Investigation of the crystal structure of a basic bismuth(III) nitrate with the composition [Bi6O4(OH)(4)](0.54(1)) [Bi6O5(OH)(3)](0.46(1))(NO3)(5.54(1))

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A basic bismuth(III) nitrate with the composition \([\text{Bi}_6\text{O}_4\text{(OH)}_4]^{0.54(1)}[\text{Bi}_6\text{O}_5\text{(OH)}_3]^{0.46(1)}(\text{NO}_3)^{5.54(1)}\) formed in a slow crystal growth mode has an ordered crystal structure with the monoclinic space group \(P2\), and lattice parameters \(a = 15.850(3)\), \(b = 14.986(3)\), \(c = 18.230(4)\) Å, \(\beta = 107.329(17)\)° and volume \(V = 4133.6\) Å\(^3\). In a very fast crystal growth mode the complex ions disorder in another \(P2\) cell, with slightly different lattice parameters \(a = 15.8404(1), b = 15.1982(1), c = 18.3122(1)\) Å, \(\beta = 106.829(1)\)° and \(V = 4219.8\) Å\(^3\). This cell can be related to two smaller cells: a monoclinic \(C2/m\) cell with \(a = 13.7161(1), b = 15.1943(1), c = 10.2399(1)\) Å, \(\beta = 98.586(1)\)° and \(V = 2110.1\) Å\(^3\) and a trigonal \(R3\) cell with \(a = 15.18650(6), c = 15.8416(1)\) Å (hexagonal setting) and \(V = 3164.1\) Å\(^3\). These smaller cells correspond to average structures and hence the X-ray data do not account for the difference in the structures of the two different complex ions. However, when analysing neutron powder diffraction data, it is possible to distinguish between the two complex ions using a trigonal structures of the compound. The chemistry of basic bismuth(III) nitrates has in the past been established from chemical analysis and X-ray single crystal structure analysis, and some X-ray powder patterns of them are reported in the ICDD data base, see Tables 1 and 2.\(^{1-10}\) The crystal structure investigations\(^{1-10}\) showed that these compounds may contain the two complex ions \([\text{Bi}_6\text{O}_5\text{(OH)}_3]^{5+}\) and \([\text{Bi}_6\text{O}_4\text{(OH)}_4]^{6+}\). The compounds listed in Tables 1 and 2 are formed in acid media where the equilibrium shown in eqn 1

\[
[\text{Bi}_6\text{O}_4\text{(OH)}_4]^{6+} + \text{H}_2\text{O} = [\text{Bi}_6\text{O}_5\text{(OH)}_3]^{5+} + \text{H}_3\text{O}^+ \tag{1}
\]

is pH dependent, so that a low pH level favours the formation of the compounds \([\text{Bi}_6\text{O}_4\text{(OH)}_4]^{6+}\)\(y\text{H}_2\text{O}\) (\(y = 1\) and 4), and a slightly higher pH level results in the formation of the compound \([\text{Bi}_6\text{O}_5\text{(OH)}_3]^{5+}\)\(y\text{H}_2\text{O}\). Summaries of the synthetic routes for

Table 1 The basic bismuth(III) nitrates. Composition and published X-ray powder patterns. The short names were introduced in a previous investigation\(^{3}\)

<table>
<thead>
<tr>
<th>Compound</th>
<th>Batch or short name</th>
<th>ICDD cards</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>([\text{Bi}_6\text{O}_5\text{(OH)}_3]^{5+})(4\text{H}_2\text{O})</td>
<td>C</td>
<td>84–2189</td>
<td>3</td>
</tr>
<tr>
<td>([\text{Bi}_6\text{O}_5\text{(OH)}_3]^{5+})(\text{H}_2\text{O})</td>
<td>D</td>
<td>71–1360, 70–2235</td>
<td>4,5</td>
</tr>
<tr>
<td>([\text{Bi}_6\text{O}_5\text{(OH)}_3]^{5+})(3\text{H}_2\text{O})</td>
<td>A</td>
<td>70–1226</td>
<td>6</td>
</tr>
<tr>
<td>([\text{Bi}_6\text{O}_5\text{(OH)}_3]^{5+})(2\text{H}_2\text{O})</td>
<td>X</td>
<td>4,5</td>
<td></td>
</tr>
<tr>
<td>([\text{Bi}_6\text{O}_5\text{(OH)}_3]^{5+})(\text{H}_2\text{O})</td>
<td>X</td>
<td>7*</td>
<td></td>
</tr>
<tr>
<td>([\text{Bi}_6\text{O}_5\text{(OH)}_3]^{5+})(\text{H}_2\text{O})</td>
<td>01–072–7618</td>
<td>9</td>
<td></td>
</tr>
<tr>
<td>([\text{Bi}_6\text{O}_5\text{(OH)}_3]^{5+})(\text{H}_2\text{O})</td>
<td>10</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

