Phasor model of full scale converter wind turbine for small-signal stability analysis

Ghiga, Radu; Wu, Qiuwei; Nielsen, Arne Hejde

Published in:
The Journal of Engineering

Link to article, DOI:
10.1049/joe.2017.0476

Publication date:
2017

Document Version
Publisher's PDF, also known as Version of record

Link back to DTU Orbit

Citation (APA):

General rights
Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.
Phasor model of full scale converter wind turbine for small-signal stability analysis

Radu Ghiha, Qiuwei Wu, Arne Hejde Nielsen

Centre for Electric Power and Energy, Department of Electrical Engineering, Technical University of Denmark, Denmark
E-mail: qw@elektro.dtu.dk

Published in The Journal of Engineering; Received on 9th October 2017; Accepted on 1st November 2017

Abstract: The small-signal stability analysis of power system electromechanical oscillations is a well-established field in control and stability assessment of power systems. The impact of large wind farms on small-signal stability of power systems has been a topic of high interest in recent years. This study presents a phasor model of full scale converter wind turbines (WTs) implemented in MATLAB/SIMULINK for small-signal stability studies. The phasor model is typically used for dynamic studies of power systems consisting of large electric machines. It can also be applied to any linear system. This represents an advantage in small-signal stability studies, which are based on modal analysis of the linearised model and are usually complemented with dynamic simulations. The proposed model can represent a single WT or an aggregated wind power plant. The implemented model for small-signal stability analysis was tested in the Kundur’s two area system. The results show that the proposed WT model is accurately linearised and its impact on power system oscillation is similar to that of previous research findings.

1 Introduction

The installed capacity of wind power and the size of each installation have been increasing rapidly, with the European offshore sector installation just over 3 GW of wind power only in 2015 [1]. The role and impact of large penetration of wind power can be significant in the operation and security of the power system [2, 3]. A topic of interest is the effect of large wind power plants (WPPs) on small-signal stability of power systems. The validity of the damping results depends on accurate representation of the WPP control systems [4–6].

In a full scale converter wind turbine (FSCWT), the generator dynamics are decoupled from the grid dynamics. Hence, the wind turbine (WT) generator cannot contribute to damping the system oscillations without additional control [7]. However, this type of configuration has the advantage of controlling both active and reactive power independently, and also allows independent impact assessment of these controls on power system oscillations.

The phasor simulation method in MATLAB/SIMULINK is typically used to study low frequency electromechanical oscillations of power systems consisting of a large number of generators and loads. An advantage of this method is that sinusoidal voltages and currents are replaced with phasors expressed in the complex or polar form. Since the electromagnetic transients are not of interest, the dynamic simulation time is reduced [8]. Another advantage is that the phasor simulation can be used with any linear system, and small-signal stability studies are based on eigenvalue analysis of the linearised power system. Finally, the eigenvalue analysis is usually complemented with dynamic simulations of the non-linear system which can be several tens of seconds long. Hence, short simulation times are desired.

The aim of this paper is to present a FSCWT model that can be used in dynamic simulations, and can be linearised by the tools available in SIMULINK, without the need to build a separate state-space representation of the model. Therefore, a phasor FSCWT model with a permanent magnet synchronous generator (PMSG) is implemented in MATLAB/SIMULINK. The model consists of detailed controls in order to catch the potential impact, which might have on power system oscillations. The eigenvalues of the system are first analysed with no wind power injected in the network, and then with increasing wind power penetration. To verify the accuracy of the linearised system, the linear and non-linear responses of the system are compared.

This paper is organised as follows. In Section 2, the WT concept is presented. Section 3 describes the controls implemented for this model. Section 4 shows the results and conclusions are drawn in Section 5.

2 WT concept

The concept of the FSCWT is shown in Fig. 1. The main parts are the WT rotor, PMSG, FSC, filter, and transformer. The FSC consists of a generator side and grid side that are connected by a DC-link circuit with a capacitor (Cdc). The generator three-phase AC voltage is converted into DC voltage (Vdc) by the generator side converter. The DC voltage is then inverted back into AC by the grid side converter which uses a phase-locked loop (PLL) to match the grid frequency and phase.

