low energies, the collision dynamics is well described by the approximation of isotropic scattering. The isotropy of scattering may be assumed due to the fact that numerous elastic collisions generally randomize directions of electron motion and hence one could not see any significant effects of introducing the anisotropy of scattering. The determination of the momentum transfer cross section is usually performed under the assumption of anisotropy, so the cross section has this assumption inherently built into it. Of course, for higher electron energies the approximation of isotropic scattering is no more valid and the use of differential cross sections for electron scattering is mandatory (see for example a detailed discussion in Li, 2009). The energy \(W\) of secondary ionization electrons is determined uniformly randomly in \([0,E_{in}−E_i]\) where \(E_{in}\) is the kinetic energy of the incident electron. Subsequently, we apply the conservation of energy and momentum and determine (Kön and Ebert, 2014; Celestin and Pasko, 2010) the scattering angle

\[
\cos \Theta_{\text{out}} = \cos \Theta_{\text{in}} = \frac{(E_{in}−W)(E_{in}+2m_e c^2)}{E_{in}(E_{in}−W+2m_e c^2)}
\]

of the incident electron and the emission angle

\[
\cos \Theta_i = \frac{W (E_{in}+2m_e c^2)}{E_{in}(W+2m_e c^2)}
\]

of the liberated electron with \(m_e\) being the electron’s rest mass and \(c\) the speed of light. Note that these relativistic equations are valid also for non-relativistic electron energies.

Panels b and c in Fig. 1 show the friction force

\[
F_b(E) = \sum_{ij} n_i \sigma_{ij}(E) \Delta E_i j,
\]

where \(n_i\) is the partial density \([\text{m}^{-3}]\) of \(\text{N}_2\text{O}_2\) or \(\text{CH}_4\), \(\sigma_{ij}\) is the total cross section for collision process \(j\) of electrons at molecule species \(i\) and \(\Delta E_j\) the respective energy loss of electrons. The sum is taken over all involved molecule species \(i\) and over all involved inelastic collisions \(j\). Note that excitations and ionization are the only processes below 100 eV contributing to the friction where the energy loss resulting from excitations is the threshold energy of the collision and the energy loss for ionization is \(1/2(E_{in}−E_i)\). Panel b) shows the friction of electrons in different mixtures of \(\text{N}_2\text{O}_2\). The overall shape is similar irrespective of the percentage \(\kappa\) of nitrogen. However, the strength of excitational losses for energies below 1 eV increases with decreasing \(\kappa\) since the cross section and subsequently the contribution of excitations is higher for oxygen than for nitrogen. On the contrary, the contribution of excitations above 1 eV increases with increasing percentage of nitrogen. For \(E \geq 1\) eV, there is a resonance in the cross section of the vibrational states of excited nitrogen with threshold energies of approximately 2 eV (see for example Tab. 1 in Moss et al., 2006). For energies above approximately 10 eV, the friction forces for different \(\kappa\) align because the total ionization cross section and the corresponding energy loss are comparable for nitrogen and oxygen.

Panel c) shows the friction force for different \(\text{N}_2\text{CH}_4\) mixtures. For comparison, the dashed yellow and purple lines additionally show the friction force for \(\text{N}_2\text{O}_2\) with 20% and 80% nitrogen. Whilst the overall shape of the friction force is different than for \(\text{N}_2\text{O}_2\), we observe the same dependency on \(\kappa\). Since the cross section for exciting methane for electron energies between 0.2 eV and 2 eV is larger than for nitrogen,
Because of the resonance of the cross section for exciting nitrogen above 2 eV, the friction increases with $\kappa$ for energies between 2 eV and 5 eV. For energies above 5 eV, the friction increases and becomes smaller for large $\kappa$ with an exception between 8 and 15 eV where the friction is almost independent of $\kappa$. Comparing the friction force in N$_2$:O$_2$ (b) and in N$_2$:CH$_4$ (c) as a function of electron energy for different percentages $\kappa$ of molecular nitrogen. For comparison, the dashed yellow and purple lines in c) show the friction force for a N$_2$:O$_2$ mixture with 20% and 80% nitrogen. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Fig. 1. a) Cross sections for electron scattering in N$_2$, O$_2$ and CH$_4$. We show cross sections for momentum transfer in elastic collisions, total cross sections for electronic excitation (including dissociation into neutral fragments) and cross sections for electron-impact ionization. b, c) The friction force in N$_2$:O$_2$ (b) and in N$_2$:CH$_4$ (c) as a function of electron energy for different percentages $\kappa$ of molecular nitrogen. For comparison, the dashed yellow and purple lines in c) show the friction force for a N$_2$:O$_2$ mixture with 20% and 80% nitrogen. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

