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Published in:
Proceedings of the National Academy of Sciences of the United States of America

Link to article, DOI:
10.1073/pnas.1802155115

Publication date:
2018

Document Version
Publisher's PDF, also known as Version of record

Link back to DTU Orbit

Citation (APA):
Contributions of the glycocalyx, endothelium, and extravascular compartment to the blood–brain barrier

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Edited by Berislav V. Zlokovic, University of Southern California, Los Angeles, CA, and accepted by Editorial Board Member Marcus E. Raichle August 16, 2018 (received for review February 8, 2018)

The endothelial cells that form the blood–brain barrier (BBB) are coated with glycocalyx, on the luminal side, and with the basement membrane and astrocyte endfeet, on the abluminal side. However, it is unclear how exactly the glycocalyx and extravascular structures contribute to BBB properties. We used two-photon microscopy in anesthetized mice to record passive transport of four different-sized molecules—sodium fluorescein (376 Da), Alexa Fluor (643 Da), 40-kDa dextran, and 150-kDa dextran—from blood to brain, at the level of single cortical capillaries. Both fluorescein and Alexa penetrated nearly the entire glycocalyx volume, but the dextrans penetrated less than 60% of the volume. This suggested that the glycocalyx was a barrier for large but not small molecules. The estimated permeability of the endothelium was the same for fluorescein and Alexa but several-fold lower for the larger dextrans. In the extravascular compartment, co-localized with astrocyte endfeet, diffusion coefficients of the dyes were an order of magnitude lower than in the brain parenchyma. This suggested that the astrocyte endfeet and basement membrane also contributed to BBB properties. In conclusion, the passive transport of small and large hydrophilic molecules through the BBB was determined by three separate barriers: the glycocalyx, the endothelium, and the extravascular compartment. All three barriers must be taken into account in drug delivery studies and when considering BBB dysfunction in disease states.

blood–brain barrier | glycocalyx | astrocytes | diffusion | permeability

The blood–brain barrier (BBB) is a unique defense system that protects the brain from harmful agents and pathogens. Unfortunately, the BBB also restricts entry of a wide range of drugs developed to treat brain diseases. Tracer kinetic analysis was developed to quantify whole-brain uptake of compounds, but that technique has provided little information about the microstructure of the BBB (1–4). Advances in confocal and two-photon fluorescence imaging have allowed researchers to study the BBB at the microscopic level, on scales that range from an entire brain region down to a single vessel (5–8).

The majority of two-photon microscopy studies of BBB permeability have focused on imaging a brain region (typically spanning several hundred microns) and recording fluorescence intensities from extra- and intravascular compartments. Those data allowed calculations of BBB permeability based on theoretical models (7, 9, 10). In those models, BBB permeability was described as an average property of all vessels in the imaged region.

Those experiments could not resolve the contributions of individual vessels and even less the composition of the barrier. Several studies have, however, suggested that, in addition to the vascular endothelium, structures associated with the endothelium might also act as barriers (11–16). These structures include the endothelial glycocalyx, basement membrane, and astrocyte endfeet.

Here, we hypothesized that the BBB consists of a sequence of barriers, each limiting blood-to-brain transport of small and large molecules. To test this hypothesis, we performed high-resolution two-photon imaging of single capillaries and introduced fluorescent dyes into the bloodstream. We also used different fluorescent dyes to label the glycocalyx and astrocyte endfeet, which enabled us to associate fluorescent tracers that crossed the BBB with each anatomical component. Our data suggested that the BBB consisted of at least three different barriers that individually affected BBB permeability. The properties of this “tripartite” BBB should be considered when designing the delivery of large drug molecules and when studying disease states.

Results

Imaging Setup. We used fast-scanning two-photon microscopy to record real-time images of single brain blood vessels oriented perpendicular to the focal plane. During these recordings, we continuously injected fluorescent dyes into the blood (Fig. 1A and B). We evaluated changes in the distribution of fluorescence intensity outside the vessel, caused by the dye traversing the BBB. We performed this evaluation with a theoretical model (see Theon), based on the cylinder concept developed by Krogh. This model was designed to analyze the blood-to-brain transfer of an inert, diffusible solute that could permeate blood vessel walls (17). A blood vessel was modeled as an infinite cylinder inside a medium that was rotationally symmetric about the vessel (Fig. 1C). Therefore, we only analyzed data from blood vessels that were oriented perpendicular to the focal plane (Fig. 1D). To assist in the interpretation of the recorded images, we estimated the resolution of our microscope inside the brain.