\* The present investigation has led to the conclusion that batch-X samples do not contain \(\text{H}_2\text{O}\) (see section 1).
the formation of the basic bismuth(III) nitrates can be found in the literature.\textsuperscript{11}

During an investigation of homogeneous hydrolysates by the use of aqueous solutions of urea,\textsuperscript{12} it was observed that a homogeneous hydrolysis of bismuth(III) nitrate resulted in the formation of a crystalline compound called batch-X.\textsuperscript{7} Chemical analyses indicated that this compound could have the composition $[\text{Bi}_6\text{O}_5(\text{OH})_3]^{(\text{NO}_3)_5}$. A subsequent analysis resulted in the composition $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{(\text{NO}_3)_5.5}$. The thermogravimetric analysis of batch-X material showed a loss in weight after transformation to $\alpha$-$\text{Bi}_2\text{O}_3$ of 19.4%, which was in accord with the loss of 19.2% for a compound with the composition $[\text{Bi}_6\text{O}_5(\text{OH})_3]^{(\text{NO}_3)_5}$. However, this was less than the expected 19.7% Bi and 19.5% NO$_3^-$ in good agreement with the composition $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{(\text{NO}_3)_5}$. The NMR pattern supported that batch-X is related to the general formula: $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{(\text{NO}_3)_5}$. This can be interpreted as the assignment of chemical composition to batch-X would have to be a choice between these two chemical formulas. Therefore, because the present neutron diffraction crystal structure analyses do not indicate any water content in batch-X material, it is concluded that these samples are without water of crystallisation.

A synchrotron X-ray powder pattern of a batch-X sample was indexed in a trigonal cell using hexagonal setting with the unit cell $a = 15.185(1)$, $c = 15.834(2)$ Å and the space group R3.\textsuperscript{7}R3 Depending upon how many very weak reflections were used in the indexing calculations,\textsuperscript{7} the data could also be indexed with a monoclinic cell with $a = 10.237(2)$, $b = 7.592(2)$, $c = 18.230(4)$ Å and $\beta = 98.65(2)$°.\textsuperscript{9} A number of attempts to solve the structure of samples from batch-X using synchrotron X-ray single crystal and powder diffraction data\textsuperscript{7,9} failed when using the trigonal cell, because unrealistically short Bi–Bi distances (1.83–2.28 Å) were obtained.

Subsequently, two crystal structure investigations on basic bismuth(III) nitrates, $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{(\text{NO}_3)_5}$ and $[\text{Bi}_6\text{O}_5(\text{OH})_3]^{(\text{NO}_3)_5}$,\textsuperscript{9} have been published by Henry et al. The model of the first structure\textsuperscript{9} has a monoclinic unit cell, $a = 15.850(3), b = 14.986(3), c = 18.230(4)$ Å, $\beta = 107.329(17)$° and the space group $P2_1$. The chemical formula of this compound corresponds to the general formula: $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{(\text{NO}_3)_5}$. With $x = 0.0$, the model contains four independent Bi$_6$-octahedra or a total of 24 independent Bi-atoms. The calculated powder pattern of $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{(\text{NO}_3)_5}$ (ICDD card no. 01-072-7618) has 199 reflections in the $d$-spacing range 17.40–2.271 Å, including a large number of weak and not well resolved peaks.

The model of the second structure\textsuperscript{5} has a trigonal unit cell, $a = 15.1332(6)$ and $c = 15.7909(9)$ Å (hexagonal setting) and the space group R3.\textsuperscript{5} The chemical formula of that compound corresponds to the general formula: $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{(\text{NO}_3)_5}$. With $x = 0.5$, it contains six $[\text{Bi}_6\text{O}_5(\text{OH})_3]$ ions packed into the structure and in addition six other $[\text{Bi}_6\text{O}_5(\text{OH})_3]$ ions packed close to the first set of ions in a complex way, resulting in very short Bi–Bi distances (Bi1–Bi2a = 1.724 and 2.334 Å; Bi1b–Bi2b = 1.795 and 2.398 Å),\textsuperscript{5} which indicates that the structure could be disordered or contains stacking faults.