the friction force increases for an increasing percentage of methane. Because of the resonance of the cross section for exciting nitrogen above 2 eV, the friction increases with $\kappa$ for energies between 2 eV and 5 eV. For energies above 5 eV, the friction increases and becomes smaller for large $\kappa$ with an exception between 8 and 15 eV where the friction is almost independent of $\kappa$. Comparing the friction force in N$_2$:O$_2$ mixtures with the friction force in N$_2$:CH$_4$ mixtures reveals that, for fixed $\kappa$, the strength of the friction force above approximately 2 eV is similar for mixtures with oxygen and with methane, hence the energy loss of electrons above 2 eV is comparable. However, it is noticeable that for energies below 2 eV and fixed $\kappa$, the friction in N$_2$:CH$_4$ mixtures is approximately one to two orders of magnitude higher than in mixtures with oxygen.

2.4. Photoionization

In oxygen-nitrogen mixtures, one additional process contributing to the evolution of streamer discharges is photoionization: Electrons can excite nitrogen which subsequently emits UV photons. In return, these UV photons ionize oxygen and thus deliver a new source of electrons (Zheleznyak et al., 1982; Luque et al., 2007; Bourdon et al., 2007; Wormeester et al., 2010; Köhn et al., 2017). Although this process is not crucial for the development for negative fronts, it supports their motion (see e.g. a discussion in Luque et al., 2007; Köhn et al., 2017). For positive streamer fronts moving towards the cathode, however, photoionization is one of the key drivers next to background ionization (Pancheshnyi, 2005; Nijdam et al., 2011).

In oxygen, we use the model of Zheleznyak et al. (1982), Chanrion and Neubert (2008), and Köhn et al. (2017) which relates the number of UV photons with energies between 12.10 eV and 12.65 eV to the number of electron impact ionization. This is the energy range where photons do not interact with nitrogen and predominantly ionize molecular oxygen. Beyond 12.65 eV, photons mainly excite nitrogen and do not contribute to the ionization of oxygen anymore (Liu et al., 2012; Carter, 1972). The ionization energy of molecular nitrogen is 15.6 eV, thus larger than the upper limit for UV photoionization. Note that the threshold energy for the ionization of oxygen is 12.1 eV, thus on the lower limit of the energy of considered UV photons.

Since the ionization energy of methane is 12.6 eV, photoionization by UV photons still contributes to the development of electron avalanches or streamers in N$_2$:CH$_4$, even though less efficiently. We thus implement the model of Zheleznyak et al., but evaluate the UV photoionization process randomly in (12.65 − 12.6)/(12.65 − 12.1) = 9% of all photoionization events in the model by Zheleznyak et al. only.
which is the ratio of the energy intervals of UV photoionization in methane and in oxygen.

2.5. The electric breakdown field

During the motion of electrons through ambient gas, electrons undergo two competing processes: First, they gain energy through the background electric field and they lose energy through inelastic collisions with the ambient gas molecules. Second, amongst these inelastic collisions, electrons are capable of ionizing the ambient gas and multiply the total electron number as long as the primary electron’s energy is above the ionization threshold energy. As a competing process, electrons attach to molecules reducing the total electron number. These two processes compete with each other and severely depend on the ambient electric field (Raizer, 1991). The breakdown (or critical) field \( E_b \) is defined as the electric field when the attachment rate equals the ionization rate. Thus, in order to initiate and sustain an electron avalanche and eventually transition into a streamer, electric fields at least above the breakdown field are required such that there is a sufficient number of ionization events.

