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Cooperative Rendezvous and Docking for Underwater Robots using Model Predictive Control and Dual Decomposition

Mikkel Cornelius Nielsen^{1,2}, Tor Arne Johansen¹, Mogens Blanke^{1,2}

Abstract—This paper considers the problem of rendezvous and docking with visual constraints in the context of underwater robots with camera-based navigation. The objective is the convergence of the vehicles to a common point while maintaining visual contact. The proposed solution includes the design of a distributed model predictive controller based on dual decomposition, which allows for optimization in a decentralized fashion. The proposed distributed controller enables rendezvous and docking between vehicles while maintaining visual contact.

I. INTRODUCTION

Intervention, maintenance, and repair (IMR) operations are an increasingly critical area of application in the offshore industry. Deployment of future sub-sea production facilities is anticipated to occur in deeper and more remote locations. The increased depth require more frequent maintenance, which is already a complicated task at places not directly accessible by humans. The offshore IMR operations are typically carried out by *Remotely-Operated-Vehicles* (ROVs). The vision of the complete autonomy in the future has increased the interest in *Autonomous-Underwater-Vehicles* with intervention capabilities (I-AUVs). Multiple recent projects have considered persistent autonomy for intervention-type marine vehicles.

The FP7 project PANDORA investigated the problem of physical intervention between underwater vehicles and underwater panels [16], [20]. The TRITON project investigated docking and manipulation between underwater vehicles and stationary facilities [21], [22].

Operating near exposed offshore structures involves considerable risk [32], [31]. The NextGenIMR project considered the mitigation of operational risk in autonomous interventions such as probability of mission success in case of degradation of the AUV during an active mission combined with shared control with human supervisors [29], [28]. Extending the autonomy to multiple I-AUVs could potentially allow for more flexible and fault-tolerant operations [7], [11]. Multi-vehicle systems with interaction capabilities would allow for smaller vehicles with more specialized tasks such as data-muling, transportation of tools, or collection of test samples [33]. In each case, the vehicles would have to rendezvous to make the

exchange while possibly solving another objective — such as structural monitoring — simultaneously.

Rendezvous and docking are not novel concepts, and multiple authors have considered docking for AUVs. However, the most classic examples are under-actuated torpedo type vehicles [2], [6] and [19], whereas the most common types of IMR vehicles are bulky and fully-actuated [4], [27]. The aeronautical literature has investigated rendezvous and docking for spacecrafts [17], [18], [24], [23], but does not consider damping forces due to the low drag coefficient of the thermospheric layer.

The issue of multi-vehicle rendezvous and docking with multiple objectives, input constraints, and visual constraints pose a challenging problem. Model Predictive Control (MPC) is an advanced control strategy often employed to solve problems where constraints pose a central issue in the objectives. Several authors, [5], [8], [12], have investigated distributed MPCs (DMPCs). Dual decomposition is a frequently applied method, which decomposes a large central optimization problem into smaller sub-problems that can be solved locally.

The decomposition transforms the coupled objective function into decoupled objective functions with coupling constraints. Afterwards, the constraints are relaxed using Lagrangian relaxation and the individual vehicles enforce the coupling constraints by manipulation of the dual variables. Multiple authors, [9], [26], [14], [10], have exploited the dual decomposition technique in various contexts. However, none have considered multi-vehicle docking.

This paper proposes a new multi-vehicle docking control strategy. The strategy utilizes a DMPC by dual decomposition to achieve rendezvous while the vehicles maintain visual contact with each other. The rendezvous problem is solved as a consensus problem solved by introducing a consensus point with a coupled equality constraint between the vehicles. Inspired by, [24] and [23], the visual constraint of the cameras are constructed as inequalities. The constraints are decomposed using dual decomposition and subsequently relaxed by Lagrangian relaxation. The dual variables are then updated by negotiation between neighboring vehicles to thereby enforce the relaxed constraints.

