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Published in:
International Journal of Hydrogen Energy

Link to article, DOI: 10.1016/j.ijhydene.2016.08.035

Publication date:
2016

Document Version
Peer reviewed version

Link back to DTU Orbit

Citation (APA):
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To cite this version:

HAL Id: hal-01353305
https://hal.archives-ouvertes.fr/hal-01353305
Submitted on 11 Aug 2016

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Molecular dynamics simulations of ternary Pt$_x$Pd$_y$Au$_z$ fuel cell nanocatalyst growth

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Abstract: Molecular dynamics simulation of PEMFC cathodes based on ternary Pt$_{70}$Pd$_{15}$Au$_{15}$ and Pt$_{50}$Pd$_{25}$Au$_{25}$ nanocatalysts dispersed on carbon indicate systematic Au segregation from the particle bulk to the surface, leading to an Au layer coating the cluster surface and to the spontaneous formation of a Pt@Pd@Au core-shell structure. For Au content below 25at%, surface Pt$_x$Pd$_y$ active sites are available for efficient oxygen reduction reaction, in agreement with DFT calculations and experimental data. Simulations of direct core@shell system prepared in conditions mimicking those of plasma sputtering deposition pointed out an increase of the number of accessible Pt$_x$Pd$_y$ surface active sites. Core-shell nanocatalyst morphology changes occur due to impinging Pt kinetic energy confinement and dissipation.

Keywords: Molecular dynamics simulations; ternary nanocatalyst; PEMFC; fuel cell electrode; core-shell; alloy
1. Introduction

Improving design and/or reducing noble metal content in electrocatalysts for fuel cell electrodes while maintaining and/or increasing proton exchange membrane fuel cell (PEMFC) performance in terms of durability and power density are crucial challenges for PEMFC mass market applications [1-4]. A possible way consists in combining noble metals (Pt, Pd, Au ...) [5-11] and non-noble metals for preparing binary and ternary nanocatalysts. While non-noble metals are interesting from a cost reduction point of view, they may lead to reduced stability compared to pure platinum due to their dissolution capability [12-17]. Pt$_x$Pd$_{1-x}$ binary catalysts have been proposed as possible candidates for both PEMFC electrodes, the anode for the hydrogen oxidation reaction and the cathode for improved oxygen reduction reaction (ORR) compared with pure platinum [18-22]. At the same time, Au addition was proposed to improve durability of the nanocatalysts [23-27]. On the other hand, the atomic structure and morphology [28] also play very important roles in the electrocatalytic efficiency for ORR. Beside experimental investigations, molecular simulations in conditions matching experiments are also of particular interest [4, 29]. While density functional theory (DFT) simulations are able to predict both structure and composition of nanocatalysts leading to higher ORR efficiency, molecular dynamics (MD) simulations are able to predict their growth mode and the final possible structure when simulations are carried out with initial conditions consistent with experimental ones [30, 31]. This is of interest for comparing structure predictions and consistency with ORR efficiency and cyclic voltammetry results. The present work is devoted to MD simulations applied to the synthesis of PtPdAu ternary catalysts by both a wet chemical method at room temperature and a plasma sputtering co-deposition, based on the availability of recent detailed experimental [32] and DFT results [27].

2. Initial conditions for MD simulations.
Molecular dynamics simulation is a simple way to calculate at every times the trajectory of an ensemble of atoms subjected to forces, by solving the Newton equations of motion [33-37]. Growth of ternary catalysts is a typical situation, where MD simulations can be called for [32]. The required input parameters are only a relevant choice of initial conditions, especially the velocities that should be selected from velocity distributions as close as possible to those of experimental context studied.

In the present study, Pt, Pd and Au atoms are deposited on a model porous carbon issued from microscopy analysis [38], and thus expected to closely match carbon morphology of a PEMFC active layer. The dimensions of the model porous carbon substrate are $6 \times 6 \times 6 \text{ nm}^3$, containing 17,040 atoms, corresponding to a density of $1.57 \text{ g cm}^{-3}$ and to a porosity of 48%.