All transport properties, including the ionization and attachment rates for electrons in \( \text{N}_2: \text{O}_2 \) and \( \text{N}_2: \text{CH}_4 \) mixtures, are calculated using a multi term theory for solving the Boltzmann equation (Dujko et al., 2010). The input data for the Boltzmann equation are the cross sections for electron scattering in \( \text{N}_2, \text{O}_2 \) and \( \text{CH}_4 \) presented in Section 2.3. The ionization coefficient is a monotonically increasing function of the electric field for both \( \text{N}_2: \text{O}_2 \) and \( \text{N}_2: \text{CH}_4 \) mixtures over the range of the electric fields considered in this work. On the other hand, the attachment coefficient firstly increases with the applied electric field, reaching a maximal value, and then it starts to decrease. As expected, we have found that the attachment rate is reduced for increasing concentration of \( \text{N}_2 \) in both \( \text{N}_2: \text{O}_2 \) and \( \text{N}_2: \text{CH}_4 \) mixtures over the entire range of electric fields considered. This follows from the fact that \( \text{N}_2 \) is a non-attaching gas. We have also found that the ionization rate is reduced for increasing concentration of \( \text{N}_2 \) in these mixtures. By increasing the nitrogen concentration, more and more inelastic channels are open, the electrons can lose several discrete values of energy in various inelastic collisions. Due to this inelastic cooling effect, the mean swarm energy is reduced and as a consequence, the ionization rate drops off. Finally, the ionization rate in the pure \( \text{N}_2 \) is less than the ionization rates in both \( \text{O}_2 \) and \( \text{CH}_4 \) over a range of the applied electric field which follow directly from the energy dependence of the cross sections for electron scattering. More details are described in the accompanying paper (Bošnjaković et al., 2019).

Fig. 2 shows the breakdown field as a function of the percentage \( \kappa \) of nitrogen in \( \text{N}_2: \text{O}_2 \) mixtures and in \( \text{N}_2: \text{CH}_4 \) mixtures with a gas density of \( 2.9 \cdot 10^{25} \text{ m}^{-3} \). The plot also shows the ratio of the breakdown fields between these two different mixtures (right y-axis).

Fig. 3 shows the electron density and the electric field (third column) for gas mixtures with 80% nitrogen in ambient fields of 1.5\( E_b \) (first row), 2\( E_b \) (second row), 3\( E_b \) (third row), where \( E_b \) is \( 3.5 \text{ MV m}^{-1} \) in mixtures with oxygen and \( 1.6 \text{ MV m}^{-1} \) in mixtures with methane, after different time steps. In columns one to three, the left halve of each panel show the electron density or electric field in mixtures with 20% oxygen, i.e. the concentration on Earth, whereas the right halve show the density and field in mixtures with 20% methane which we refer to as Earth-like Titan. Fig. 4 shows the electron density in Earth-like Titan mixtures at the end of our simulations.

In our simulations, the electron-ion patch on Earth develops into a bidirectional streamer for any field above 1.5\( E_b \). The electric field shows the typical streamer-like pattern with an enhanced field at the tips and a shielded field inside the streamer body. Exchanging oxygen with methane dramatically changes the picture; the process of forming electron avalanches or eventually streamers becomes delayed significantly irrespective of the applied field. Columns one and two show that there is hardly any development whilst in mixtures with oxygen, streamers have already formed after the same time steps. However, the electric field shows the same pattern as in \( \text{N}_2: \text{O}_2 \) with an enhanced field at the tips of the electron patch and a vanishing shield in the patch’s interior.

As Fig. 4 illustrates, we observe three different scenarios in mixtures with \( \text{CH}_4 \) at the end of the simulations depending on the ambient electric field. In a field of 1.5\( E_b \), the field at the positive front increases; however, the positive front does not move, hence there is no development of a positive streamer front. On the negative side, an electron avalanche, but no streamer front forms, without any significant field increase at the top. At the end of the simulation, the field at the tip is 1.8\( E_b \) and the electron density is \( \leq 10^{17} \text{ m}^{-3} \). In an ambient field of 2\( E_b \), the situation does not change significantly at the positive front. The field increases, but the front does not develop. On the negative front, however, we observe the formation of a streamer-like channel. During the simulation, the field at the tip varies between approximately 3\( E_b \) and 6\( E_b \) whereas the field is shielded in its interior. In contrast to the density with 1.5\( E_b \) in Fig. 4a, the electron number slightly multiplies and reaches a density of \( \approx 10^{19} \text{ m}^{-3} \) after 15.92 ns. In \( E_{\text{min}} = 3\( E_b \) there is the distinct formation of a positive and of a negative streamer front similar to as in air. Since the breakdown fields in \( \text{N}_2: \text{O}_2 \) and in \( \text{N}_2: \text{CH}_4 \) differ by a factor of \( \approx 2 \), the absolute value of 3\( E_b \) in \( \text{N}_2: \text{CH}_4 \) corresponds to the value of 1.5\( E_b \) in air. Hence, the evolution of the electron density and of the electric field is comparable although delayed.

