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Theisen, Lukas Roy Svane; Galeazzi, Roberto; Blanke, Mogens

Published in:
Proceedings of the 9th IFAC Conference on Control Applications in Marine Systems

Link to article, DOI:
10.3182/20130918-4-JP-3022.00048

Publication date:
2013

Citation (APA):

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Unmanned Water Craft Identification and Adaptive Control in Low-Speed and Reversing Regions

Lukas R. S. Theisen * Roberto Galeazzi * Mogens Blanke *,**

* Department of Electrical Engineering, Automation and Control Group, Technical University of Denmark, Kgs. Lyngby, Denmark
(e-mail: {lrst, rg, mb}@elektro.dtu.dk)
** Centre for Autonomous Marine Operations and Systems (AMOS), Norwegian University of Science and Technology, Trondheim, Norway

Abstract: This paper treats $L_1$ adaptive hovering control of an unmanned surface vehicle in a station-keeping mode where a region of zero control authority and under-actuation are main challenges. Low-speed and reversing dynamics are identified from full scale sea trials, and parameter uncertainty is estimated. With significant parameter variation, an $L_1$ adaptive controller is employed for heading control. The $L_1$ family of controllers allows for several topologies and an architecture is suggested that suits heading control of a vessel, the requirements of which differ from that of previous $L_1$ literature. The control design is tackled directly in discrete time to allow a fast embedded implementation in the vehicle. Analysis of robustness, tracking performance and wave disturbance response are detailed in the paper.

Keywords: $L_1$ adaptive control, surface vehicle control, unmanned systems, system identification

1. INTRODUCTION

Personal water crafts (PWC) are capable of fast and agile manoeuvring and provide endurance over long distances making them suitable for complex autonomous missions. Certain missions may require station keeping as one of the use-modes, which is achieved through heading and speed control at low speed forward and aft.

The realisation of station keeping for the PWC is certainly a challenge since the system is under-actuated. The vehicle has an azimuth impeller equipped with an elevator, which can be used to change the vertical direction of the impeller jet. This actuation is perfect at high forward speed to execute fast manoeuvres; however at low speed the controllability of the system reduces.

Control of under-actuated vehicles has received a great attention (see e.g. Pettersen and Fossen (2000); Fossen and Strand (2001); Blanke (2005); Pereira et al. (2008)), but it still is an open and interesting control problem. Fossen and Strand (2001) proposed the weather optimal heading control, where the marine craft is steered to be on a virtual circle headed towards the centre. A set of model parameters were at hand for the considered vessel and a PD regulator was designed using the backstepping design methodology with the inclusion of integral action.

For the PWC there is no model readily available, and the identification of the system dynamics solely relies on full scale motion data always affected by induced oscillations in the wave frequency range. This results in significant parameter variation, which calls in for robust and adaptive control strategies.

The development of the $L_1$ adaptive control theory (Hovakimyan and Cao, 2010) has allowed for design of controllers ensuring uniform closed loop transient response over a wide range of parametric uncertainties, while guaranteeing robustness and stability. Svendsen et al. (2012) took the first steps towards a fully autonomous PWC by designing and implementing two independent $L_1$ adaptive controllers for cruise and steering control at medium to high speed.

This paper proposes a low speed adaptive heading controller suitable for station keeping. The architecture of the $L_1$ adaptive controller is modified in order to best fit the heading control problem, and the controller is completely and directly designed in discrete time to allow fast embedded implementation in the vehicle. Robustness and performance of the proposed heading controller is analysed w.r.t. model uncertainties and disturbances.

2. SYSTEM CONFIGURATION

The water jet vehicle is a modified Sea-Doo GTX 215 personal water craft (see Fig. 1), whose physical specifications are listed in table A.1. A radio link between the vehicle and a ground station allows remote command of three servos, which control the throttle, the azimuthal angle of the water jet, and the elevator angle of a blade constraining the angle of attack of the pressurised water stream w.r.t. the horizontal.