A picture of this substrate is shown in Figure 1.

![Figure 1. Snapshot of the model porous carbon substrate.](image)

Periodic boundaries are applied in the lateral directions, thus exposing the top of the structure as a free surface. 10,000 metal atoms are thrown toward the carbon substrate every delay time of 4 ps. The final simulated loading roughly corresponds to an experimental $10 \mu \text{g cm}^{-2}$ catalyst loading. The time step for integrating the equation of motion is 1 fs. The initial position of the atoms is 8Å above the substrate and with randomly chosen \{x,y\} coordinates.
The elemental type is randomly selected between Pt, Pd, Au before each atom injection, mimicking random deposition of elements, one after the other. Pt, Pd, Au atoms interact with one another and with the atoms of the nanostructured carbon substrate atoms within a cut-off distance of 8 Å. The initial velocities of the incoming Pt, Pd, Au atoms are sampled from a Maxwell-Boltzmann distribution with mean kinetic energies \( \langle E_{\text{Pt}} \rangle = 3.20 \text{ eV}, \langle E_{\text{Pd}} \rangle = 3.15 \text{ eV} \) and \( \langle E_{\text{Au}} \rangle = 2.62 \text{ eV} \) as most probable values in the case of plasma sputtering, and mean kinetic energies \( \langle E_{\text{Pt}} \rangle = \langle E_{\text{Pd}} \rangle = \langle E_{\text{Au}} \rangle = 0.026 \text{ eV} \) as most probable values for chemical synthesis at room temperature (or for high pressure plasma sputtering). The temperature of the substrate in all simulations is assumed to be 300 K. The substrate temperature is controlled by applying a Berendsen heat bath, employing a relaxation time of 1 ps. This allow the system to relax in a realistic way between two successive atom depositions. The carbon–carbon interactions in the substrate are modeled by a Tersoff potential [31, 39]. The noble metal interactions are treated by the Embedded Atom Method (EAM) potential [30, 31, 40, 41]. Such many-body potentials have been validated in conditions of sputtering deposition [40, 42, 43]. The metal–carbon interactions are estimated using a 12–6 Lennard–Jones (LJ) potential [44]. The simulations are carried out using LAMMPS software [37, 45].

3. Results and discussion

3.1 MD simulations for a chemical synthesis at room temperature of Pt\(_{50}\)Pd\(_{25}\)Au\(_{25}\) and Pt\(_{70}\)Pd\(_{15}\)Au\(_{15}\).

Previous experimental results [32] and DFT calculations [27] have proven that Pt\(_{50}\)Pd\(_{25}\)Au\(_{25}\) and Pt\(_{70}\)Pd\(_{15}\)Au\(_{15}\) lead to improved catalytic activity towards ORR and that gold could be responsible for improved catalyst stability. The choice for gold content below 25% was dictated by the necessity to obtain a good compromise between catalytic activity and stability, due to gold segregation to nanocatalyst surface [27, 32]. Similar trends in chemical ordering were revealed when more comprehensive searches were performed, utilizing genetic
algorithms to elucidate stable structures of PtAu and PtPdAu nanoparticles, though these searches were performed at 0K in vacuum [46,47].

Metal deposition is the first dynamical step leading to the nanocatalyst structure and composition. Figures 2 and 3 display growth steps of the Pt$_{50}$Pd$_{25}$Au$_{25}$ and Pt$_{70}$Pd$_{15}$Au$_{15}$ nanocatalysts, respectively, in conditions mimicking a room temperature synthesis.
Figure 2. Snapshots of the Pt$_{50}$Pd$_{25}$Au$_{25}$ nanocatalyst growth on porous carbon. Total number of injected atoms is: side view (a) 1000 (b) 2000 (c) 3000 (d) 5000 (e) 7000 (f) 10000, top view (g) 1000 (h) 2000 (i) 3000 (j) 5000 (k) 7000 (l) 10000. C, Pt, Pd, Au.
Figure 3. Snapshots of the Pt$_{70}$Pd$_{15}$Au$_{15}$ nanocatalyst growth on porous carbon. Total number of injected atoms is: side view (a) 1000 (b) 2000 (c) 3000 (d) 5000 (e) 7000 (f) 10000, top view (g) 1000 (h) 2000 (i) 3000 (j) 5000 (k) 7000 (l) 10000. ● C, ● Pt, ● Pd, ● Au.