From a comparison between the patterns calculated by means of the model parameters listed in Ref. 9 and 10, it is evident that the structure of $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{(\text{NO}_3)_5}$ differs from that of $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{+(\text{NO}_3)_5}$. The observed synchrotron X-ray powder pattern of the batch-X sample $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{+(\text{NO}_3)_5}$, \textit{H}_2\text{O}\textsuperscript{+} was apparently almost identical to the calculated pattern of $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{+(\text{NO}_3)_5}$ with 24 well resolved reflections in the $d$-spacing range 7.597–2.262 Å. However, because a similar model had already been explored and rejected in the previous investigations of batch-X samples,\textsuperscript{7,8} (see above) it seemed relevant to consider other probable model structures of the group of compounds with the general formula $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{+(\text{NO}_3)_5}\text{·}\text{H}_2\text{O}\textsuperscript{+}$. As a starting point, the following hypotheses will be tested:

- The model of the structure of $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{+(\text{NO}_3)_5}$ is related to that of $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{+(\text{NO}_3)_5}$.
- The two compounds reported as $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{+(\text{NO}_3)_5}\text{·}\text{H}_2\text{O}\textsuperscript{+}$ and $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{+(\text{NO}_3)_5}$ have almost identical powder patterns and are assumed to be related.
- The compounds reported as $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{+(\text{NO}_3)_5}\text{·}\text{H}_2\text{O}\textsuperscript{+}$, $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{+(\text{NO}_3)_5}$ and $[\text{Bi}_{6.5}\text{O}_3(\text{OH})_3]^{+(\text{NO}_3)_5}$ may all be described as structures containing $[\text{Bi}_{6.5}\text{O}_5(\text{OH})_3]^+$ ions and $[\text{Bi}_{6.5}\text{O}_5(\text{OH})_3]^+$ ions in an ordered or a disordered arrangement.

Below, section 2 presents the X-ray and neutron diffraction data for samples of batch-X material followed, in section 3, by model considerations that are important when testing if these hypotheses are valid or not. The final data analyses related to these models are presented in section 4 and summary and conclusion in section 5.

### Table 2 Unit cell dimensions for the compounds listed in Table 1

<table>
<thead>
<tr>
<th>Ref.</th>
<th>$a$/Å</th>
<th>$b$/Å</th>
<th>$c$/Å</th>
<th>$\beta$ (°)</th>
<th>Volume/Å$^3$</th>
<th>Space group</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>9.059(4)</td>
<td>17.050(2)</td>
<td>18.269(2)</td>
<td>120.00(1)</td>
<td>2443.7</td>
<td>$P_2_1/c$</td>
</tr>
<tr>
<td>4</td>
<td>9.313(2)</td>
<td>13.514(7)</td>
<td>19.575(5)</td>
<td>114.12(1)</td>
<td>2248.5</td>
<td>$P_2_1/c$</td>
</tr>
<tr>
<td>5</td>
<td>9.289(2)</td>
<td>13.462(4)</td>
<td>19.327(5)</td>
<td>114.13(2)</td>
<td>2228.5</td>
<td>$P_2_1/c$</td>
</tr>
<tr>
<td>6</td>
<td>17.152(1)</td>
<td>9.181(1)</td>
<td>17.752(1)</td>
<td>127.830(7)</td>
<td>2207.9</td>
<td>$P_2_1/c$</td>
</tr>
<tr>
<td>7</td>
<td>10.237(2)</td>
<td>7.592(2)</td>
<td>6.863(2)</td>
<td>98.65(2)</td>
<td>527.3</td>
<td>R3</td>
</tr>
<tr>
<td>8</td>
<td>15.185(1)</td>
<td>15.185(1)</td>
<td>15.834(2)</td>
<td>3131.8</td>
<td>3161.9</td>
<td>R3</td>
</tr>
<tr>
<td>9</td>
<td>15.850(3)</td>
<td>14.986(3)</td>
<td>18.230(4)</td>
<td>107.329(17)</td>
<td>4133.7</td>
<td>$P_2_1$</td>
</tr>
<tr>
<td>10</td>
<td>15.1332(6)</td>
<td>15.1332(6)</td>
<td>15.7909(9)</td>
<td>3131.8</td>
<td>R3</td>
<td></td>
</tr>
</tbody>
</table>

* Equivalent to $C_2/m$ in this work.
Table 3  Unit cell parameters obtained in the indexing of patterns and refinement of the unit cells (this work)