The organization of this paper is as follows: Section II describes the model dynamics used in the paper. Then the overall problem is presented in a centralized fashion in Section III. In Section IV the distributed controller is derived from the centralized problem using dual decomposition. Section V presents and discusses the results of the simulation.

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Finally, Section VI draws the conclusion along with possible future extensions of the study.

II. MODELING

This section starts by an assumption made to reduce problem to a planar case. The dive-plane is stabilized by an active attitude and heave control system. The vehicle considered in this paper is a horizontal plane model of three *degrees-of-freedom* (DOF). Two coordinate frames are considered, first the global navigation frame denoted by $\{n\}$ is approximated by a local earth-fixed North-East plane and secondly body-fixed frames attached to each of the vehicles such that the frames are aligned with the principle axes. The pose of a vehicle in the global frame is denoted $\boldsymbol{\eta}$ is defined as follows:

$$\boldsymbol{\eta} = [N, E, \psi]^T, \quad (1)$$

where N and E are the position coordinates in the North-East frame and ψ is the yaw-angle relative to north. The body-fixed velocity vector is denoted $\boldsymbol{\nu}$ and defined as:

$$\boldsymbol{\nu} = [u, v, r]^T, \quad (2)$$

where u is the *surge* velocity along the longitudinal x -axis, v is the *sway* velocity along the lateral y -axis and r is the rotation velocity around the local downward pointing axis $x \times y$. The transformation matrix \mathbf{J}_ψ defines the kinematic relationship between body-fixed and global frame velocities as follows:

$$\dot{\boldsymbol{\eta}} = \overbrace{\begin{bmatrix} \cos(\psi) & -\sin(\psi) & 0 \\ \sin(\psi) & \cos(\psi) & 0 \\ 0 & 0 & 1 \end{bmatrix}}^{\mathbf{J}_\psi} \boldsymbol{\nu}. \quad (3)$$

Fig. 1 shows the global coordinate frame with the origin denoted \mathcal{O}_n along with the two coordinate frames attached to two vehicles.

A. Kinetics

Underwater vehicles are affected by hydrodynamic effects. As a consequence a vehicle experiences the effect of hydrodynamic damping and added mass.

$$\mathbf{M}\dot{\boldsymbol{\nu}} + \mathbf{D}(\boldsymbol{\nu})\boldsymbol{\nu} = \mathbf{u}, \quad (4)$$

where \mathbf{M} and \mathbf{D} are the inertia and damping matrix, respectively, and defined as,

$$\mathbf{M} \triangleq \text{diag}(m_{11}, m_{22}, m_{33}), \quad \mathbf{D} \triangleq \text{diag}(d_{11}, d_{22}, d_{33}), \quad (5)$$

and \mathbf{u} being the force input in each DOF. The model Eq. (3) and (4) is represented on standard *Ordinary-Differential-Equation* (ODE) form by aggregating the pose and body-velocity vector as follows:

$$\dot{\mathbf{x}} = [\dot{\boldsymbol{\eta}}^T, \dot{\boldsymbol{\nu}}^T]^T. \quad (6)$$

The combined state evolution can then be written as follows:

$$\dot{\mathbf{x}} = \mathbf{f}(\mathbf{x}, \mathbf{u}). \quad (7)$$

When considering multiple vehicles in Section III, the vehicles associated with the i -th vehicle is assigned an index i .

III. MULTI-VEHICLE MODEL PREDICTIVE CONTROL FOR DOCKING

This section defines the consensus and visual constraint, as well as, the centralized MPC controller. Two objectives, consensus and visual constraints, are defined and combined into a centralized controller.