Fig. 5 shows the front velocities in the early stages of the evolution of electron avalanches and streamers for \( \kappa = 0.8 \) for \( \text{O}_2 \) and \( \text{CH}_4 \) and for
all considered electric fields. Depending on the electric field, the streamer velocity in N₂:O₂ lies between $10^0$ and $10^1$ mm ns$^{-1}$ and is similar for the positive and the negative streamer front. For $E_{\text{amb}} = 1.5E_k$ and $E_{\text{amb}} = 2E_k$ in N₂:CH₄ the velocity of the positive front lies between $10^{-2}$ and $10^{-1}$ mm ns$^{-1}$ and is decreasing with time which is in agreement with panels a–c and d–f in Fig. 3 with no distinct fronts for these fields, similarly for negative fronts. For $3E_k$, Fig. 3i shows the development of a positive and a negative streamer front. The slope of the velocity is comparable to the increase of streamer velocities in air in a field of $1.5E_k$; however, in air, positive fronts and negative fronts are faster than in N₂:CH₄.

The delayed motion of fronts in mixtures with methane is related to the drift of electrons. Fig. 6a shows the drift velocity of electrons in nitrogen-methane and nitrogen-oxygen mixtures as a function of the ambient field. It is higher and increasing more significantly in mixtures with oxygen. Consequently the motion of fronts in N₂:CH₄ mixtures is delayed. Note that the calculation of the drift velocity does not consider space charges and therefore neglects the highly enhanced electric field in the streamer tips. Such high field tips usually accelerate electrons more efficiently than the ambient electric field which in turns lead to a higher velocity of streamer fronts than the electron drift velocity. In addition, a very steep gradient in the electron number density leads to a strong diffusive flux further enhancing the velocity of the propagating fronts. The differences in the avalanche-to-streamer transition as well as in the streamer evolution between Earth and Earth-like Titan for the same $E_{\text{amb}}/E_k$ results from different ionization lengths in N₂:O₂ and in N₂:CH₄ as well as from the reduced probability for photoionization. Fig. 6b shows the effective ionization coefficient as a function of the electric field. It shows that ionization in a mixture with 20% methane is less effective than in a mixture with 20% oxygen for all considered field strengths. Beyond, the growth of the ionization coefficient is much less dominant in N₂:CH₄ mixtures than in N₂:O₂. Panel c) shows the ionization length $\Lambda_{\text{ion}}$ as a function of $E/E_k$. In N₂:O₂ the ionization length varies from approximately 0.1 mm for $1.5E_k$ to 0.01 mm for $3E_k$ whilst it amounts to 4 mm for $1.5E_k$ in N₂:CH₄ mixtures with 80% nitrogen. Hence, in $1.5E_k$ in mixtures with methane, the ionization length is comparable to the size of the simulation domain preventing the occurrence of a significant amount of ionization. Since ionization is less effective in mixtures with methane, the build-up of space charges and thus the formation of enhanced electric field tips is delayed which reduces the electron energies and the further drive of ionization. Note that the ionization coefficient and the ionization length for $3E_k$ in N₂:CH₄ is comparable to the ionization coefficient for $1.5E_k$ in N₂:O₂.

For the same time steps and fields as in Figs. 3 and 4, panels a–c in Fig. 7 show the electron energy distribution. The solid and dashed lines show the typical streamer-like energy distributions of electrons in air.
(Chanrion and Neubert, 2008) with maximum energies of \( \approx 50 \text{ eV} \) (1.5\( E_k \), a), \( \approx 65 \text{ eV} \) (2\( E_k \), b) and \( \approx 80 \text{ eV} \) (3\( E_k \), c). However, for the same \( E_{\text{amb}}/E_k \) (remember that \( E_k \) is smaller in mixtures with methane), the maximum electron energies in N\(_2\):CH\(_4\) are \( \approx 15 \text{ eV} \) (a), \( \approx 20 \text{ eV} \) (b) and \( \approx 30 \text{ eV} \) (c), thus only a little above the ionization energy of nitrogen (15.6 eV) and of methane (12.6 eV). Hence, the ionization is not effective enough to create high field tips to accelerate electrons into the energy regime where they can further create a substantial electron multiplication. Comparing the electron numbers below 1 eV in N\(_2\):CH\(_4\) reveals that in an ambient field of 1.5\( E_k \), the electron number does not change significantly because of inefficient ionization whereas in a field of 3\( E_k \), the electron number increases significantly as a function of time.