<table>
<thead>
<tr>
<th>Pattern/sample</th>
<th>Technique</th>
<th>(a/\text{Å})</th>
<th>(b/\text{Å})</th>
<th>(c/\text{Å})</th>
<th>(\beta(°))</th>
<th>Volume/Å(^3)</th>
<th>Space group</th>
<th>Program/case</th>
</tr>
</thead>
<tbody>
<tr>
<td>1/X X-ray, powder</td>
<td>15.1865(1) 15.1865(1) 15.8416(1)</td>
<td>3164.1</td>
<td>R(^3)</td>
<td>FullProf/A</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>15.8404(2)</td>
<td>15.1982(1)</td>
<td>18.3122(1)</td>
<td>106.829(1)</td>
<td>4219.8</td>
<td>P(^2)</td>
<td>FullProf/B</td>
<td></td>
<td></td>
</tr>
<tr>
<td>13.7154(2)</td>
<td>15.1928(1)</td>
<td>20.4696(5)</td>
<td>98.502(1)</td>
<td>4218.5</td>
<td>P(^2)</td>
<td>FullProf/C</td>
<td></td>
<td></td>
</tr>
<tr>
<td>13.7161(1)</td>
<td>15.1943(1)</td>
<td>10.2399(1)</td>
<td>98.386(1)</td>
<td>2110.1</td>
<td>C(2/m)</td>
<td>FullProf/D</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6.837(1)</td>
<td>15.186(1)</td>
<td>10.235(1)</td>
<td>98.66(2)</td>
<td>1059.6</td>
<td>P(^2)</td>
<td>DICOVOL04</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2/X neutron, powder</td>
<td>15.1846(6)</td>
<td>15.1846(6)</td>
<td>15.8470(5)</td>
<td>3164.4</td>
<td>R(^3)</td>
<td>FullProf</td>
<td></td>
<td></td>
</tr>
<tr>
<td>13.742(1)</td>
<td>15.151(1)</td>
<td>20.522(1)</td>
<td>98.42(1)</td>
<td>4114.1</td>
<td>P(^2)</td>
<td>FullProf</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6.849(2)</td>
<td>7.589(2)</td>
<td>10.236(1)</td>
<td>98.61(2)</td>
<td>526.0</td>
<td>P(^2)</td>
<td>DICOVOL04</td>
<td></td>
<td></td>
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<tr>
<td>13.745</td>
<td>15.183</td>
<td>10.257</td>
<td>98.275</td>
<td>2118.3</td>
<td>P(^2)</td>
<td>ITO</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3/X* X-ray, powder</td>
<td>15.200(1)</td>
<td>15.200(1)</td>
<td>15.863(1)</td>
<td>3174.0</td>
<td>R(^3)</td>
<td>FullProf</td>
<td></td>
<td></td>
</tr>
<tr>
<td>15.8933(5)</td>
<td>14.3337(7)</td>
<td>18.297(1)</td>
<td>106.95(5)</td>
<td>3987.2</td>
<td>P(^2)</td>
<td>FullProf</td>
<td></td>
<td></td>
</tr>
<tr>
<td>13.168(1)</td>
<td>15.1964(5)</td>
<td>20.585(1)</td>
<td>98.23(1)</td>
<td>4076.8</td>
<td>P(^2)</td>
<td>FullProf</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5/X X-ray, crystal X7B NSLS</td>
<td>15.1797</td>
<td>15.1797</td>
<td>15.8364</td>
<td>3106.2</td>
<td>R(^3)</td>
<td>SC-1</td>
<td></td>
<td></td>
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<tr>
<td>13.716(3)</td>
<td>15.176(3)</td>
<td>10.225(3)</td>
<td>98.60(3)</td>
<td>2104.4</td>
<td>C(2/m)</td>
<td>SC-2</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

* See section 2 for further information.

2. Experimental

The chemicals used when making the batches of bismuth(III) nitrate prepared for the present investigation were routinely checked by collecting X-ray diffraction patterns using a Stoe-Stadie diffractometer with CuK\(\alpha\) radiation, \(\lambda = 1.540598\) Å. The produced samples were checked in the same way and the patterns were indexed with the programs DICVOL04\(^{19}\) and ITO\(^{20}\) in order to confirm that the samples used were all batch-X samples. Refinements of the unit cell parameters were then made using the program FullProf\(^{18}\) in the profile matching mode (Le Bail type matching). Several samples were prepared and used to collect better data, which were used in the crystal structure analyses presented in section 4. The final data consisted of two synchrotron X-ray powder diffraction patterns, one neutron powder diffraction pattern and two sets of independent single crystal synchrotron X-ray diffraction data as listed below.

**Powder pattern 1**

A synchrotron X-ray powder pattern was recorded at 25 °C on the Swiss Norwegian beam line at ESRF using a wavelength \(\lambda = 1.0982\) Å and covering the 2\(\theta\) range from 8.00° to 56.80° in steps of 0.01°.\(^{7}\) The pattern is shown in Fig. 1. It can be indexed in a trigonal and three monoclinic unit cells with refined cell parameters as listed in Table 3.