The elevator angle or deflection $\beta$ of the blade w.r.t. the horizontal is in the interval $\beta \in [0^\circ; 55^\circ]$ and a deflection $\beta$ corresponds to a deflection of the water jet of $2\beta$, as illustrated in Fig. 1. Similarly the azimuth $\delta$ controls the
3. PWC REVERSING DYNAMICS

For low speed operations such as station keeping where the speed is below 3 m/s the personal water craft behaves as a fully displaced vessel; hence the influence of the vertical dynamics into the manoeuvring characteristic is negligible. For larger ships it is assumed that the heave, roll and pitch are fairly small (Petersen and Fossen, 2000). This assumption is extended to the dynamics of the water jet vehicle; however this may be true only in confined waters.

The 3 DOF surge-sway-yaw linear manoeuvring model is formulated according to (Clarke and Horn, 1997; Fossen, 2011). Let \( \eta \triangleq [N, E, \psi]^T \) be the generalised position vector w.r.t. an Earth-fixed frame, and \( \nu \triangleq [u, v, r]^T \) the generalised velocity vectors w.r.t. a body-fixed frame. The PWC dynamics in the horizontal plane is then given by

\[
\dot{\eta} = R(\psi)\nu
\]

(1)

\[
M\dot{\nu} + N(u_0)\nu = \tau_e + \tau_c
\]

(2)

where \( M \) is the mass-inertia matrix including rigid-body and added mass; \( N(u_0) \) contains the linear contribution from the frictional and Coriolis-centripetal forces and moments evaluated at the forward speed \( u_0 \); \( \tau_e \) and \( \tau_c \) are the vectors of generalised control and environmental forces; \( R(\psi) \) is the rotation matrix that maps velocities from body- to the Earth-fixed frame.

Assuming that surge can be decoupled from steering, \( M \) and \( N \) in (2) read

\[
M = \begin{bmatrix}
m - X_u & 0 & 0 \\
0 & m - Y_u & mx_y - Y_r \\
0 & mx_y - N_r & I_z - N_r_f
\end{bmatrix}
\]

\[
N(u_0) = \begin{bmatrix}
-X_u & 0 & 0 \\
0 & Y_u & mu_0 - Y_r \\
0 & -mu_0 & mx_y u_0 - N_r
\end{bmatrix}
\]

where \( m \) is the mass of the vehicle, \( I_z \) is the rigid body inertia around the \( z \)-axis, \( x_y \) is the horizontal coordinate of the centre of gravity w.r.t. the origin of the body-fixed manoeuvring frame (\( z \)-down), and \( X(\cdot), Y(\cdot), N(\cdot) \) are the hydrodynamic derivatives.

Said \( T \) the thrust force, the control input vector \( \tau_c = [\tau_{cX}, \tau_{cY}, \tau_{cZ}]^T \) is given by

\[
\tau_c \triangleq b(\delta, \beta)T = \begin{bmatrix}
\cos \delta \cos(2\beta) \\
-\sin \delta \cos(2\beta) \\
L_0 \sin \delta \cos(2\beta)
\end{bmatrix}
\]

(3)

The available of only the motion data gathered during full scale sea trials obviously precludes the possibility of identifying the coefficients of the matrices \( M \) and \( N(u_0) \). Therefore the identification of the low-speed reversing dynamics relies on linear output models parameterised in terms of time constants and gains. Hence the action of environmental forces/moments \( \tau_e \) is modelled as output disturbances.

3.1 Low-Speed Surge Dynamics Identification

The decoupled surge dynamics reads

\[
\dot{u}(t) = \frac{-X_u - u(t) + f(h, t)}{m - X_u} \cos(2\beta(t)),
\]

(4)

where \( f(h, t) \) is the body component of the thrust. The throttle handle \( h \) has been constrained to the constant value \( h = 1 \), it is therefore assumed \( f(h, t) = f \) is constant. Equation (4) can be rewritten in transfer function form as

\[
u(s) = \frac{K_u}{T_u s + 1} g(s),
\]

(5)

where \( g(s) \) is the Laplace transform of \( \cos(2\beta(t)) \); \( K_u \triangleq \bar{f} \) is the steady state surge gain for a constant \( \beta \); \( T_u \triangleq (X_u/(m - X_u))^{-1} \) is the time constant. The parameters \( K_u \) and \( T_u \) are estimated from full scale data collected in response to elevator steps. The identified model is

\[
M_{u,g} : \quad \nu(s) = \frac{2.46}{5.58 s + g(s)}
\]

(6)

whose fit to the data set in identification is 92.3%, and in validation is 85.4%. Figure 2 shows the comparison between the full scale data and the surge model \( M_{u,g} \) for the identification and validation data sets.