A. Notation

Consider a multi-vehicle system comprised of n agents. The agents interact through a network defined by a graph-topology \mathcal{G} . Agent i in the network correspond to a vertex v_i in the graph, the connection between individual agents are defined by the edge $e_{ij} = v_i v_j$. Together the set of vertices \mathcal{V} and the set of edges \mathcal{E} constitute a graph \mathcal{G} .

$$\mathcal{G} = \{\mathcal{V}, \mathcal{E}\}. \quad (8)$$

Each agent in the graph has a set of neighbors \mathcal{N}_i consisting of all vertices in the graph connected to the agent

$$\mathcal{N}_i(\mathcal{G}) = \{v_j \in \mathcal{V} \mid v_i v_j \in \mathcal{E} \vee v_j v_i \in \mathcal{E}\}. \quad (9)$$

The graph \mathcal{G} in this paper is un-directed. However, the notational convenience, an arbitrary direction is assigned. Thereby there exist a set of predecessors and successors for each vertex,

$$\mathcal{N}_i^+(\mathcal{G}) = \{v_j \in \mathcal{V} \mid v_i v_j \in \mathcal{E}\}, \quad (10)$$

$$\mathcal{N}_i^-(\mathcal{G}) = \{v_j \in \mathcal{V} \mid v_j v_i \in \mathcal{E}\}, \quad (11)$$

such that $\mathcal{N}_i = \mathcal{N}_i^+ \cup \mathcal{N}_i^-$.

B. Line-of-Sight Constraints

To utilize visual navigation between vehicles, it is necessary to restrict the motion between them such that they never loose esight of each other. Inspired by work in [23], [24], and [25], the *line-of-sight* (LOS) constraints can be formulated as follows:

$$\begin{aligned} \mathbf{n}_{i,j}^+ \mathbf{e}_{j,i} &\leq 0, \text{ for } \forall v_i \in \mathcal{V} \wedge v_j \in \mathcal{N}_i, \\ \mathbf{n}_{i,j}^- \mathbf{e}_{j,i} &\leq 0, \text{ for } \forall v_i \in \mathcal{V} \wedge v_j \in \mathcal{N}_i, \end{aligned} \quad (12)$$

where the normal vectors $\mathbf{n}_{i,j}^+$, and $\mathbf{n}_{i,j}^-$ are parameterized in the i th vehicles respective camera rotation. Notice, that the \mathbf{n} vectors are parameterized in the states, and thus are time-varying. The $\mathbf{e}_{j,i}$ is the relative position between the vehicle in the global frame and is assumed measured by the local camera.

$$\mathbf{e}_{j,i} = [N_j - N_i, E_j - E_i]^T.$$

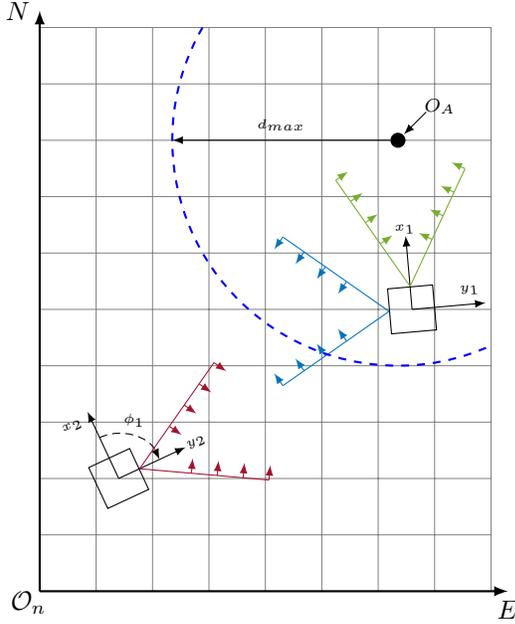


Fig. 1: Figure shows a multi-vehicle system consisting of two vehicles v_1 and v_2 as well as an object O_A . Vehicle v_1 is equipped with two cameras shown in blue and green, while vehicle v_2 is equipped with one camera marked with brown. The arrows on the cone-limits mark the direction of the normal vector of the constraint. ϕ_1 on v_2 shows the relative rotation between the onboard camera and the vehicle.