Side views at lower Pt contents show cluster growth as core-shell structure in the early deposition time (Figures 2(a,b)): a core of Pt atoms is growing surrounded by a Pd
monoatomic shell and an outer Au shell. This is consistent with the hierarchy of surface energies deduced from the EAM parametrization. Table 1 gives the surface energies of the low index facets for Pt, Pd, Au compared to the experimental ones [41]. Although the calculated values from EAM differ from the average experimental values by ca. 40%, the order of the experimental values $E_{\text{Pt}} > E_{\text{Pd}} > E_{\text{Au}}$ is conserved, albeit a moderately enhanced propensity for structures with higher surface may be expected.

**Table 1.** EAM and average experimental surface energies of the low index faces of Pt, Pd, Au in Jm$^{-2}$ [40].

<table>
<thead>
<tr>
<th></th>
<th>Pt</th>
<th>Pd</th>
<th>Au</th>
</tr>
</thead>
<tbody>
<tr>
<td>(111)</td>
<td>1.44</td>
<td>1.22</td>
<td>0.79</td>
</tr>
<tr>
<td>(100)</td>
<td>1.65</td>
<td>1.37</td>
<td>0.92</td>
</tr>
<tr>
<td>(110)</td>
<td>1.75</td>
<td>1.49</td>
<td>0.98</td>
</tr>
<tr>
<td>Experimental, face averaged</td>
<td>2.49</td>
<td>2.00</td>
<td>1.5</td>
</tr>
</tbody>
</table>

Increasing the atom number results in the coalescence of small aggregates (Figure 2(c)). With a higher number of atoms deposited, the Au atoms always stay on the surface, meaning that in the course of cluster growth, segregation of Au always occurs. DFT-level calculations (see calculational details in Ref [48, 49]) performed on 1-2 nm icosahedral Pt nanoclusters show low activation energies for Au-surface segregation, which would be negligible under experimental deposition conditions. In these calculations, the Au atom was initially placed in the subsurface layer of the particle and the nudged elastic band pathway calculated for Au moving to the surface. This revealed negligible energy barriers for the particle reconstruction allowing for exposure of Au to the surface. Compared to this low activation barrier, there was significantly greater stabilization of the particle when Au occupied surface compared to subsurface positions. Nevertheless, some Au atoms are present inside big clusters (Figures 2(d,e,f)). This occurs for Au atoms far enough from the outer surface. This means that
segregation is only possible when a small number of atom exchanges are involved. When the Au atom is too deeply inside the cluster core, it can’t move towards the surface. Figures 2(c-f) also show that, even if a number of the Pd atoms segregate to the outer surface with Au atoms, when increasing the cluster size Pd and Pt atoms are mixed. Top views in Figures 2(g-l) indicate a low Pt surface ratio. Actually, at the final stage of metal deposition (Figures 2(f,l)), the cluster skin has a composition close to Pt_{10}Pd_{45}Au_{45} while the core has a composition of ca. Pt_{60}Pd_{20}Au_{20}.