3.2 Low-Speed Steering Dynamics Identification

The linear output yaw model associated to (2) is

\[
r(s) = H_{\text{nom}}(s)\delta(s) + r_u(s), \quad H_{\text{nom}} = \frac{K_n}{T_n s + 1}
\]

(7)

which is the first order Nomoto model (Nomoto et al., 1957) affected by external disturbances, where

\[
K_n = -N_d D_n, \quad T_n = (I_z - N_r) D_n
\]
with $D_n = (m x_g - Y_r) u_0 - N_e)^{-1}$. The wave disturbance $r_w(s)$ is modelled as the output of a second order filter driven by white noise $e_w(t)$

$$r_w(s) = \frac{\kappa_w s}{s^2 + 2\lambda_w \omega_w s + \omega_w^2} e_w(s).$$

(8)

The model (7) is used for identifying the low-speed manoeuvring dynamics of the PWC. The wave model (8) is introduced to take into account the presence of wave motion in the experimental data sets. The identification of the yaw dynamics is performed by using full scale motion data collected during 19 circular tests at different elevator angles $\beta$. The Box-Jenkins model structure (Box and Jenkins, 1970) is used to represent the dynamics (7), and the model’s parameters are estimated using the prediction error method (Ljung, 1999).

Figure 3 shows the estimated Nomoto model parameters with $\pm 1\sigma$ uncertainty. The estimates have generally a very low uncertainty, except for the two sea trials performed at $\beta \approx \pi/4$ where the vehicle is close to the controllability singularity. The estimate of the pole 1/$T_n$ is not very consistent, i.e. experiments repeated at the same elevator angle do not provide similar values, especially for $\beta \approx 0$. This may address the influence of the low frequency component of the wave motion on the estimation of the PWC dynamics. Instead the estimate of the gain $K_n / T_n$ is more robust, with the presence of only two outliers for $\beta = 0$. Figure 3 also shows the sign dependency of the input gain on the deflection of the elevator. This poses an important issue for the design of adaptive controllers, which requires the definition of a new control input, as shown in Sec. 4.1.

Standard methods of system identification have been used to assess the validity of the identified Nomoto models, such as parameter’s sign test and residual whiteness. The analysis of these two indicators clearly addressed the under-parametrisation of the chosen model structure with respect to the dynamics present on the full scale data. Low complexity models are sought here and the first order Nomoto model is used as it catches the essential manoeuvring characteristics of the vehicle.

4. TOWARDS STATION KEEPING

In the design towards a station keeping system, a heading controller is an important aspect. This section presents a step towards station keeping in projecting a discrete time $L_1$ adaptive heading controller for the PWC. Surge control can be performed using e.g. (Fossen and Strand, 2001; Pettersen and Fossen, 2000), and it is not be considered further in this paper.

4.1 Forced Yaw Acceleration

A new control input is defined as the forced yaw acceleration

$$\ddot{a}_w^* (\beta, \delta) \triangleq -\frac{N_\delta(\beta)}{I_z - N_e} \delta,$$

(9)

where $N_\delta(\beta) = T_{E} \cos(2\beta)$ is a function of the elevator angle. By including $N_\delta$ in the new control input the sign of the input gain is preserved. This guarantees that the input gain does not switch sign during system’s operation, which is needed in order to design the adaptive controller.

Figure 4 shows the dependency of the physical torque gain $N_\delta$ on the elevator deflection. $N_\delta$ has been estimated by

$$D_n = \frac{T_n}{I_z - N_e} \Rightarrow N_\delta = \frac{K_n}{D_n},$$

(10)

where $T_n$ has been computed by considering the PWC as a rigid rod with most of the mass placed at the centre, and the added inertia $N_e < 0$ has been assumed constant and equal to 80% of $I_z$ ($I_z - N_e \approx 460$ kg m$^2$).