The control system of the FSCWT consists of three main controllers. The pitch controller regulates the angle of the blades (β) to prevent the rotor speed (ωr) from exceeding its rated value. The generator side control adjusts the generator currents in order to control its active (Pgen) and reactive power (Qgen) outputs. The grid side control maintains Vdc to its rated value, and controls the reactive power (Qgrid) output and the AC voltage at the terminal of the WT.

3 WT phasor model

The block diagram of the WT phasor model implemented in SIMULINK is shown in Fig. 2. The Vabc/Vdq block has a PLL implemented that computes the angle of the terminal voltage phasor and uses it to align the internal dq-reference. The WT is interfaced with the network through a controlled current source and connected to the grid at the point of connection (POC). The remaining blocks are described in the following subsections.

3.1 Aerodynamic model and pitch controller

The Aerodynamics block calculates the mechanical torque (Tm) as

\[ T_m = P_{out}/\omega_r \]

The mechanical power \( P_{out} \) converted from the wind power plant.
The speed is calculated inside this block as [9]

\[ P_m = 0.5 \rho \pi A v^3 C_p (\lambda, \beta) \]  

(1)

where \( \rho \) is the air density (kg/m\(^3\)), \( A \) is the rotor swept area (m\(^2\)), \( v \) is the wind speed (m/s), \( C_p \) is the power coefficient, and \( \lambda \) is the tip speed ratio (\( v_t/v \)), and \( v_t \) is the blade tip speed (m/s). The generic equation used to approximate \( C_p \) is given in [9].

Fig. 3 shows the pitch controller of the WT. The blade pitch angle (\( \beta \)) is calculated based on the error between the measured rotor speed and the reference value (\( \omega_{\text{ref}} = 1.0 \) p.u.). The angle is kept at zero degree as long as the rotor speed does not exceed the reference value. An angle change rate limiter is implemented to model the blade rotation speed.

3.2 Mechanical model
The mechanical model is used to simulate the WT drive train which consists of the rotor hub with blades, rotor shaft, and generator rotor. In order to reflect the torsional shaft oscillations that can occur due to a severe network disturbance, a two-mass model should be implemented [10]. This model is also adequate when investigating the effect of wind gusts, or the change in the active power set-point [11].

Fig. 4 shows the mechanical model implemented in this paper, where \( H_t \) and \( H_g \) are the inertia constants of the rotor and generator, respectively [12]. The damping coefficient is \( D \), and the shaft stiffness is \( K_{sf} \).

3.3 Converter control models
The block diagram of the generator side converter control is shown in Fig. 5. The reactive power reference (\( Q_{\text{ref}} \)) is set to zero and the converter controls the \( d \)-axis current (\( I_{d,\text{gen}} \)) to achieve unity power factor at the generator terminals. The active power reference (\( P_{\text{ref}} \)) can be calculated based on a maximum power point tracking method [13], or it can be given by the WPP control as shown in Fig. 2. The generator side controller adjusts the \( q \)-axis current (\( I_{q,\text{gen}} \)) in order to control the active power production (\( P_{\text{gen}} \)).

The grid side converter control shown in Fig. 6 keeps the DC-link voltage (\( V_{\text{dc}} \)) to its nominal value by controlling the \( d \)-axis grid current (\( I_{d,\text{grid}} \)). The AC voltage and reactive power at the WT terminal are controlled by adjusting the \( q \)-axis current (\( I_{q,\text{grid}} \)).

The reference voltage (\( V_{\text{ref}} \)) is calculated in the WPP control block and sent to the WT in order to keep the AC voltage at the terminal to its rated value. The block diagram in Fig. 6 is based on [14].
3.4 PMSG phasor model