Figure 3 displays snapshots illustrating the growth of Pt_{70}Pd_{15}Au_{15} prepared by a room temperature chemical method. As for the Pt_{50}Pd_{25}Au_{25}, the cluster growth starts by forming a Pt core surrounded by Pd and Au atoms, which finally cover almost completely the Pt core (Figures 3(a,b,c) and Figures 3(g,h)). When increasing the number of deposited atoms, clusters coalesce, keeping the memory of the initial clusters with the appearance of Pd boundaries inside the Pt core (Figures 3(d,e,f)). For further increasing cluster size in the course of deposition, platinum is occupying the surface skin to an increasing extent (Figure 3(j,k,l)). In the final stage, the surface composition Pt_{33}Pd_{33}Au_{33}, offers more efficient catalytic sites for ORR, while the core composition is Pt_{60}Pd_{20}Au_{20}.

In both cases, when increasing atom deposition numbers, clusters are polycrystalline as it is clearly shown on the side views of Figures 2(f) and 3(f). Crystallinity of model catalysts from MD simulations can be established by calculating the radial density function (RDF) g(r), which provides the nearest-neighbor (NN) distribution. Narrow peaks mean that the layer is very organized due to well-defined nearest-neighbor distances. Figure 4 displays the total RDF corresponding to figures 2(l) and 3(l).
Figure 4. Normalized total RDF $g(r)$ of final configuration corresponding to Figures 2(l) and 3(l).

In addition, Table 2 gives nearest-neighbor distances (up to the 7th) issued from ternary nanocatalysts RDF compared to theoretical face centered cubic crystal nearest-neighbor distances from single Pt, Pd and Au.

**Table 2.** NN distances (in Å) determined from RDF of figures 2(l) and 3(l), from theoretical fcc crystal Pt, Pd and Au. $a_0$ is the lattice parameter.

<table>
<thead>
<tr>
<th>NN distance</th>
<th>1st NN</th>
<th>2nd NN</th>
<th>3rd NN</th>
<th>4th NN</th>
<th>5th NN</th>
<th>6th NN</th>
<th>7th NN</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pt</td>
<td>$\frac{1}{\sqrt{2}} a_0$</td>
<td>$a_0$</td>
<td>$\frac{3}{\sqrt{2}} a_0$</td>
<td>$\sqrt{2} a_0$</td>
<td>$\frac{5}{\sqrt{2}} a_0$</td>
<td>$\sqrt{3} a_0$</td>
<td>$\frac{7}{\sqrt{2}} a_0$</td>
</tr>
<tr>
<td>Pd</td>
<td>2.77</td>
<td>3.92</td>
<td>4.80</td>
<td>5.54</td>
<td>6.20</td>
<td>6.79</td>
<td>7.33</td>
</tr>
<tr>
<td>Au</td>
<td>2.88</td>
<td>4.08</td>
<td>5.00</td>
<td>5.77</td>
<td>6.45</td>
<td>7.06</td>
<td>7.63</td>
</tr>
<tr>
<td>Simulated</td>
<td>2.72</td>
<td>3.92</td>
<td>4.82</td>
<td>5.57</td>
<td>6.27</td>
<td>-</td>
<td>7.37</td>
</tr>
</tbody>
</table>

The RDF of both ternary catalysts are very similar. The peak positions are close to Pt and Pd values, while Au values are slightly higher. One should notice that Au does not contribute significantly to the RDF except to the 1st NN because Au atoms are mainly located at the
surface, forming a monolayer. Moreover, the existence of the 2\textsuperscript{nd} NN is due to parallel atomic planes. Indeed, 2\textsuperscript{nd} NN always only lies in planes above and below the reference atom plane. There is no 2\textsuperscript{nd} NN atom in a single fcc atomic plane. So, well defined NN peaks and the presence of 2\textsuperscript{nd} NN demonstrate the crystalline state of the model ternary nanocatalysts from MD simulations. The very slight differences between the two RDF plots indicate that Pt\textsubscript{50}Pd\textsubscript{25}Au\textsubscript{25} is slightly less ordered than Pt\textsubscript{75}Pd\textsubscript{15}Au\textsubscript{15}. This is mainly due to the lower Pt content, which, as the predominant element, is driving the crystallinity of the sample. The simulation results presented above are in very good agreement with those obtained experimentally for the ORR activity of Pt\textsubscript{50}Pd\textsubscript{25}Au\textsubscript{25} and Pt\textsubscript{70}Pd\textsubscript{15}Au\textsubscript{15} catalysts prepared by a room temperature chemical method (water in oil microemulsion) \cite{32}; the low Pt surface composition in Pt\textsubscript{50}Pd\textsubscript{25}Au\textsubscript{25} compared with Pt\textsubscript{70}Pd\textsubscript{15}Au\textsubscript{15} is responsible of the lower activity of the former catalyst compared to that of the latter one. It is also worth to note that the surface enrichment by Au of the ternary catalysts after ageing tests was observed \cite{32}, confirming experimentally the propensity of gold atom to segregate towards the surface.