The indirect estimate of $N_\delta$ is strongly affected by the inconsistency in the estimate of $T_n$ for values of $\beta$ close to zero. Hence the values of $N_\delta$ are scattered, determining an uncertainty in the magnitude of $\dot{a}_w^*$. This uncertainty is modelled as

$$a_w^*(\beta, \delta) \approx \omega \dot{a}_w^* (\beta, \delta), \quad \omega \in [\omega_{\min}, \omega_{\max}]$$

(11)

where $\omega$ is an uncertain input gain and $\omega_{\max} > \omega_{\min} > 0$. 
4.2 Discrete Time $L_1$ Adaptive Heading Controller

The control objective is to regulate the vehicle heading as desired, despite the presence of environmental disturbances and unknown nonlinear manoeuvring characteristics. However control effort should be limited in the wave frequencies range to reduce wear and tear of the actuator. This is fulfilled through a two step design: first a baseline PD regulator is dimensioned for the nominal heading dynamics; then the feedback loop is augmented with an $L_1$ adaptive controller, which guarantees scalable transient performance in presence of changes in system parameters. The heading controller is designed for operation at the elevator angles $\beta \in \{0^\circ; 55^\circ\}$ and for a forward speed $U < 3\text{ m/s}$.

The proposed architecture for the $L_1$ adaptive controller exploits the physical correlation between heading angle and turning rate, the yaw dynamics (12)-(13) is reduced to

$$\dot{r}(k + 1) = f_{22}\sigma(k) + g_2(\omega u_{\text{ref}}(k) + u_{\text{ad}}(k)),$$

where $\hat{\sigma}(k)$ is the estimate of the model uncertainty, and $\omega_0$ is the nominal value of the uncertain gain $\omega$.

### Adaptation law

The estimate of the unmodelled dynamics relies on the prediction error $\tilde{r}(k) = \dot{r}(k) - r(k)$ as

$$\hat{\sigma}(k) = -g_2^{-1}f_{22}\sigma(k) = -K_{\text{ad}}\hat{r}(k),$$

where $K_{\text{ad}}$ is the adaptation gain, which is clearly a function of the sampling time $T_s$ and the system parameters.

### Control law

The adaptive control signal $u_{\text{ad}}$ is a lowpass filtering of the adaptive estimate, which ensures tracking up to a chosen bandwidth

$$u_{\text{ad}}(z) = -kD(z)\hat{\eta}(z),$$

where $k$ is the feedback gain, $D(z)$ is a lowpass filter containing a pure integrator, and $\hat{\eta}(z)$ is the $\mathcal{Z}$-transform of

$$\hat{\eta}(k) = (\omega u(k) + \hat{\sigma}(k)),$$

By choosing the lowpass filter as

$$D(z) = \frac{k_1(z + z_1)}{(z - 1)(z - p_1)}$$

and assuming $\omega_0 = 1$ the control law then reduces to

$$u(z) = -C(z)\hat{\sigma}(z),$$

where $C(z)$ is the $\mathcal{Z}$-transform of

$$C(z) = \frac{kk_1(z + z_1)}{z^2 + (kk_1 - p_1 - 1)z + p_1 + kk_1z_1}.$$
4.3 Robustness Analysis of $\mathcal{L}_1$ Adaptive Controller

The bandwidth of the filter $C(z)$ sets a clear trade-off between the adaptation to unmodelled dynamics and the sensitivity of the control signal to wave disturbances. The robustness properties of the adaptive controller are investigated by a frequency analysis showing the system performance in response to changes in the nominal plant.

For the calculations the plant is given a multiplicative uncertainty $\omega$, and it is converted to discrete time along with the state predictor

$$H_{pl}(z) = Z\left\{\omega/(T_n s + 1)\right\}$$  
$$H_{sp}(z) = Z\left\{1/(T_n s + 1)\right\}$$

The discrete time $\mathcal{L}_1$ adaptive controller is shown in Fig. 5. The relevant transfer functions, namely from reference to heading and from disturbance to forced yaw acceleration, are calculated to be

$$H_{\psi\psi,ref}(z) = H_{pl}T_s k_p H_f (1 + H_{sp} K_\sigma)/d(z)$$  
$$H_{\delta\rref}(z) = -(C K_\sigma z - C K_\sigma + H_f k_D z - H_f k_D + H_f k_D H_{sp} K_\sigma - H_f k_D H_{sp} K_\sigma + T_i H_f k_p + T_i H_f k_P H_{sp} K_\sigma)/d(z)$$

where

$$d(z) = (z - 1 + H_{sp} K_\sigma - C H_{sp} K_\sigma z + C H_{sp} K_\sigma - H_{pl} K_\sigma + H_{pl} T_i k_p H_f + H_{pl} k_D H_I z - H_{pl} k_D H_f + H_{pl} K_\sigma C - H_{pl} K_\sigma C + H_{sp} K_\sigma H_{pl} T_i k_p H_f + H_{sp} K_\sigma H_{pl} k_D H_I z - H_{sp} K_\sigma H_{pl} k_D H_f)$$