The parameterizations of the normal vectors $\mathbf{n}_{i,j}^+$ and $\mathbf{n}_{i,j}^-$ are:

$$\begin{aligned} \mathbf{n}_{i,j}^+ &: \begin{bmatrix} -\sin(\xi_{i,k} + \alpha_k) & \cos(\xi_{i,k} + \alpha_k) \end{bmatrix}, \\ \mathbf{n}_{i,j}^- &: \begin{bmatrix} \sin(\xi_{i,k} - \alpha_k) & -\cos(\xi_{i,k} - \alpha_k) \end{bmatrix}, \end{aligned} \quad (13)$$

where α_k is the camera half-angle of the visual cone for camera k , $\xi_{i,k}$ is the direction of the cone relative to the global frame $\xi_{i,k} = \psi_i + \phi_k$ with ϕ_k being the relative rotation between the vehicle i 's local x -axis and the visual cone of camera k . Fig. 1 shows the camera cone of two vehicles with respect to each other and a target.

C. Consensus Problem

The control objective is to solve the rendezvous problem, meaning the vehicles should converge to and remain at a common point.

$$\lim_{t \rightarrow \infty} \|\boldsymbol{\eta}_i - \boldsymbol{\eta}_j\| = 0 \quad \forall v_i \in \mathcal{V} \wedge v_j \in \mathcal{N}_i, \quad (14)$$

$$\lim_{t \rightarrow \infty} \|\boldsymbol{\nu}_i\| = 0 \quad \forall v_i \in \mathcal{V}. \quad (15)$$

The rendezvous objective of Eq. (14) is not feasible in practice since the vehicles cannot occupy the same space, however, in combination with the visual constraint the system will converge from a direction defined by the camera cones. Thus the vehicles will collide, but this is the desire as docking requires physical contact. Introducing the vectors

\mathbf{x} , $\boldsymbol{\eta}$, $\boldsymbol{\nu}$ and \mathbf{u} as follows:

$$\begin{aligned} \boldsymbol{\eta} &= [\boldsymbol{\eta}_1^T, \dots, \boldsymbol{\eta}_n^T]^T, \quad \mathbf{u} = [\mathbf{u}_1^T, \dots, \mathbf{u}_n^T]^T, \\ \boldsymbol{\nu} &= [\boldsymbol{\nu}_1^T, \dots, \boldsymbol{\nu}_n^T]^T, \quad \mathbf{x} = [\mathbf{x}_1^T, \dots, \mathbf{x}_n^T]^T, \end{aligned}$$

where the subscript $\boldsymbol{\eta}_i$ denotes the pose of vehicle v_i . The objective function J of the centralized problem is formulated as follows,

$$J(\mathbf{X}, \mathbf{U}) = \sum_{k=0}^{N-1} l(\mathbf{x}_{t+k|t}, \mathbf{u}_{t+k}), \quad (16)$$

where \mathbf{U} is all control inputs for all vehicles across the time horizon $\mathbf{U} = [\mathbf{u}_t, \mathbf{u}_{t+1}, \dots, \mathbf{u}_{t+N}]$, N is the control horizon, \mathbf{X} is all the state-vectors over the horizon, and the function $l(\mathbf{x}, \mathbf{u})$ is defined as:

$$l(\mathbf{x}, \mathbf{u}) = \boldsymbol{\eta}^T (\mathbf{L} \otimes \mathbf{P}) \boldsymbol{\eta} + \boldsymbol{\nu}^T \mathbf{W} \boldsymbol{\nu} + \mathbf{u}^T \mathbf{R} \mathbf{u}, \quad (17)$$

where matrix \mathbf{L} is the Laplacian matrix of the graph, \otimes is the Kronecker product, \mathbf{P} , \mathbf{W} and \mathbf{R} are tuning matrices.