The MATLAB/SIMULINK library documentation [8] provides the differential equations of the generator electrical model in the $d$–q rotor reference frame, where all the quantities in the rotor reference frame are referred to the stator as

$$\frac{d}{dt}I_{d,\text{gen}} = \frac{V_{d,\text{gen}}}{L_{sd}} - R_s L_{sd} I_{d,\text{gen}} + L_{sq} L_{sd} I_{q,\text{gen}} \omega_m$$

$$\frac{d}{dt}I_{q,\text{gen}} = \frac{V_{q,\text{gen}}}{L_{sq}} - R_s L_{sq} I_{q,\text{gen}} - L_{sd} L_{sq} I_{d,\text{gen}} - v_s - c_m v_s L_{sq}$$

where $I_{d,q,\text{gen}}$ are the stator current components, $V_{d,q,\text{gen}}$ are the stator voltage components, $v_s$ is the stator electrical frequency, $c_m$ is the flux of the permanent magnets, and $L_{sd,q}$ are the $d$-axis and $q$-axis inductances. The block diagram of the generator electric phasor model implemented in SIMULINK is shown in Fig. 7.

3.5 DC-link model

The power generated by the PMSG is supplied to the grid side converter through the DC-link. The dynamics of the capacitor voltage ($V_{dc}$) can be expressed as [15]

$$\frac{dV_{dc}}{dt} = P_{\text{gen}} - P_{\text{grid}}$$

The block diagram of the model is shown in Fig. 8.

3.6 Grid side RL filter phasor model

The WT is connected to the transformer through a three-phase RL filter. The single-phase equivalent circuit is shown in Fig. 9, and the model is described by the following differential equations [16]

$$V_{\text{conv}} - V_{\text{grid}} = L_f \frac{di_f}{dt} + R_f i_f$$

where $V_{\text{conv}}$ is the voltage at the converter side, and $V_{\text{grid}}$ is the voltage at the grid side, and $L_f$ and $R_f$ are the filter inductance and resistance, respectively. The differential equations of the filter in the rotating $d$–$q$ frame are as follows:

$$i_d = \frac{\omega}{L_f} \left( V_d - V_{d,\text{grid}} - R_f i_d + L_f i_q \right)$$

$$i_q = \frac{\omega}{L_f} \left( V_q - V_{q,\text{grid}} - R_f i_q - L_f i_d \right)$$

where $\omega = 2\pi f_{\text{rot}}$, and $V_d, V_q$ are the $dq$-components of $V_{\text{conv}}$. The filter block diagram is shown in Fig. 10.

3.7 WPP control (WPPC)

The WPPC in Fig. 2 measures the voltage ($V_{\text{POC}}$), active ($P_{\text{POC}}$) and reactive ($Q_{\text{POC}}$) powers at the POC. It sends voltage and active power references to the WPP. In this paper, the WPPC consists of an active power controller shown in Fig. 11, and a voltage controller shown in Fig. 12.

A similar voltage control has been used in [7]. It calculates a voltage reference ($V_{\text{ref}}$) based on the measured reactive power ($Q_{\text{POC}}$) and measured voltage ($V_{\text{POC}}$), and sends it to the WPP. Consequently, the WPP adjusts its output accordingly so the
The analysis is performed in MATLAB/SIULINK where the power system model is implemented using the SimPowerSystems [17].

The aggregated model of the WPP is connected to the grid through an aggregated WPP, and the small-signal stability is assessed by linearising the model. The linearisation is performed using the Simulink control design toolbox [18], directly on the initialised power system model. The control design toolbox uses exact linearisation for every function in the model.

4 Simulation results

The analysis is performed in MATLAB/SIULINK where the power system model is implemented using the SimPowerSystems [17]. The phasor WT model presented in the previous section is included in [19] for the two area network, thus considering the penetration of both the linear and non-linear systems in order to validate the linearisation.

4.1 Case study without wind power

The modal characteristics of the power system without wind power are analysed first. The model is linearised and its eigenvalues are computed. One inter-area mode and two local area modes are present in the system and their characteristics are given in Table 2. These values are very similar to the eigenvalues presented in [19] for the two area network, thus confirming these results are correct.

The modal analysis is complemented with time domain simulations of both the linear and non-linear systems in order to validate the linearisation of the model. The oscillations are excited by a step increase of 1% in the excitation voltage reference of $G_1$. The rotor speeds of generators $G_1$ and $G_3$ are shown in Fig. 14. The inter-area mode is clearly visible as the generators swing against each other. The linear and non-linear model responses overlap, validating the linearisation.