$H_{\delta\rref}(z)$ and $H_{\psi\psi,ref}(z)$ are evaluated in response to a large plant variation ($\omega = 3$). By increasing the bandwidth of $C(z)$ a better adaptation to the reference model in presence of uncertainties is achieved; however this comes at the cost of a larger gain from disturbance to control signal, as shown in Fig. 6. The bandwidth of $C(z)$ is hence chosen such that $H_{\psi\psi,ref}(z)$ has a sufficiently small magnitude in the range of frequencies where the wave disturbances is active ($\approx 3 \div 6 \text{ rad/s}$). This gives an upper limitation for the bandwidth of $C(z)$ and thereby the adaptation properties. The chosen $C(z)$ has the parameters given in table B.1.

5. PERFORMANCE ASSESSMENT

The desired closed loop step response should have an overshoot less than 5%, and a rise time of approximately 4.2 seconds. Suitable parameters for the baseline controller achieving these requirements are listed in table B.1.

The performance of heading controller is first assessed by step changes. Figure 7 shows the scalability of the transient response of the $\mathcal{L}_1$ adaptive heading controller. Figure 8 shows the performance of the PWC during an elevator step simulation. The elevator steps and causes the surge of an unmanned personal water craft, based on a discrete time $\mathcal{L}_1$ adaptive heading controller. First, a steering model for the PWC in low-speed and reversing regions was identified based on full scale motion data. The identified model showed large parameter variations in response to wave disturbances, as shown in Fig. 9. As expected the controller limits the use of control authority to counteract the wave motion, while regulating the heading around the desired value.

6. CONCLUSIONS

This paper presented a solution towards station keeping of an unmanned personal water craft, based on a discrete time $\mathcal{L}_1$ adaptive heading controller. First, a steering model for the PWC in low-speed and reversing regions was identified based on full scale motion data. The identified model showed large parameter variations in response to wave disturbances, as shown in Fig. 9. As expected the controller limits the use of control authority to counteract the wave motion, while regulating the heading around the desired value.
similar operational conditions. A robust adaptive heading controller was then designed, which combines a baseline PD regulator with a discrete time \( L_1 \) adaptive controller. The proposed control architecture exploits the physical correlation between heading angle and turning rate to reduce complexity of the state predictor and the adaptation law. A robustness analysis was carried out, which showed the trade-off between adaptation and disturbance rejection properties. Simulation results confirmed the validity of the proposed heading controller for station keeping purposes.

**ACKNOWLEDGEMENTS**

The collaboration with the Naval Drone Section of the Danish Navy is gratefully acknowledged. Enthusiastic support from Leif Kurt Hevang and from Jens Adrian, leader of the research group, is also gratefully appreciated.

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**Appendix A. PERSONAL WATER CRAFT PARAMETERS**

The parameters of the system are listed in table A.1.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nominal length (measured)</td>
<td>3.25 m</td>
<td></td>
</tr>
<tr>
<td>Width</td>
<td>1.22 m</td>
<td></td>
</tr>
<tr>
<td>Dry weight</td>
<td>388 kg</td>
<td></td>
</tr>
<tr>
<td>Engine max power</td>
<td>158 kW</td>
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</table>

**Appendix B. CONTROL SYSTEM PARAMETERS**

The parameters of the system are listed in table B.1.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Unit</th>
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</thead>
<tbody>
<tr>
<td>( \omega_1 )</td>
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<td>rad/s</td>
</tr>
<tr>
<td>( \alpha_f )</td>
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<td>rad/s</td>
</tr>
<tr>
<td>( \omega_\theta )</td>
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<td>rad/s</td>
</tr>
<tr>
<td>( k )</td>
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<td>rad/s</td>
</tr>
<tr>
<td>( k_1 )</td>
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<td>rad/s</td>
</tr>
<tr>
<td>( k_p )</td>
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<td>rad/s</td>
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<td>( k_D )</td>
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<tr>
<td>( k_H )</td>
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<td>s</td>
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</table>