Fig. 8 shows the electron density and electric field in N\(_2\):CH\(_4\) with 20% nitrogen. It shows that in all considered cases negative and positive streamer fronts form. Fig. 7d compares the electron energy distribution for \( \kappa = 0.2 \) and \( \kappa = 0.8 \) for the same fields and time steps as in Fig. 8. It shows that in all cases, the maximum electron energy is larger for \( \kappa = 0.2 \) than for \( \kappa = 0.8 \) which results from the dependence of the friction force on the percentage of nitrogen. Fig. 1c shows that the friction force in N\(_2\):CH\(_4\) has a resonance at approximately 2 eV enhanced for \( \kappa = 0.8 \), reducing the electron energies. In addition, Fig. 2 shows that the breakdown field is slightly higher for \( \kappa = 0.2 \) than for \( \kappa = 0.8 \). Consequently, since the electron energies are larger for \( \kappa = 0.2 \), the ionization of the ambient gas is more probable and the

**Fig. 5.** The velocity of the positive (first column) and negative front (second column) as a function of time for gas mixtures with 80% nitrogen.

**Fig. 6.** The drift velocity (a), the effective ionization coefficient (b) and the ionization length \( \Lambda_{\text{ion}} \) (c) as a function of the ratio of the applied electric field and breakdown field.
avalanche-to-streamer transition is facilitated.

For $\kappa = 0.2$, panels a and b in Fig. 9 show the streamer velocities in N$_2$:O$_2$ and N$_2$:CH$_4$ for all considered electric fields as a function of time. Although there is an avalanche-to-streamer transition for all field strengths, streamers move faster in oxygen than in methane. As for $\kappa = 0.8$, the streamer velocities equal $\approx 100 - 10^1$ mm ns$^{-1}$ in oxygen whilst they lie between $10^{-1}$ and approximately $100$ mm ns$^{-1}$ in the nitrogen-methane mixture. Panels c) and d) additionally show the front velocities in N$_2$:CH$_4$ in an ambient field of $3E_k$ for different percentages of nitrogen. They illustrate that both positive and negative fronts move faster in mixtures with a low percentage of nitrogen or equivalently with a significant contribution of methane. Since the breakdown electric field does not vary much as a function of $\kappa$, we explain this with the friction force and its dependency on $\kappa$. As we have discussed in Section 2.3, the friction force has a resonance at an electron energy of approx. 2 eV which is distinct for large percentages of nitrogen. Subsequently, electron energies are lower and the fronts move slower in mixtures with high percentages of nitrogen. Equivalently fronts move substantially faster in mixtures with a significant concentration of methane.

3.2. The inception of streamers on Titan

After comparing the inception and evolution of bidirectional streamers in different N$_2$:CH$_4$ and N$_2$:O$_2$ mixtures, we now focus on the evolution of plasma patches and their transition to bidirectional streamers on Saturn's moon Titan, hence in N$_2$:CH$_4$ with 98.4% nitrogen. Fig. 10 shows the electron density and the electric field in different ambient fields; we here would like to remind the reader that the number density of ambient molecules is $2.9 \cdot 10^{25}$ m$^{-3}$ which corresponds to 20 km altitude on Titan, i.e. typical cloud altitudes in its atmosphere. As supplementary material, we have added movie files displaying the temporal evolution of the electron density and the electric field for the cases presented in Fig. 10. For comparison, the last column shows the electron density and the electric field in N$_2$:O$_2$ for the same number density of ambient gas molecules. Similar to $\kappa = 0.8$, we observe the avalanche-to-streamer transition in N$_2$:CH$_4$ only for fields above $2E_k$. As for $\kappa = 0.8$, the ionization length in fields below $2E_k$ is longer in mixtures with methane, thus the ionization is delayed and subsequently also the formation of enhanced field tips. In fields $\leq 2E_k$, there is a distinct motion of electrons towards the positive electrode only; there is no motion of the positive front at all. However, the field is enhanced at the positive front and shielded at the negative front suggesting that there will not be any avalanche-to-streamer transitions at later times. Fig. 11 shows the electron energies after the same time steps and in the same electric fields as in Fig. 10. The maximum electron energy is approximately 20 eV for fields smaller than $2E_k$, thus there is no efficient drive of ionization.