D. Centralized Problem

The centralized control problem is composed of the consensus problem and the LOS constraints. The overall controller is formulated as follows:

$$\underset{\mathbf{U}}{\text{minimize}} J(\mathbf{X}, \mathbf{U}) \quad (18)$$

s.t.

$$\mathbf{u}_{i,t+k} \in \mathcal{U}_i, \quad \forall v_i \in \mathcal{V},$$

$$\mathbf{x}_{i,t+k+1|t} = \mathbf{f}_i(\mathbf{x}_{i,t+k|t}, \mathbf{u}_{i,t+k}), \quad \forall v_i \in \mathcal{V},$$

$$\mathbf{n}_{i,j}^\pm \mathbf{e}_{j,i} \leq 0, \quad \forall v_i \in \mathcal{V} \wedge v_j \in \mathcal{N}_i, \quad (19)$$

$$\mathbf{x}_{i,t+k|t} = [\mathbf{x}_{1,t+k|t}, \mathbf{x}_{2,t+k|t}, \dots, \mathbf{x}_{n,t+k|t}],$$

$$\mathbf{u}_{t+k} = [\mathbf{u}_{1,t+k}, \mathbf{u}_{2,t+k}, \dots, \mathbf{u}_{n,t+k}],$$

where \mathcal{U}_i is the input constraints for vehicle v_i

IV. COOPERATIVE MODEL PREDICTIVE CONTROL

The controller must be converted into a distributed formulation to effectively employ it in a multi-vehicle system. This section describes the usage of dual decomposition to distribute the problem among the agents.

A. Rendezvous Problem

The rendezvous problem from Sec. III-C is solved purely through the objective function in Eq. (18). However, the function itself relies on the difference in the pose of the vehicles due to \mathbf{L} . Hence the objective function is not separable. Introducing a new consensus parameter vector $\boldsymbol{\theta} \in \mathbb{R}^3$, which acts as a universal rendezvous point for the system, allows for the reformulation of the objective function. The global rendezvous point $\boldsymbol{\theta}$ is then distributed by introducing a local version $\boldsymbol{\theta}_i$ on each vehicle and adding the equality constraints as follows,

$$\boldsymbol{\theta}_i = \boldsymbol{\theta}_j \quad \forall v_i \in \mathcal{V} \wedge v_j \in \mathcal{N}_i. \quad (20)$$

The stage cost function of Eq. 17 is reformulated into the following expression:

$$l_i(\mathbf{x}_i, \mathbf{u}_i, \boldsymbol{\theta}_i) = (\boldsymbol{\eta}_i - \boldsymbol{\theta}_i)^T \mathbf{P}(\boldsymbol{\eta}_i - \boldsymbol{\theta}_i) + \boldsymbol{\nu}_i^T \mathbf{W} \boldsymbol{\nu}_i + \mathbf{u}_i^T \mathbf{R} \mathbf{u}_i. \quad (21)$$

The Hessian of l_i is only positive-semidefinite, and thus the problem is under-specified. There is no guarantee that the consensus point reaches a steady point unless additional pose constraints are applied, such as a stationary target or target area. The equality constraint of Eq. (20) is subsequently softened using Lagrangian relaxation and added to the objective function in the following section.

B. LOS-Constraint

The LOS constraints of Eq. (12) depends on the position error $e_{j,i}$ and the normal vectors are parameterized in the attitude of the local vehicle.

$$\begin{aligned} \mathbf{n}_{i,j}^+ \mathbf{p}_j - \mathbf{n}_{i,j}^+ \mathbf{p}_i &\leq 0, \\ \mathbf{n}_{i,j}^- \mathbf{p}_j - \mathbf{n}_{i,j}^- \mathbf{p}_i &\leq 0. \end{aligned} \quad (22)$$

Together, the constraints can be reformulated on matrix form as follows,

$$\mathbf{A}_{i,j} \mathbf{x}_j - \mathbf{A}_{i,j} \mathbf{x}_i \leq 0. \quad (23)$$