**Powder pattern 2**

A neutron powder diffraction pattern was recorded at 25 °C using the diffractometer D2B at ILL using a wavelength \(\lambda = 1.4949\) Å and covering the 2\(\theta\) range from 11.065° to 155.915° in steps of 0.050°. The values found by indexing and subsequent refinements of the unit cell parameters are listed in Table 3. This pattern is shown Fig. 2 and it can also be indexed in a trigonal and three monoclinic unit cells.

**Powder pattern 3**

A synchrotron X-ray powder pattern was recorded on the diffractometer at the beam line X7B at NSLS Brookhaven National Laboratory in an in situ experiment where a mixture of [Bi\(_3\)O\(_5\)(OH)\(_3\)](NO\(_3\))\(_5\)·3H\(_2\)O and urea was converted hydrothermally to a batch-X material, and finally to Bi\(_2\)O\(_2\)CO\(_3\).\(^{8}\) The

![Fig. 1](image_url)  

The synchrotron X-ray powder diffraction pattern of a batch-X sample recorded at 25 °C. The figure shows at the top: (o) observed and (—) calculated patterns, and below: the difference (—). The vertical ticks mark the Bragg peak positions. Using FullProf\(^{18}\) in the profile matching mode (Le Bail fit) with the R\(^3\) space group resulted in \(\chi^2 = 2.9, R_{wp} = 0.12\%, R_t = 0.25\%\) and profile parameters \(U = 0.031(3), V = -0.005(1), W = 0.0011(1)\) and \(Y = 0.0258(4)\). The position of the first Bragg reflection observed in this pattern with \(d_{10} = 7.59\) Å is marked. For further details see the text and Table 3.
Fig. 2  Neutron powder diffraction pattern of a batch-X sample recorded at 25 °C. The figure shows at the top (●) observed and (—) calculated patterns and below the difference (△). The vertical ticks mark the Bragg peak positions. Using FullProf\textsuperscript{15} in the profile matching mode (Le Bail fit) with the R\textbar\space{3} space group resulted in $c_2 = 1.4$, $R_{\text{Bragg}} = 0.27\%$, $R_F = 0.40\%$ and profile parameters $U = 0.08(1)$, $V = -0.09(1)$, $W = 0.060(3)$ and $Y = 0.082(3)$. The position of the first Bragg reflection observed in this pattern with $d_{110} = 7.59\ A$ is marked and shown on expanded scales in the inset. For further details see the text and Table 3.

wavelength was $\lambda = 0.9022\ \text{Å}$ covering a 2$\theta$ range from 3.0033° to 44.9902° in 0.0196° increments. The selected pattern recorded at 100 °C had a weak low angle reflection at 2$\theta = 5.107^\circ$ corresponding to a $d$-spacing of 10.13 Å. This reflection was not observed in powder patterns 1 and 2, because these patterns did not include the corresponding low angle regions. The pattern 3 can be indexed in a trigonal and two monoclinic cells with refined unit cell parameters listed in Table 3. Pattern 3 may also be indexed in the trigonal cell of pattern 1, but with a different zero offset and a slightly larger $\chi^2$. The diffraction data for pattern 3 is displayed in Fig. 3b as a function of scattering vector length $|q| = 2\pi/d = 4\pi\sin(\theta)/\lambda$ in order to allow direct comparison with the corresponding data for patterns 1 (3a) and 2 (3c).

Fig. 3  Powder diffraction patterns of batch-X samples displayed as intensity vs. scattering vector length $|q| = 2\pi/d = 4\pi\sin(\theta)/\lambda$. The data in (a) and (c) is X-ray and neutron data recorded at 25 °C, respectively, while the data in (b) is X-ray data recorded at 100 °C (see text for an explanation). The figure shows the (●) observed and (—) calculated patterns. Using FullProf\textsuperscript{15} in the profile matching mode (Le Bail fit) for the data in (b) with the R\textbar\space{3} space group resulted in $\chi^2 = 0.9$, $R_{\text{Bragg}} = 0.19\%$, $R_F = 0.29\%$ and profile parameters $U = -0.55(3)$, $V = 0.21(1)$, $W = 0.011(1)$ and $Y = 0.024(2)$. The position of the first Bragg reflection observed in this pattern with $d_{110} = 10.13\ A$ is marked and shown on an expanded intensity scale in the inset (d). For further details see captions to Fig. 1 and 2, the text and Table 3.
Single crystal data

Two sets of single crystal synchrotron X-ray diffraction data were collected and they agree with the results from the powder diffraction data. Data set SC-1 was recorded on a diffractometer at HASYLAB, Hamburg using the wavelength $\lambda = 0.6562\ \text{Å}$. Data set SC-2 was recorded on a diffractometer at the beam line X7B at NSLS Brookhaven National Laboratory using the wavelength $\lambda = 0.9269\ \text{Å}$. The unit cells used in these measurements are also listed in Table 3. At HASYLAB a trigonal cell was used, and at NSLS Brookhaven a monoclinic cell. Both data sets were recorded at $25\ ^\circ\text{C}$.