For fields above $2E_k$, we observe an avalanche-to-streamer transition within the borders of the simulation domain. However, comparing the evolution on Titan (third column) and in N$_2$:O$_2$ (fourth column), reveals that both streamer fronts move significantly slower in Titan's
$E_{\text{amb}} = 1.5E_{k}, t = 5.12 \, \text{ns}$  $E_{\text{amb}} = 2E_{k}, t = 3.01 \, \text{ns}$  $E_{\text{amb}} = 3E_{k}, t = 1.27 \, \text{ns}$

Fig. 8. The electron density (first row) and the electric field (second row) in $N_2:CH_4 = (20\%):(80\%)$, i.e. $\kappa = 0.2$, in different electric fields after different time steps.

a) $\kappa = 0.2$, negative  

b) $\kappa = 0.2$, positive

c) $E_{\text{amb}} = 3E_{k}$, negative  

d) $E_{\text{amb}} = 3E_{k}$, positive

Fig. 9. a, b) The velocity of the negative (a) and positive front (b) as a function of time for gas mixtures with $\kappa = 0.2$ nitrogen. c, d) The velocity of the negative and of the positive front in $N_2:CH_4$ in an ambient field of $3E_{k}$ for different percentages of nitrogen.
atmosphere. Additionally, the electron density in N2:CH4 is smaller and branching is favored. The dot-dashed and dotted lines in Fig. 11 compare the electron energies for these two cases. There is a significant number of electrons above 20 eV resulting in more electron impact ionization. However, as a consequence of the friction force, the number of electrons above 20 eV is amplified in N2:O2 in comparison to N2:CH4 which accelerates the formation of a double-headed streamer. Furthermore, the less probable photoionization in N2:CH4 additionally delays the streamer development.

4. Conclusions and outlook

We have investigated the motion of electrons and the streamer inception in N2:CH4 and in N2:O2 mixtures with number densities of 2.9 · 10^{25} m^{-3} with different percentages κ of nitrogen in ambient fields of 1.5E_k, 2E_k and 3E_k. Whilst streamers form for all considered cases in N2:O2, we observe the streamer inception in N2:CH4 mixtures depending on κ and the ambient field E_{amb}. Table 1 shows which combinations of κ and E_{amb} favor the formation of double-headed streamers in N2:CH4 within the simulation domain. There are two scenarios: For small percentages of nitrogen, fields as low as 1.5E_k are sufficient to incept streamers; if the percentage of nitrogen is increased, higher and higher fields are required. Ambient fields slightly above the breakdown field, where the rate of ionization is higher than the rate for attachment, the effective ionization coefficient for large κ is not sufficient to effectively ionize the ambient gas within the simulation domain. For large percentages of nitrogen and small fields, the ionization length can be larger than or comparable to the size of the simulation domain preventing us from observing the inception of streamers.

Considering that for all κ, the breakdown field in N2:CH4 is approximately half as large as the breakdown field in N2:O2 and that the friction force below 3 eV is larger in N2:CH4, fronts move one to two orders of magnitude faster in nitrogen-oxygen mixtures than in nitrogen-methane mixtures independent of whether we observe an avalanche-to-streamer transition. As an additional effect, photoionization is less effective in N2:CH4, hence, the motion of the fronts is further

![Fig. 10. The electron density (first row) and the electric field (second row) in N2:CH4 = (98.4%):(1.6%) (columns one to three) and in N2:O2 = (98.4%):(1.6%) (fourth column) in different ambient fields after different time steps.](image)

![Fig. 11. The energy distribution for κ = 0.984 for the same fields and time steps as in Fig. 10.](image)

<table>
<thead>
<tr>
<th>κ</th>
<th>E_{amb} 1.5E_k</th>
<th>2E_k</th>
<th>3E_k</th>
</tr>
</thead>
<tbody>
<tr>
<td>20%</td>
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<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>40%</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>60%</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>80%</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>98.4%</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
</tr>
</tbody>
</table>