Significance

The vascular endothelium constitutes the main barrier that restricts the transport of molecules from blood to brain. However, the barrier properties of structures adjacent to the vascular endothelium are understudied. Based on two-photon microscopy imaging of single cortical capillaries, we found that the blood–brain barrier (BBB) consisted of at least three elements: the endothelial glycocalyx, which forms a barrier on the blood side to large but not small molecules; the endothelium; and the basement membrane and astrocyte endfeet—the final line of defense on the brain side. All three elements restricted permeation of large molecules and should be taken into account when studying drug delivery and disease states.

Author contributions: N.K., H.F., and M.L. designed research; N.K. performed research; N.K. and H.F. analyzed data; and N.K., H.F., and M.L. wrote the paper.

The authors declare no conflict of interest.

This article is a PNAS Direct Submission. B.V.Z. is a guest editor invited by the Editorial Board.

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This article contains supporting information online at www.pnas.org/lookup/suppl/doi:10.1073/pnas.1802155115/-/DCSupplemental.

Published online September 14, 2018.
We hypothesized that the entire region that separates the vessel lumen from the brain parenchyma contributes to the BBB (Fig. 2A). Thus, the glycocalyx on the luminal side of the endothelium, the endothelium itself, and the extravascular compartment all contribute to the BBB. We found experimental support for this hypothesis as follows.

We located these three compartments in images by locating the endothelial glycocalyx and the astrocyte endfeet. To this end, the glycocalyx was labeled with Alexa Fluor (AF) 594-conjugated wheat germ agglutinin (WGA-Alexa; red in Fig. 2B), and the endfeet were labeled with sulforhodamine 101 (SR101; green in Fig. 2B). Then we analyzed the distribution across the three compartments independently for each of four diffusing dyes. Fig. 2C shows the distribution of one of the dyes, the 150-kDa fluorescein isothiocyanate-dextran (Dex150).

We based our definition of the extravascular compartment on the values we found for the diffusion coefficients in this region and the large difference between these values and the values found in the brain parenchyma. Starting at the peak of the fluorescence emitted by astrocyte endfeet (dashed circle in Fig. 2A), our extravascular compartment spanned the region, in which the experimental distribution of fluorescence agreed with the fitted solution to Eq. 1. Note that this fitted solution assigns a given dye a diffusion coefficient that is constant in time and space throughout the compartment. This simple but demanding property defines the compartment.

This extravascular compartment did not include the space closest to the vascular endothelium, because there, the distributions of fluorescence were not typically rotationally symmetric. Moreover, we could not determine an exact boundary between the extravascular compartment and the brain parenchyma from our data. We believe that a continuous transition between the two spaces was more likely.

We treated the space between the glycocalyx and the extravascular compartment as a single compartment, called “the
endothelium" (see Fig. 2D). Based on the anatomy of the neurovascular unit (18, 19), this space, in addition to the vascular endothelium, may contain fragments of basement membrane, perivascular space, and pericytes, which we did not identify on our fluorescence images.

Our definitions of the endothelium and the extravascular compartment were based not on their anatomy but on their functional transport properties (permeability and diffusion coefficients) revealed by our data. The third compartment that we studied was the glycocalyx, located between the vessel lumen and the endothelium (see Fig. 2D).