Finally, since the constraint is now linear in the state, a local optimization problem can be formulated,

$$\begin{aligned} J_i(\mathbf{X}_i, \mathbf{U}_i, \boldsymbol{\Theta}_i) &= \sum_{k=0}^{N-1} \left[l(\mathbf{x}_{i,t+k|t}, \mathbf{u}_{i,t+k}) \right. \\ &+ \sum_{j \in \mathcal{N}_i} [\boldsymbol{\lambda}_{j,t+k}^T \mathbf{A}_{j,i} - \boldsymbol{\lambda}_{i,j,t+k}^T \mathbf{A}_{i,j}] \mathbf{x}_{i,t+k|t} \\ &\left. + \sum_{j \in \mathcal{N}_i^+} \boldsymbol{\mu}_{i,j,t+k}^T \boldsymbol{\theta}_{i,t+k} - \sum_{j \in \mathcal{N}_i^-} \boldsymbol{\mu}_{i,j,t+k}^T \boldsymbol{\theta}_{i,t+k} \right], \end{aligned} \quad (24)$$

where $\boldsymbol{\lambda}_{j,i}$, and $\boldsymbol{\mu}_{i,j}$ are the Lagrangian multipliers associated with the LOS constraint from vehicle j to vehicle i and the consensus equality constraint associated with the edge $e_{i,j}$ respectively. \mathbf{X}_i is the states of vehicle i over the time horizon, $\mathbf{X}_i = [\mathbf{x}_{i,t|t}, \mathbf{x}_{i,t+1|t}, \dots, \mathbf{x}_{i,t+N-1|t}]$, \mathbf{U}_i is the inputs over the time horizon $\mathbf{U}_i = [\mathbf{u}_{i,t}, \mathbf{u}_{i,t+1}, \dots, \mathbf{u}_{i,t+N-1}]$ and $\boldsymbol{\Theta}_i$ is the locally computed consensus point across the time horizon, $\boldsymbol{\Theta}_i = [\boldsymbol{\theta}_{i,t}, \boldsymbol{\theta}_{i,t+1}, \dots, \boldsymbol{\theta}_{i,t+N-1}]$. The control problem can now be reformulated as a local optimization problem as follows:

$$\text{minimize } J_i(\mathbf{X}_i, \mathbf{U}_i, \boldsymbol{\Theta}_i) \quad (25)$$

s.t.

$$\begin{aligned} \mathbf{u}_{i,t+k} &\in \mathcal{U}_i, \\ \mathbf{x}_{i,t+k+1|t} &= \mathbf{f}_i(\mathbf{x}_{i,t+k|t}, \mathbf{u}_{i,t+k}), \end{aligned} \quad (26)$$

The dual variables $\boldsymbol{\lambda}$ for the visual inequalities are updated using the projected sub-gradient method [3] as follows:

$$\boldsymbol{\lambda}_{i,j,t+k}^{r+1} = \boldsymbol{\lambda}_{i,j,t+k}^r + \kappa_{i,j}^r (\mathbf{A}_{i,j,t+k} [\mathbf{x}_{j,t+k|t}^{*r} - \mathbf{x}_{i,t+k|t}^{*r}])_+, \quad (27)$$

where $(\cdot)^*$ are the resulting optimal values from the solution to Eq. (25-26), $(\cdot)^r$ denotes the r th iteration, $(\cdot)_+$ is the projected gradient, and $\mathbf{A}_{i,j,t+k}$ is the visual constraint matrix updated over the time horizon.

The dual variables $\boldsymbol{\mu}$ for the consensus equality constraints are likewise updated using the sub-gradient method [3].

$$\boldsymbol{\mu}_{i,j,t+k}^{r+1} = \boldsymbol{\mu}_{i,j,t+k}^r + \gamma_{ij}^r (\boldsymbol{\theta}_{i,t+k}^{*r} - \boldsymbol{\theta}_{j,t+k}^{*r}). \quad (28)$$

The overall control algorithm is shown in Algorithm 1.