1.5E_k, 2E_k and 3E_k. Table 1 shows which combinations of κ and E_{amb} favor the formation of double-headed streamers in N2:CH4 within the simulation domain. There are two scenarios: For small percentages of nitrogen, fields as low as 1.5E_k are sufficient to incept streamers; if the percentage of nitrogen is increased, higher and higher fields are required. Ambient fields slightly above the breakdown field, where the rate of ionization is higher than the rate for attachment, the effective ionization coefficient for large κ is not sufficient to effectively ionize the ambient gas within the simulation domain. For large percentages of nitrogen and small fields, the ionization length can be larger than or comparable to the size of the simulation domain preventing us from observing the inception of streamers.
damped.

On Titan with methane percentages between 1.4% and 5%, we do not observe any streamer inception for ambient fields below $\sim 3E_1$ which equals a field strength of 4.2 MV m$^{-1}$. Simulations have calculated large scale electric fields as high as 2 MV m$^{-1}$ in Titan's atmosphere (Tokano et al., 2001). Thus, at first glance it seems that streamer inception is not feasible in Titan's atmosphere. However, one may not forget that typical large scale electric fields in Earth's thunderclouds are typically in the order of 0.1–0.2 MV m$^{-1}$ (Marshall et al., 1995, 2005) whereas the classical breakdown fields at cloud altitudes vary between approximately 2.0 MV m$^{-1}$ at 4 km altitude and 0.5 MV m$^{-1}$ at 16 km altitude, thus approximately an order of magnitude larger. Although the exact mechanism of lightning initiation on Earth is still under debate (Gurevich and Karashtin, 2013; Dubinova et al., 2015), its existence, altitude, thus approximately an order of magnitude larger. Although the classical breakdown field which is still uncertain since it is only provided by models, but not by direct measurements. Moreover, even if we conclude the existence of small (cm-long) streamer discharges in Titan's atmosphere, this does not allow us to conclude about the existence of lightning. Although their existence cannot be ruled out completely, 127 flybys of Cassini did not reveal any traces of lightning (Fischer, 2018). Thus, either lightning was too weak to be detected (Fischer and Gurnett, 2011; Fischer, 2018), or it was not present at all because of the high field needed to incite streamers. Since even on Earth, the streamer-to-lightning-leader transition is not fully understood yet (da Silva and Pasko, 2013), we propose further work to study this transition in Titan's atmosphere.

Since the primordial atmosphere of Earth had a similar chemical composition as Titan's atmosphere, our model here allows us to also study the inception of streamers on the early Earth.

We here speculate that similar to the processes in terrestrial streamer discharges, run-away electrons and subsequently X-rays might be produced in Titan's atmosphere. In future work, we will estimate the occurrence and the fluence of these phenomena related to Titan γ-ray flashes (TGRFs) and discuss their effect on Titan's atmosphere.

The model presented in this manuscript also allows to study the streamer inception in different atmospheres, for example, of exoplanets (Bailey et al., 2014; Hodosán et al., 2016a,b), provided appropriate cross sections for the scattering of electrons of the atmospheres' constituents are known. Hence, in future work, we strive to investigate which known exoplanets are likely to show discharge phenomena and also tackle the question of associated high-energy beams.

Acknowledgments

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Appendix A. Supplementary data

Supplementary data to this article can be found online at https://doi.org/10.1016/j.icarus.2019.05.036.

References

Boljokavac, D., Simonović, I., Petrović, Z., Zrinskii, C., Agrač, N., Uršić, M., 2016. Titan’s electric field which is still uncertain since it is only provided by models, but not by direct measurements. Moreover, even if we conclude the existence of small (cm-long) streamer discharges in Titan’s atmosphere, this does not allow us to conclude about the existence of lightning. Although their existence cannot be ruled out completely, 127 flybys of Cassini did not reveal any traces of lightning (Fischer, 2018). Thus, either lightning was too weak to be detected (Fischer and Gurnett, 2011; Fischer, 2018), or it was not present at all because of the high field needed to incite streamers. Since even on Earth, the streamer-to-lightning-leader transition is not fully understood yet (da Silva and Pasko, 2013), we propose further work to study this transition in Titan’s atmosphere.

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