**Estimation of the Glycocalyx Partition Coefficient.** We defined the partition coefficient, \( \alpha_g \), as the ratio of two fluorescence intensities. The first intensity was the Dex150 fluorescence at the point that it coincided with the peak of the WGA-Alexa fluorescence, which labeled the glycocalyx (Fig. 2D); the second intensity was the Dex150 fluorescence in the plasma, at the middle of the vessel. Thus, the \( \alpha_g \) could be interpreted as the fraction of glycocalyx volume that was accessible to the dye-containing plasma (20). Fig. 2D shows that the fluorescence intensity of Dex150 was uniform in the center of the vessel, but it dropped by almost 50% in the glycocalyx. Fig. 3 A–F summarizes the values obtained for \( \alpha_g \) with all four dyes, and SI Appendix, Fig. S8 discusses potential sources of bias in these estimates. We found no difference in \( \alpha_g \) between sodium fluorescein (NaF; mean ± SEM: 0.93 ± 0.02) and AF (mean ± SEM: 0.91 ± 0.02). For both NaF and AF, \( \alpha_g \) values were roughly twice as large as the \( \alpha_g \) value of 40-kDa fluorescein isothiocyanate-dextran (Dex40; mean ± SEM: 0.56 ± 0.03) and Dex150 (mean ± SEM: 0.44 ± 0.03). Dex40, which was smaller than Dex150, penetrated the glycocalyx more efficiently than Dex150 (Fig. 3F). When we treated the glycocalyx with the enzyme hyaluronidase, \( \alpha_g \) of Dex150 increased from 0.44 ± 0.03 (mean ± SEM) to 0.80 ± 0.05 (mean ± SEM; Fig. 3F), which was consistent with the findings reported by Henry and Duling (21).

**Diffusion Explains the Observed Transport of Fluorescent Dyes in the Extravascular Compartment.** For the quantitative analysis of dye diffusion, we applied polar coordinates with origin in the center of the vessel (SI Appendix, Fig. S1). We found that the instantaneous distributions of fluorescence did not depend on the polar angle. This rotational symmetry of the data simplified the ensuing analysis by making the radial dimension the only spatial dimension of relevance. By allowing us to average data values over the polar angle, the rotational symmetry also improved the statistics of data. This made it more challenging to fit a model to data and hence more significant that we achieved to do so.

Fig. 3G and H shows how Dex150 traverses the brain endothelium and travels beyond the astrocyte endfoot when a sufficiently large concentration gradient is created across the BBB. We collected and analyzed data from vessels loaded with NaF, AF, Dex40, or Dex150. We found that the changes in fluorescence intensity, \( I_{ev} \), for both NaF and Dex150 (mean ± SEM) were roughly twice as large as the \( \alpha_g \) value of 40-kDa fluorescein isothiocyanate-dextran (Dex40; mean ± SEM: 0.56 ± 0.03) and Dex150 (mean ± SEM: 0.44 ± 0.03). Dex40, which was smaller than Dex150, penetrated the glycocalyx more efficiently than Dex150 (Fig. 3F).

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Permeability of the Vascular Endothelium. We estimated the permeability, $P$, of the vascular endothelium, as described in Fig. 4 C and D (see also Theory). The quality of the one-parameter fits shown in Fig. 4 C and D demonstrated that i) our interpretation of the space-time distribution of fluorescence outside the blood vessel showed that the flux away from the vessel was simply proportional to the independently observed fluorescence inside the vessel;
After no. 40

The BBB that emerged from this analysis can be thought of as three Ohmic resistors connected in series: the glycocalyx, the endothelium, and the extravascular compartment (Fig. 24). A concentration difference across the BBB corresponds to a voltage difference across the three resistors. The flux of molecules across the BBB corresponds to the electrical current through the three resistors. This analogy is deep, because permeability and conductance are simply different names for parameters that quantify a linear relationship between cause (difference in voltage/concentration) and effect (current/flux). Thus, because the glycocalyx and extravascular compartments function as barriers in comparison with the vessel lumen and the parenchyma, they reduce the concentration difference across the endothelium, and hence, they reduce the flux through it. This effect is greater for larger molecules, because they encounter greater resistance in the glycocalyx. Moreover, as the resistance in the extravascular compartment slows diffusive transport away from the blood vessel, potential pathogens may be exposed to immune cells near the blood vessel for a longer time.