3. Space group, unit cells and possible structure models

3.1. Space group determination in the case of a heavy atom structure

It should be noted that, for these compounds, the determination of the space group and crystal structure from X-ray diffraction is that of a typical heavy atom structure analysis because the scattering is dominated by the scattering contributions from the Bi atoms. A possible pitfall is therefore to overlook very weak reflections in the determination of unit cell and space group when analysing data from both powder and single crystal diffractometers. The result may well be that the unit cell is determined too small and hence that the space group is determined incorrectly. Thus, the cell used in the X7B NSLS measurements had a volume only half that of the original monoclinic cell found for the $[\text{Bi}_6\text{O}_4(\text{OH})_5]_6^+ (\text{NO}_3)_9$ structure (Table 1). Furthermore, the two independent acquisitions of single crystal data from batch-X crystals resulted in assignments of a trigonal space group for one of the crystals and a monoclinic space group for the other crystal. Similar conflicting results were obtained when indexing the powder diffraction patterns (see Table 3), e.g. the very small cells found when using DICVOL04. A significant evidence of the fact that these smaller unit cells are incorrect is the observation of the Bragg peak at $d \sim 10\ \text{Å}$ in pattern 3 (Fig. 3b and 3d). In the Le Bail profile matching fits to the overlapping peaks at $d_{100} = 10.143\ \text{Å}$ and $d_{110} = 9.872\ \text{Å}$ with intensity ratio $10:1$ in space group $P\overline{2}_1$.

The crystal structures of the compounds listed in Table 1 may all be described in the monoclinic space groups, except for the structure of $[\text{Bi}_6\text{O}_5(\text{OH})_4]_6^+ (\text{NO}_3)_9$. They contain four or eight of the complex Bi ions. Only $[\text{Bi}_6\text{O}_5(\text{OH})_4]_6^+ (\text{NO}_3)_9$ is described in the trigonal space group $R\overline{3}$, and contains a total of six complex Bi octahedra. A relevant question to ask is therefore: can the $R\overline{3}$ structure be related to the monoclinic structure described in the space group $P\overline{2}_1$? In the following, several structural models are considered in order to answer this question.

3.2. The published structure model with stacking faults of the complex Bi-ions. The crystals prepared for the structure investigation of $[\text{Bi}_6\text{O}_5(\text{OH})_4]_6^+ (\text{NO}_3)_9$ were obtained in a rapid growth mode, where drops of an acid bismuth nitrate solution were dropped into a 50:50 ethanol water solution. This resulted in a rapid dilution and precipitation of crystals where the two complex ions were packed in the crystals in a disordered way. Similarly, the crystals of samples from bath-X were also made in a process of very fast crystal growth. Here, the hydrolysis of urea to ammonia and carbon dioxide pulled the equilibrium of the ions from $[\text{Bi}_6\text{O}_5(\text{OH})_4]_6^+$ towards $[\text{Bi}_6\text{O}_5(\text{OH})_4]_6^+$, a process also observed in the in situ experiment. As argued in section 1, it is more likely that batch-X material does not contain a
Table 4 Relevant data for the original and additional unit cell choices associated with this work* and ref. 9 and 10

<table>
<thead>
<tr>
<th>Space group</th>
<th>P2₁(M1) monocl.</th>
<th>O1 orthorhombic</th>
<th>P2₁ monoclinic</th>
<th>C2₁/m monoclinic</th>
<th>R3 trigonal</th>
<th>O2 orthorhombic</th>
<th>P2₁(M2) monoclinic</th>
</tr>
</thead>
<tbody>
<tr>
<td>ac-plane projection A B C D</td>
<td>K L M N</td>
<td>A E F C</td>
<td>G H I J</td>
<td>O P Q R</td>
<td>S T U V</td>
<td>X Y Z W</td>
<td></td>
</tr>
<tr>
<td>Ref. this work</td>
<td>this work</td>
<td>this work</td>
<td>this work</td>
<td>this work</td>
<td>this work</td>
<td>this work</td>
<td></td>
</tr>
<tr>
<td>Fig.</td>
<td>4a and 4b</td>
<td>4a</td>
<td>4b</td>
<td>4d</td>
<td>5b</td>
<td>5a</td>
<td>5a and 5b</td>
</tr>
<tr>
<td>a/Å</td>
<td>15.8404</td>
<td>15.8404</td>
<td>13.7154</td>
<td>13.7449</td>
<td>15.1761</td>
<td>15.1765</td>
<td>15.8146</td>
</tr>
<tr>
<td>Volume/Å³</td>
<td>4129.8</td>
<td>6329.7</td>
<td>4218.5</td>
<td>4133.6</td>
<td>2110.1</td>
<td>3164.1</td>
<td>4218.8</td>
</tr>
</tbody>
</table>