4.2 Case study with wind power

For this case, the aggregated phasor WPP model is included in the two area system at bus 5 as shown in Fig. 13. The wind power injected in the system is increased from 30 to 560 MW in five steps. The WPP is a scaled up 5 MW WT with the parameters of the generator and drive train given in Table 3. It is known that the modal characteristics of the power system can be affected by a significant change in the dispatch of existing power units and the power flow [20]. In this study, the influence of the proposed WT model on the power system oscillations is of interest. Therefore, the system power flow is kept unchanged by lowering the power set-point of generator $G_1$ for each step increase in wind power. The dispatch of the other three generators remains constant, and so does the MVA rating of all generators.

The entire model is linearised and the modal characteristics of the system with wind power are shown in Table 4. The results confirm that the full-load converter WT model has a small effect on the

![Fig. 13 Kandur’s two area system case study](image)

![Fig. 14 Rotor response of generators $G_1$ and $G_3$ with no wind power](image)

| Table 1 | WPP collector system parameters |
|-------------|-----------------|-------------|
| Collector parameters | Park transformer |
| $R_*$, $\Omega$ | $X_*$, $\Omega$ | $B_c$, $\mu$S | $X_p$, $\%$ |
| 0.086 | 0.070 | 321.97 | 12.2 |

<table>
<thead>
<tr>
<th>Voltage at the POC</th>
<th>Reference voltage in the WPPC</th>
</tr>
</thead>
<tbody>
<tr>
<td>$K_d$</td>
<td>0.04</td>
</tr>
</tbody>
</table>

| Table 2 | Modal characteristics of the power system without wind penetration |
|-------------|-----------------|-------------|
| Type of control | Inter-area mode | Area 1 local mode | Area 2 local mode |
| | Eigenvalue/(frequency in Hz, damping ratio) | | |
| PSS | $-0.689 \pm j4$ | $-2.56 \pm j8.42$ | $-2.49 \pm j8.9$ |
| (f = 0.65, | (f = 1.4, $\zeta = 0.291$) | (f = 1.47, | $\zeta = 0.269$) |
| $\zeta = 0.17$) | | |

<table>
<thead>
<tr>
<th>Table 3</th>
<th>Parameters for the wind turbine</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parameter</td>
<td>Value</td>
</tr>
<tr>
<td>Permanent magnet synchronous generator</td>
<td></td>
</tr>
<tr>
<td>rated power ($P_\text{nom}$)</td>
<td>5 MW</td>
</tr>
<tr>
<td>rated voltage ($V_\text{nom}$)</td>
<td>0.69 kV</td>
</tr>
<tr>
<td>$L_s$</td>
<td>0.017 pu</td>
</tr>
<tr>
<td>$L_{sd}$</td>
<td>1.0 pu</td>
</tr>
<tr>
<td>$L_{sq}$</td>
<td>0.7 pu</td>
</tr>
<tr>
<td>$\Psi_m$</td>
<td>1.4 pu</td>
</tr>
<tr>
<td>drive train</td>
<td></td>
</tr>
<tr>
<td>$H_e$</td>
<td>6.0 s</td>
</tr>
<tr>
<td>$H_d$</td>
<td>0.9 s</td>
</tr>
<tr>
<td>$D_s$</td>
<td>1.5</td>
</tr>
<tr>
<td>$K_{ef}$</td>
<td>296</td>
</tr>
</tbody>
</table>

This is an open access article published by the IET under the Creative Commons Attribution-NoDerivs License (http://creativecommons.org/licenses/by-nd/3.0/)
The degree of interaction of the WPP and generators in the inter-area oscillation is evaluated with the aid of the normalised participation factors shown in Table 5. Generator G1 has the highest participation in the inter-area mode, while the WT has a negligible effect on this mode shape. A similar conclusion is drawn in [7].

### 5 Conclusion

In this paper, a phasor model of a FSCWT for small-signal stability assessment is implemented in MATLAB/SIMULINK. The Simulink control design toolbox is used to linearise the entire initialised model and the linearisation result is validated by comparing the step responses of the linear and non-linear systems with dynamic simulations. The results show that the responses match for small disturbances (1% step in generator excitation voltage reference). Hence, the phasor model is linearised accurately.