In Vivo Estimates of Fluorophore Partitioning into the Glycocalyx Provide a Better Description than Glycocalyx Thickness. We reported glycocalyx partition coefficients for fluorescent dyes entering into the glycocalyx in single vessels in vivo. In our opinion, this coefficient is more descriptive than the glycocalyx thickness or related quantities reported elsewhere (15, 21, 28–30). The partition coefficient is specific to individual molecules, and it can be interpreted as the fraction of the glycocalyx volume that is accessible to the specific molecule. In contrast, the glycocalyx thickness does not contain molecule-specific information. We propose that the partition coefficient can be interpreted in terms of the glycocalyx microstructure. Electron microscopy images have demonstrated that the glycocalyx is a collection of dense, bush-like structures, which cover the surface of an endothelial cell (31, 32).

We showed that NaF and AF distributed nearly throughout the entire glycocalyx volume, which indicated that the glycocalyx did not serve as a barrier to small molecules, like NaF and AFs; instead, the glycocalyx was essentially equivalent to blood plasma. However, based on our results with Dex40 and Dex150, larger molecules were less able to penetrate the dense glycocalyx structures. An integration of the fluorescence signals over low- and high-density regions showed that Dex150 fluorescence in the glycocalyx was 44% of its intensity in the blood plasma (Fig. 3F).

When a molecule has a low glycocalyx partition coefficient, it may only reach a fraction of the endothelial surface, which reduces its flux through the BBB and, consequently, its total brain uptake. Our results were supported by the findings of Vink and Duling, who demonstrated that small dyes and low-molecular weight dextrans could penetrate the glycocalyx of cremaster muscle capillaries, but 70 kDa anionic and neutral dextrans were confined to the central part of the capillary (11, 33).

Knowledge of the glycocalyx partition coefficient might increase the accuracy of measurements of the glycocalyx thickness. Previously, these measurements typically relied on the assumption that high-molecular weight anionic dextrans (like 70-kDa dextran) could not permeate the glycocalyx (30). Nieuwdorp et al. (34) developed a quantitative approach for measuring the glycocalyx volume in human patients. They assumed that a reference fluorescent dye could distribute throughout the entire glycocalyx volume. In a review of that approach, Michel and Curry (20) questioned that assumption and suggested that a method for measuring the glycocalyx partition coefficient was required. In the present study, we have provided that method.

The Extravascular Compartment Is also a Diffusion Barrier. After a molecule in the blood has traversed the glycocalyx and the endothelium, it encounters the extravascular compartment. With the simplest possible reaction–diffusion model, we showed that, for the four fluorescent dyes we studied, the diffusion coefficients in the extravascular compartment were approximately one order of magnitude lower than the diffusion coefficients of similar-sized compounds in the brain parenchyma (22, 25).

Once a molecule has crossed the endothelium, we expect a significant increase in the geometric path length of its radial diffusion: Instead of diffusing radially, the molecule is forced to travel along the astrocyte endfeet (and possibly the pericyte membrane) to find the exit points between the neighboring
**endfeet (Fig. 2A).** Moreover, astrocyte endfeet are connected to each other through gap-junctions, and they are connected to endothelial cells through complex interactions with the basal lamina and extracellular matrix (figure 3 in ref. 18). This tight complex may serve as an additional barrier to compounds that cross the vascular endothelium (18, 19, 35, 36). Indeed, Nuriya et al. (15) demonstrated that astrocyte endfeet formed a barrier for compounds moving from the brain parenchyma to the blood.
vessel. Several studies have also shown that compounds in the perivascular spaces (19) were hindered in a size-dependent manner (16, 37), consistent with the size dependence of the diffusion coefficients we observed (Table 1).

Convective transport occurs in the perivascular spaces of large brain vessels and inside the brain ventricles (37–41), but it is debatable whether convection is important for the transport of compounds within the brain parenchyma (18, 42). Here, we demonstrated that the local fluorescence intensity in the extravascular compartment changed over time and space in a manner consistent with simple diffusion. The radial diffusion coefficient was constant in space and time. Consequently, we could exclude convection as a mechanism of transport.