\section*{3.2 Simulation of plasma sputtering deposition and growth of Pd\textsubscript{25}Au\textsubscript{25}@Pt\textsubscript{50} core@shell ternary nanocatalysts}

As it is necessary to enrich the nanocatalyst surface by Pt in order to increase the ORR activity, a possible way is to use alternate plasma sputtering deposition, firstly of the core element(s) and secondly the shell element(s) \cite{31}. For comparison to the Pt\textsubscript{50}Pd\textsubscript{25}Au\textsubscript{25} ternary nanocatalyst grown in conditions matching chemical synthesis (but also plasma sputtering with high pressure-target to substrate distance product \cite{31}), we are considering the growth of the Pd\textsubscript{25}Au\textsubscript{25}@Pt\textsubscript{50} nanocatalyst.

Figure 5 displays the evolution of the Pd\textsubscript{25}Au\textsubscript{25}@Pt\textsubscript{50} nanocatalyst growth on the previous porous carbon model.
Figure 5. Snapshots of the deposited core@shell ternary nanocatalyst Pd\textsubscript{25}Au\textsubscript{25}@Pt\textsubscript{50}. Total number of injected atoms is: side view (a) 1000 (b) 2000 (c) 3000 (d) 5000 (e) 7500 (f) 8000, (g) 9000 (h) 9500 (i) 9600 (j) 10000; top view (k) 1000 (l) 2000 (m) 3000 (n) 5000 (o) 7500 (p) 8000, (q) 9000 (r) 9500 (s) 9600 (t) 10000.

In the AuPd core deposition step, the nanocatalyst is growing to form clusters. It should be noticed that initial clusters grow on the carbon pore entrance (Figure 5(k)), as a result of the
Au and Pd diffusion. This diffusion is due to the mean high kinetic energies involved in the present sputtering simulations: around 3 eV for Pd and Au (see Section 2). When first 5000 atoms, randomly selected as being either Pd or Au, have been released to the carbon substrate, the deposition of 5000 Pt atoms starts and the Pd-Au deposition is stopped. Figure 5(e) shows a well-defined core shell PdAu@Pt nanocatalyst with a very low surface Au content (Figure 5(o)). These snapshots are taken close before the starting of a cluster coalescence mechanism. When the clusters have coalesced, the nanocatalyst morphology changes to that of a nanowire, and for further Pt deposition, the nanowire is continuously enriched by segregating Au atoms (Figure 5(p-r)). When continuing Pt deposition, the Au coated nanowire suddenly transforms into nanofilm morphology (Figure 5(h-i and r-s)), for which the outermost surface is coated by an almost complete Au monolayer. It should be noted that the film interface with carbon is also coated by an Au monolayer. This shows the strong propensity of Au to diffuse outside the nanocatalyst. A small quantity remains in the Pd phase, as the difference in surface energies is lower than for Pt. While the final nanofilm is almost completely covered by an Au atom monolayer, the efficiency of the catalyst for ORR will be affected. Though by controlling the sputtering process, suitable morphologies and surface compositions can be tuned to the desired one, which is relevant for the targeted catalysis efficiency.