* The parameters listed in bold are the results of the Le Bail profile matching analyses of pattern 1 (X-rays) and pattern 2 (neutrons). The parameters listed in italics are calculated from the unit cells for P2₁, (columns 2–5) and R3 (columns 6 to 8). The parameters for the orthorhombic cell (O1) have been calculated from the monoclinic P2₁(M1) cell. The parameters for the orthorhombic cell (O2) and monoclinic cell (M2) have been calculated from the trigonal R3 cell.

Table 5 Refined Bi atom positions for space group C2₁/m, a = 13.7161(1), b = 15.1943(1), c = 10.2399(1) Å, β = 98.586(1)°

<table>
<thead>
<tr>
<th>Atom</th>
<th>x/a</th>
<th>y/b</th>
<th>z/c</th>
<th>B (Å²)</th>
<th>Occupancy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bi1a</td>
<td>0.163(1)</td>
<td>0.137(2)</td>
<td>0.151(2)</td>
<td>1.0</td>
<td>1.0</td>
</tr>
<tr>
<td>Bi1b</td>
<td>0.416(1)</td>
<td>0.066(2)</td>
<td>0.209(2)</td>
<td>1.0</td>
<td>1.0</td>
</tr>
<tr>
<td>Bi2a</td>
<td>0.288(2)</td>
<td>0.081(2)</td>
<td>0.475(2)</td>
<td>1.0</td>
<td>1.0</td>
</tr>
<tr>
<td>Bi2b</td>
<td>0.163(2)</td>
<td>0.078(2)</td>
<td>0.012(2)</td>
<td>1.0</td>
<td>1.0</td>
</tr>
<tr>
<td>Bi3a</td>
<td>0.321(1)</td>
<td>0.136(2)</td>
<td>0.334(2)</td>
<td>1.0</td>
<td>1.0</td>
</tr>
<tr>
<td>Bi3b</td>
<td>0.061(1)</td>
<td>0.055(2)</td>
<td>0.261(2)</td>
<td>1.0</td>
<td>1.0</td>
</tr>
</tbody>
</table>

water molecule. The composition could then be described by the formula: [Bi6O5(OH)₃]⁺[Bi6O4(OH)₄]²⁺[NO3]³⁻, with x = 0.0, and the ratio between the two complex ions would be 1:1, in agreement with chemical Bi and NO₃⁻ analyses, or in other words, the chemical composition of batch-X samples is the same as the chemical composition of the material investigated by Henry et al. in 2003.

However, as mentioned in section 1, the X-ray diffraction pattern calculated from the published structure of Henry et al. in 2006 is almost identical with the present powder pattern 1 (Fig. 1). Therefore, it must be assumed that the chemical composition for the R3 space group determined by Henry et al. in 2006 is the same as that found in their former investigation. Because the four different Bi-complexes of that structure overlap, this further implies that the R3 is a disordered structure with composition [Bi6O5(OH)₃][Bi6O4(OH)₄][NO3]³⁻, where the ratio between the two Bi-complexes need not be 1:1. In section 4.3, the present neutron powder diffraction data of batch-X material (pattern 2, Fig. 2 and 6) is analysed in terms of this assumption.

4. Refinement of the batch-X diffraction data

4.1. Space group and model refinements of possible crystal structures of powder pattern 1

When using FullProf in a Le Bail type profile match calculation, pattern 1 can be matched with four different unit cells as listed below (Case-A, -B, -C and D). Within the accuracy of the data, the zero offset for pattern 1 was found to be small and therefore was kept fixed at zero during refinement. The half width parameters U, V, W and Y were determined by profile refinement using only the R3 space group (Case-A) and fixed to these values when refining the pattern in the other space groups (Case-B, -C and -D). This procedure was adopted in order to limit the number of matched profiles to a realistic number. The resulting half width parameters are quoted in the caption to Fig. 1 and were used in the subsequent structure refinements of pattern 1 using the ordered and disordered Bi₆-ion octahedra. All profile matching and model refinement calculations were made using FullProf and the Le Baille method.
structure refinements mentioned in the following were continued until convergence was reached.