Diffusion coefficients in the brain parenchyma are typically estimated by injecting a fluorescent dye through a pipette and modeling the spatiotemporal changes in local fluorescence. That approach assumes that the medium is homogeneous and isotropic across hundreds of microns around the injection site (22, 43). On the other hand, to simplify our calculations for the extravascular compartment, we only needed to assume that the medium was rotationally invariant with respect to rotations around the center of the vessel; thus, we only studied vessels that exhibited this property. Because the radial span of the vessel was only a few microns, we assumed, and we could confirm, that the vessel was the only source of fluorescent dye in a given extravascular compartment. However, on a larger spatial scale, all blood vessels are sources of fluorescence in the brain, which makes modeling prohibitively complex. This complexity prevented us from analyzing diffusion in the brain parenchyma based on fluorescence.

Shi et al. estimated the diffusion coefficients of fluorescent dyes in the space surrounding cerebral blood vessels. They reported values that agreed well with diffusion coefficients previously reported for the brain parenchyma. However, although they used a radial diffusion model that assumed rotational symmetry with respect to the vessel, their image data (figure 4a in ref. 8) showed an absence of the symmetry, which challenges the accuracy of their estimates. Our results suggested two different diffusion coefficients for each dye. One coefficient described diffusion in the extravascular compartment, and the other described diffusion in the brain parenchyma. Single-molecule tracking microscopy has been used for measuring both diffusion coefficients for a single dye molecule (44). That approach would have high reliability because it would not require switching methods between measurements (45).

**Vascular Endothelium Permeability from Two-Photon Images.** Early quantitative methods showed that the permeability of blood vessels in the brain was much smaller than in other tissues (46, 47). Currently, microscopic imaging methods are routinely used to estimate BBB permeability both in vitro (48, 49) and in vivo (7–9, 50). In the present work, we injected fluorescent dyes intravasally (i.v.), which resulted in minimal interference with cerebral blood flow compared with other in vivo methods (8, 50). We developed a method for measuring the resulting plasma fluorescence intensity directly from images without red blood cells. For diffusion in the vessel periphery, we measured only the fluorescence close to the vessel (3–5 μm), and the experiments were brief (1–2 min). Thus, we effectively eliminated any potential contributions to the observed fluorescence from vessels other than the one on which we focused. Finally, we identified some anatomical components of the BBB and separated the glycocalyx and extravascular components from the measurement of vascular endothelium permeability.

The permeabilities presented here were within an order of magnitude of permeabilities reported previously for fluorescent dyes of similar size, both in vivo (8, 50–52) and in vitro (48, 49, 53, 54). In particular, our estimation of Dex40 permeability (1.40 ± 0.15 × 10⁻⁷ cm/s) agreed well with other in vivo estimates of 1.15 ± 0.23 × 10⁻⁷ cm/s (table 1 in ref. 8) and 1.7 ± 0.9 × 10⁻⁷ cm/s (table 1 in ref. 50). Our permeability for Dex150 (0.51 ± 0.14 × 10⁻⁷ cm/s) was, as expected, lower than that for Dex70 and higher than that of IgG (table 1 in ref. 8). Yuan et al. and Shi et al. (8, 50) reported a higher BBB permeability for NaF than our value. However, they studied postcapillary venules, which were shown to exhibit loose BBB architecture compared with capillaries (55); hence, venules are expected to have higher BBB permeability than capillaries.

Our finding that estimated permeabilities declined with increasing dye size (Table 1) was consistent with a paracellular transport mechanism. It was not surprising that high-molecular weight polymers, particularly dextrans, could move through narrow spaces that are smaller than their size, estimated by the hydrodynamic radius or the radius of gyration, because the properties of linear polymers differ from those of rigid particles of similar size (see SI Appendix, Using Fluorescently Labeled Dextrans as Probes to Study Transport in Brain Tissue). The polymer coil can thread through tight and narrow spaces, by starting at one of its ends or by starting with a “hernia.” For example, one can directly visualize how a single 48.5-kbp DNA diffuses through pores that are approximately seven times smaller than its radius of gyration (figure 5 in ref. 56). Indeed, experimental data from glomerular capillaries showed higher permeability for dextrans than for proteins of similar size (57–60). However, the probability of dextran passage through the narrow BBB spaces is much smaller than that of a compact molecule with a diameter similar to a dextran monomer. This low probability results in very small, but experimentally measurable, BBB permeabilities to large dextrans.