For the nanowire phase, where Pt is still released to the surface, the structure evolved from crystalline to disordered, just before the transformation into nanofilm morphology. This can be seen on the side view of Figure 5(g, h); the corresponding RDF plot is displayed in Figure 6, where the structure change from crystalline one to disordered one is depicted by the broadening of 1\textsuperscript{st}, 3\textsuperscript{rd} and 5\textsuperscript{th} NN peaks and wiping out of 2\textsuperscript{nd}, 4\textsuperscript{th} and 6\textsuperscript{th} NN peaks.
The nanofilm formed just after the transition is also disordered with the same effects on the RDF plots, i.e. broadening and wiping out of peaks. Further deposition of Pt atoms leads to complete crystallization of the nanofilm (Figure 5(i-j)). This is supported by the total RDF plots (Figure 7) just after the nanowire to nanofilm transformation and at the end of the simulated deposition.
Figure 7. Total RDF plot of the initial and final Pd$_{25}$Au$_{25}$@Pt$_{50}$ nanofilm corresponding to Figure 5(i and j).

Figure 7 gives a clear account of the crystallization of the nanofilm for the further Pt deposition. The final nanofilm exhibits an almost perfectly crystallized structure.

One can further notice that the RDF of the non-crystallized film is similar to the RDF of a liquid. Indeed when checking nanocatalyst temperature increase above the thermostated substrate at 300K (Figure 8), temperature peaks correspond to phase transformation from cluster to nanowire, nanowire crystallization, nanowire to nanofilm transformation and nanofilm crystallization, followed by temperature relaxation into the substrate. This means that the energy delivered by Pt impact on the existing nanocatalyst is confined into the nanostructure and when it increases due to Pt deposition, it leads to various transformations. The nanofilm morphology allows completely dissipating the energy into the substrate due to the highest nanocatalyst contact area with the carbon substrate. One should recall that the only
way to dissipate energy of the cluster is through interaction with the thermostated substrate. The maximum temperature rise is 350 K leading to a catalyst film temperature of 650 K. Supported Pt nanoclusters are known to fuse below 650 K [50]. Transition to nanofilm in a fused state is expected to have higher wettability and thus the nanofilm can relax to a crystalline state when cooling down.

**Figure 8.** Nanocatalyst temperature increase during the deposition. The various phase changes are indicated.

**4. Conclusion**

Molecular Dynamics simulations are carried out for describing the growth of carbon supported Pt$_{50}$Pd$_{25}$Au$_{25}$ and Pt$_{70}$Pd$_{15}$Au$_{15}$ in conditions matching chemical synthesis or soft
plasma sputtering deposition at high pressure. Comparison with DFT prediction and
electrochemical analysis highlights the role of spontaneous upward diffusion of gold atoms.
Moreover, measured ORR decreasing activity on chemically synthetized Pt\textsubscript{x}Pd\textsubscript{y}Au\textsubscript{z} above
25% atomic Au content is consistent with the surface Au content increase, and in turn with the
lowering of the surface PdPt active site number predicted by MD simulations.
An alternative to chemical synthesis is the plasma sputtering method that allows versatile
deposition of nanocatalyst. MD simulations matching conditions of such a technique show
possible tuning of the composition, structure and morphology of the cluster. High surface
active site content is possible when considering core@shell structure growth. MD simulations
show that morphology transformation, occurring during such a growth process, is driven by
the kinetic energy transferred by Pt atoms on the already deposited PdAu core. This
transferred kinetic energy is thus confined in the nanostructure for a while, allowing
successive transformation from cluster to nanowire and nanofilm due to nanocatalyst
temperature increase. These transformations allow final thermal relaxation of the
nanocatalyst.

**Acknowledgments**

The research leading to these results has received funding from the European Union's Seventh
Framework Programme (FP7/2007-2013) for the Fuel Cells and Hydrogen Joint Technology
Initiative under grant agreement #325327 (SMARTCat project).

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