The modal characteristics of the test system are analysed with and without wind power, and the results match previous research findings. The participation factors show that the FSCWT does not have a significant impact on the inter-area mode, which confirms the results from previous research. Therefore, the proposed model can be used either as a single WT or as an aggregated model to perform small-signal stability studies of power systems with large wind penetration.

### 6 References


---

**Table 4 Modal characteristics of the power system with wind penetration**

<table>
<thead>
<tr>
<th>Wind power, MW</th>
<th>Inter-area mode</th>
<th>Area 1 local mode</th>
<th>Area 2 local mode</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Eigenvalue/(frequency in Hz, damping ratio) with wind power</td>
<td></td>
<td></td>
</tr>
<tr>
<td>30</td>
<td>−0.692 ± j3.99</td>
<td>−2.6 ± j8.35</td>
<td>−2.49 ± j8.9</td>
</tr>
<tr>
<td></td>
<td>(f=0.64, ζ=0.171)</td>
<td>(f=1.39, ζ=0.297)</td>
<td>(f=1.47, ζ=0.269)</td>
</tr>
<tr>
<td>50</td>
<td>−0.694 ± j3.99</td>
<td>−2.62 ± j8.3</td>
<td>−2.49 ± j8.9</td>
</tr>
<tr>
<td></td>
<td>(f=0.64, ζ=0.171)</td>
<td>(f=1.39, ζ=0.301)</td>
<td>(f=1.47, ζ=0.269)</td>
</tr>
<tr>
<td>100</td>
<td>−0.699 ± j3.97</td>
<td>−2.67 ± j8.18</td>
<td>−2.49 ± j8.9</td>
</tr>
<tr>
<td></td>
<td>(f=0.64, ζ=0.173)</td>
<td>(f=1.37, ζ=0.311)</td>
<td>(f=1.47, ζ=0.269)</td>
</tr>
<tr>
<td>200</td>
<td>−0.707 ± j3.94</td>
<td>−2.74 ± j7.92</td>
<td>−2.49 ± j8.9</td>
</tr>
<tr>
<td></td>
<td>(f=0.65, ζ=0.176)</td>
<td>(f=1.33, ζ=0.327)</td>
<td>(f=1.47, ζ=0.27)</td>
</tr>
<tr>
<td>560</td>
<td>−0.704 ± j3.79</td>
<td>−2.6 ± j7.02</td>
<td>−2.49 ± j8.9</td>
</tr>
<tr>
<td></td>
<td>(f=0.61, ζ=0.182)</td>
<td>(f=1.19, ζ=0.347)</td>
<td>(f=1.47, ζ=0.27)</td>
</tr>
</tbody>
</table>

---

**Table 5 Normalised rotor participation factors**

<table>
<thead>
<tr>
<th>State variable</th>
<th>Participation factors for inter-area mode</th>
</tr>
</thead>
<tbody>
<tr>
<td>δ (G1)</td>
<td>0.32</td>
</tr>
<tr>
<td>δ (G2)</td>
<td>0.15</td>
</tr>
<tr>
<td>δ (G3)</td>
<td>1</td>
</tr>
<tr>
<td>δ (WT)</td>
<td>0.87</td>
</tr>
<tr>
<td>δ (WPP)</td>
<td>&lt;10⁻²</td>
</tr>
</tbody>
</table>

---

Fig. 15 Rotor responses of generators G1 and G3 with 560 MW wind power

Fig. 16 Reactive power at WPP PCC

Fig. 17 Voltage at WPP PCC

Fig. 18 Active power at WPP PCC

This is an open access article published by the IET under the Creative Commons Attribution-NoDerivs License (http://creativecommons.org/licenses/by-nd/3.0/)
A page of a document with the referenced text:

Rostamkolai N., Piwko R.J., Larsen E.V., ET AL.:


Knuppel T., Nielsen J.N., Jensen K.H., ET AL.:

MATLAB documentation center. Available at https://wwxw.mathworks.com/help/