Another way to cross the BBB is through an endothelial cell. Particularly, fluid-phase endocytosis has been used to explain how some proteins and dextrans can penetrate the BBB (61, 62). If this transport is not limited by the number of vesicles available for endocytosis, one may expect the flux of dextran through the BBB to be proportional to the concentration of dextran in the blood. Consequently, this contribution to the flux of dextran across the BBB is inseparably included in the permeability we measure (Fig. 4 C and D).

For hydrophobic compounds that can diffuse through the endothelial cell membrane, a threshold exists in the 400–600 Da range, which could supposedly distinguish BBB-permeable from BBB-nonpermeable molecules (63). We found no evidence for such a threshold for hydrophilic NaF (376 Da) and AF (643 Da) (Table 1). Our data indicate that the endothelium permeability for hydrophilic compounds depends more smoothly on molecular weight and that the differences in the total flux of a compound through the BBB depends also on its glycocalyx partition coefficient and on its diffusion coefficient in the extravascular compartment.

Finally, we showed that mannitol did not change the diffusion coefficient in the extravascular compartment but produced a more than twofold increase in endothelium permeability. Our results supported the hypothesis that mannitol induced endothelial cell shrinkage, which then increased the paracellular permeability (64).

**Limitations of the Model.** The method of analysis developed here applies only to vessels that are oriented perpendicular to the focal plane. These vessels were not expected to differ from vessels with different orientations. Larger vessels are scarcer than small capillaries; thus, it might be challenging, and hence time-consuming, to find a large vessel with a cylindrical shape and a perpendicular orientation. Our method also demanded rotational invariance in the distribution of fluorescence around the vessel. In the case of the mannitol-disrupted BBB, this demand was not satisfied for a large fraction of...
we used NaF (Sigma-Aldrich; 1% solution in saline), AF 488 (AF; 1 μM and 20 μM), and Fig. S3 shows that, in the brain, at depths from 50 to 200 μm, the estimated N.A. values were 1.05, 1.01, and 1.00, respectively. The fitted values of N.A. were estimated using quantum dots conjugated with WGA lectin, which binds to the endothelial glycoprotein. After a bolus injection of quantum dots (100 μL of a 5-nM solution), we could identify quantum dots in clusters or in isolation, sparsely covering the inner surfaces of vessels. The studied vessel is the only source of diffusing compound in the imaging region.

Our method for in situ estimation of the resolution of a two-photon microscope may be useful for other studies that use high-resolution imaging in the brain. In comparison with the injection of quantum dots or fluorescent beads into the brain with a pipette, our method is less invasive and technically simple (it requires only single i.v. injection), and it can be used for routine checks of resolution.

**Theory.** Our model was based on the following assumptions, which are similar to those of Krogh's cylinder model (17, 22):

i) The vessel has a cylindrical shape and is oriented perpendicular to the focal plane.

ii) The distribution of fluorescence intensity in the extravascular compartment has cylinder symmetry.

iii) Diffusion is the only mechanism of transport in the extravascular compartment.

iv) The studied vessel is the only source of diffusing compound in the imaging region.

v) The vessel's diameter does not change during the experiment.

vi) Loss of fluorescence by photobleaching or otherwise can be described well with the data obtained with a relatively high-N.A. objective (N.A. = 1.4) has been explained theoretically and shown experimentally (70, 71). Consequently, we estimated the resolution of the microscope with theoretical values for the full-width-at-half-maximum (FWHM) of the microscope’s theoretical PSFs (table 1 and equation 3 in ref. 69). The estimated resolutions, measured from quantum dots on a glass slide, were ΔXY = 0.28 μm and ΔZ = 1.06 μm.