Algorithm 1 Distributed Controller

Input: $\boldsymbol{\lambda}^0, \boldsymbol{\mu}^0$

- 1: **for** $r = 0, \dots, L - 1$ **do**
 - 2: Solve local optimization problem Eq. (25) to obtain $\mathbf{X}_i^{*r}, \mathbf{U}_i^{*r}$ and $\boldsymbol{\Theta}_i^{*r}$
 - 3: Communicate the local state trajectories \mathbf{X}_i^{*r} and consensus point sequence $\boldsymbol{\Theta}_i^{*r}$, to neighbors in \mathcal{N}_i .
 - 4: Compute the new price sequences $\boldsymbol{\lambda}^{r+1}$ and $\boldsymbol{\mu}^{r+1}$ locally by applying Eq. (27) and (28)
 - 5: **end for**
 - 6: Set $\boldsymbol{\lambda}^0 = \boldsymbol{\lambda}^L$ and $\boldsymbol{\mu}^0 = \boldsymbol{\mu}^L$
 - 7: Apply first element of the control sequence \mathbf{U}_i^{*L-1} to the local plant.
-

V. SIMULATIONS

In this section a simulation is conducted to show the application of the controller. The simulation is implemented in Python using CasADI [1]. The model of Eq. (7) is discretized using Runge-Kutta4. The applied optimization solver is the interior-point implementation IPOPT [34].

Parameter	Value	Unit
$\kappa_{i,j}$	30	[-]
γ_{ij}	2	[-]
\mathbf{D}_i	$\text{diag}(30, 30, 1)$	[-]
\mathbf{M}_i	$\text{diag}(10, 10, 1)$	[-]
$\ \mathbf{u}\ _\infty$	$[5, 5, 1.5]$	[-]
L	15	[-]
$\mathbf{x}_{1,0}$	$[4, 3, -0.2, 0, 0, 0]$	[-]
$\mathbf{x}_{2,0}$	$[1, -2, -0.58, 0, 0, 0]$	[-]
O_A	$[6.1, 3]$	[m]
d_{max}	3	[m]
\mathbf{P}_i	$\text{diag}(15, 15, 15)$	[-]
\mathbf{W}_i	$\text{diag}(10, 10, 10)$	[-]
\mathbf{R}_i	$\text{diag}(10, 10, 10)$	[-]
N	30	[-]
α_k	25	[deg°]
δt	0.05	[s]

TABLE I: Parameters and initial conditions used in the simulation scenario.

A. Monitoring and Rendezvous

The simulation scenario consists of two vehicles v_1 , and v_2 and a stationary target O_A . Vehicle v_1 is inspecting target O_A , while at the same time rendezvous and docking with vehicle v_2 . The inspecting vehicle is required to stay within

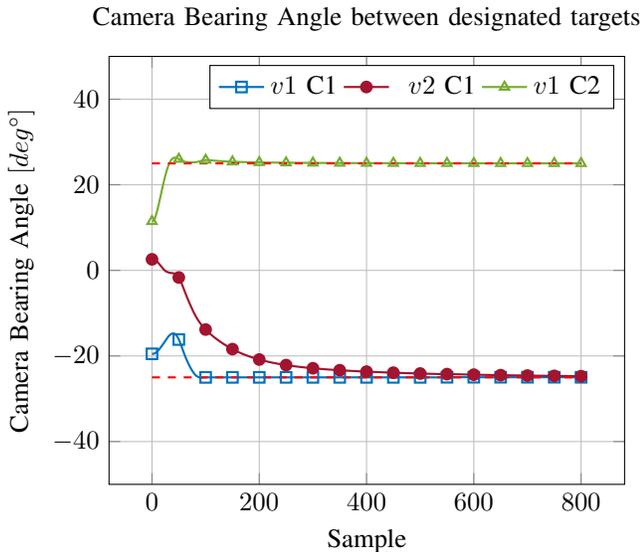


Fig. 2: The figure shows bearing angles in each of the cameras. The bearings of the cameras overshoots the limits slightly and thereby violates the constraint, however, in practice this could be avoided by defining a safety limit a couple of degrees inside the actual field-of-view

a certain distance of the target and maintain visual contact. Fig. 1 shows the scenario, where d_{max} is the maximum distance allowed between v_1 and O_A . The distance constraint is implemented as a quadratic constraint as follows:

$$(\mathbf{p}_{O_A} - \mathbf{p}_1)^T (\mathbf{p}_{O_A} - \mathbf{p}_1) \leq d_{max}^2. \quad (29)$$