As in other turbid media, imaging in the brain deteriorates with increasing depth in both lateral and axial resolutions. We collected fluorescence intensities at the interface between blood and brain tissues. There, one may expect a further reduction in resolution, due to a mismatch of refractive indices. To estimate the two-photon microscope's resolution there, we used quantum dots conjugated with WGA lectin, which binds to the endothelial glycoprotein. After a bolus injection of quantum dots (100 μL of a 5-nM solution), we could identify quantum dots in clusters or in isolation, sparsely covering the inner surfaces of vessels. The studied vessel is the only source of diffusing compound in the imaging region.
The flux, \( J(t) \), of a fluorescent dye through a unit surface of the BBB is proportional to its permeability, \( P \):

\[
J(t) = P \left( C_G(t) - C_B(t) \right),
\]
where \( C_G(t) \) and \( C_B(t) \) are the concentrations of the fluorescent dye in the glycosylation and at the inner surface of the extravascular compartment, respectively (Fig. 2D). We assumed that the measured fluorescence intensity \( I(t, r) \) was proportional to the dye concentration, \( I(t, r) = K^{-1} C(t, r) \), where \( K \) was the proportionality constant.

When the dye was distributed only in the extravascular spaces, not in cells, the coefficient \( \alpha \) could be introduced to estimate the volume fraction of the extravascular spaces, relative to the total volume of the tissue (43). Then, the relationship between the fluorescence intensity measured in the extravascular compartment of a vessel, \( I_{ev}(t) \), and the concentration of the dye, \( C_{ev}(t) \), could be calculated as \( C_{ev}(t) = K \alpha I_{ev}(t) \), where \( 0 < \alpha < 1 \). We assumed that only a fraction of the glycosylation volume, \( \alpha g \), was accessible to the fluorescent dye and that an equilibrium existed between the dye in the plasma and that in the glycosylation at all times. Accordingly, the dye's concentration in the glycosylation was \( C_G(t) = \alpha K I(t) \), where \( I(t) \) was the fluorescence intensity in blood plasma. Thus, \( J(t) \), from Eq. 2, could be expressed in terms of the measured fluorescence intensities as follows:

\[
J(t) = P \left( \frac{\alpha g}{\alpha} K I(t) - \frac{1}{\alpha} K I_{ev}(t) \right) = \alpha g P K I(t).
\]

The approximate expression was valid for the majority of datasets when \( I(t, r) \gg I_{ev}(t) \).

We used NaF, AF, Dex40, and Dex150 as fluorescent dyes. We assumed that the dyes moved freely within the vessel and had no interactions with any blood components (73, 74). We also assumed that the dyes, as hydrophilic molecules, could not permeate cell membranes but instead distributed in the extravascular spaces (22, 75).

We showed that the spread of fluorescence of the studied dyes in the extravascular compartment agreed well with the reaction–diffusion equation (Eq. 1). The effective diffusion coefficient, \( D^* \), was related to the diffusion constant in free medium (agarose gel), \( D \), and the tortuosity of the tissue, \( \lambda \), through \( \lambda^2 = D/D^* \) (43).

We placed the surface of our model cylinder at the location of the peak of the SR103 (astrocyte) fluorescence (Fig. 2D). There, we set a time-dependent boundary condition. SI Appendix, Fig. S5A shows an example of experimentally measured fluorescence intensity at the boundary, \( I(t, R) \), and its smoothed version, calculated with a locally weighted scatterplot smoothing regression.

The second boundary condition was defined by assuming a zero flux far \((R \rightarrow \infty) \) from the cylinder surface. This assumption holds when no molecule reaches \( R \) from the studied vessel or any other vessel during the experiment. In the numerical model, we placed \( R_m \) approximately 30 \( \mu \)m away from the cylinder surface; thus, \( R_m \gg R \).

A straightforward way to implement an initial condition for Eq. 1 is to use the measured fluorescence distribution at the initial time, \( I(t_0, R) \), but this approach has several disadvantages. First, like any experimentally measured intensity profile, the \( I(t_0, R) \) contained noise, which would influence the fitting, particularly at early times, before the irregularities of \( I(t_0, R) \) were smoothed by diffusion. Second, the reaction term \( K_i I(t, R) \) in Eq. 1 depended on the absolute value of fluorescence intensity, which could contain dye-independent autofluorescence. In general, measurements of fluorescence intensity contain both the dye fluorescence and nonspecific autofluorescence. See SI Appendix for more theory.