The location of the object \mathbf{p}_{O_A} is stationary, and known. Thereby, the constraint (29) is simply an inequality constraint on vehicle one. Moreover, the visual constraint (13) is only from the vehicle to the object and requires no dual decomposition and communication between them.

Table I contains the dynamics parameters, initial conditions, and tuning parameters. Fig. 2 shows the bearing angles measured in the cameras. The bearings move towards the visual constraint limits and overshoots slightly. The overshoot is natural since the visual constraints are implemented using Lagrangian relaxation, and the number of iterations for updating the dual variables are limited. The overshoot is easily dealt with if one defines the limits lower than the actual camera field of view. Fig. 3 shows the trajectories of the vehicles. Vehicle v_1 shown in blue starts inside the designated target area looking at object O_A , while vehicle v_2 starts outside the area with v_1 inside the field-of-view. Note that the constraint of (29) imposes an implicit restriction on the pose of vehicle one. Hence the consensus point of (21) is attracted to the position of vehicle one. The constraint violation is a trade-off between both the tuning of the consensus and the number of iterations for the update of the dual variables and as such more iterations would allow a better estimate of the actual dual variables. The subgradient method is converging

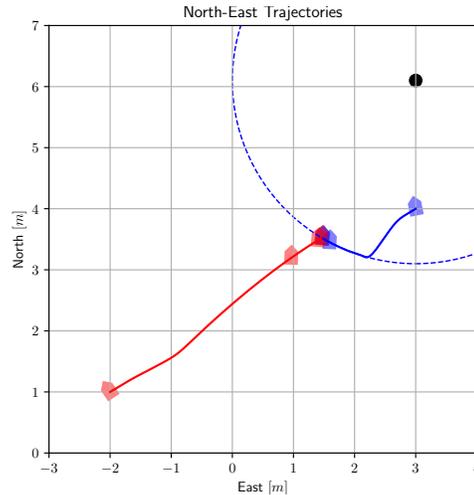


Fig. 3: The trajectories show that each vehicle move towards each other while trying to maintain visual contact. Vehicle v_1 stays within the prescribed distance of the target while keeping both v_1 and O_A inside the respective camera field-of-view.

at a sub-linear rate and thus to obtain accurate dual variables a large number of iterations are required [13], [15]. The communication requirement quickly increases as a result of the sharing of state trajectories and optimal consensus point sequences. One possible solution would be to allow second-order information to the update of the dual variables at the expense of slightly more data communication for each iteration. The second-order information would allow up to quadratic convergence of the dual variables and as such reduce the necessary iterations significantly [13], [15]. The bandwidth of underwater optical communication would allow for the increased communication requirement within a few tens of meters [36], [35]. The communication requirement for the specific simulation was approximately 1.7 Mbit/s. The bandwidth of acoustic communication range up to 0.5 Mbit/s at 60m [30], but the bandwidth can by manipulation of the sampling time δt , the max iteration L and the length of the control horizon N be significantly lowered.

VI. CONCLUSION

In this paper, we presented a distributed model predictive controller for the solution to a cooperative rendezvous and docking problem under visual camera constraints. The problem consisted of two subparts, namely a consensus problem and a visual field-of-view restriction. A DMPC was derived using dual decomposition. A simulation study was conducted to show the application of the controller, where two vehicles conduct are rendezvous and docking maneuver while one of the vehicles stay within a maximum prescribed distance of a designated target and maintain visual contact.

The present communication technology does allow the proposed method to work, but for robustness reduction in communication is a topic of future research.

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