**Case-A.** A trigonal space group $R\bar{3}$ with hexagonal setting, $a = 15.18650(6)$, $c = 15.8416(1)$ Å, $V = 3164.1$ Å$^3$ with $R_{\text{max}} = 0.12\%$, $R_F = 0.25\%$ and $\chi^2 = 2.9$ (Fig. 1). This cell corresponds to lattice parameters of the published structure of $[\text{Bi}_6\text{O}_4\text{(OH)}_2]\text{(NO}_3\text{)}_6$ (see Table 1). Using pattern 1 and $R\bar{3}$ in conjunction with the *ab initio* structure solving program FOX16 confirms that the structure of sample-X has indeed a disordered arrangement of the two types of complex Bi-ions, $[\text{Bi}_6\text{O}_4\text{(OH)}_2]^{3+}$ and $[\text{Bi}_6\text{O}_4\text{(OH)}_2]^{4+}$. The structure model26 has four Bi-ion sites each with approximate occupancy $\frac{1}{2}$. Thus, in hexagonal setting, its trigonal $R\bar{3}$ unit cell has a total of 18 Bi-ion sites (18') of the average composition or rather a mixture of 18 ions $[\text{Bi}_6\text{O}_4\text{(OH)}_2]^{3+}$ and $[\text{Bi}_6\text{O}_4\text{(OH)}_2]^{4+}$. This is in reasonable agreement with the average composition $[\text{Bi}_6\text{O}_4\text{(OH)}_2]^{3+}$ of a batch-X sample found in the chemical analysis.* A model calculation using pattern 1 and scattering contribution from only the four Bi-atoms on the 18$'$ sites resulted in $R_{\text{max}} = 26.5\%$, $R_F = 18.3\%$ and $\chi^2 = 9.5$.

**Case-B1.** A monoclinic space group $P2_1_1$, $a = 15.8404(1)$, $b = 15.1982(1)$, $c = 18.3122(1)$ Å, $\beta = 106.829(1)^\circ$, $V = 4219.8$ Å$^3$ with $R_{\text{max}} = 0.33\%$, $R_F = 0.35\%$ and $\chi^2 = 1.5$. This unit cell does indeed match the cell of the published structure of $[\text{Bi}_6\text{O}_4\text{(OH)}_2]^{3+}$ of a batch-X sample found in the chemical analysis.* A model calculation using pattern 1 and scattering contribution from only the four Bi-atoms resulted in $R_{\text{max}} = 26.5\%$, $R_F = 18.3\%$ and $\chi^2 = 9.5$. It corresponds to the $P2_1_1$ cell projected as in the parallelogram ABCD in Fig. 4. Using the program FullProf14 and pattern 1 in a structure refinement with the refined $P2_1_1$ unit cell and the published structure model9 with scattering contributions from only the 24 Bi atoms resulted in a very bad fit with $R_{\text{max}} = 65.4\%$, $R_F = 52.7\%$ and $\chi^2 = 21.1$. This is a surprisingly poor fit because the Bi-atoms give the major contribution to the X-ray scattering and the missing scattering contributions from the O- and N-atoms cannot account for the discrepancy.

**Case-B2.** Close inspection of the packing of the $\text{Bi}_6$ octahedra in the $P2_1_1$ structure of $[\text{Bi}_6\text{O}_4\text{(OH)}_2]^{3+}$ (called M1 below) suggests a disordered modification of this model. Fig. 4 reveals that the $\text{Bi}_6$ octahedra have centres lying close to planes parallel to the ac-planes at $y = 1/4$ and $y = 3/4$. In addition, the figure also shows that the $\text{Bi}_6$-octahedra with $z$-coordinates between 0 and $\frac{1}{4}$ have almost the same relative positions to each other as the $\text{Bi}_6$-octahedra with $z$ coordinates between $\frac{1}{2}$ and 1. If an additional set of 24 Bi atoms is introduced in the present model calculation with the coordinates $x, y, z + \frac{1}{2}$ derived from the $x, y, z$ coordinates of the first 24 Bi atoms, this corresponds to a disordered arrangement of the $\text{Bi}_6$ octahedra of the model. This model calculation resulted in a significant improvement of the fit with $R_{\text{max}} = 32.7\%$, $R_F = 30.5\%$ and $\chi^2 = 8.2$, indicating that the data of pattern 1 may be modelled better in this $P2_1_1$ monoclinic unit cell with a disordered arrangement of two sets of 24 Bi octahedra where the atoms in each set has occupancy $\frac{1}{2}$ than with an ordered arrangement of $\text{Bi}$ octahedra.

**Case-C.** A monoclinic space group $P2_1$, $a = 13.7154(2)$, $b = 15.1928(1)$, $c = 20.4696(5)$ Å, $\beta = 98.502(1)^\circ$ and $V = 4218.50$ Å$^3$ with $R_{\text{max}} = 0.21\%$, $R_F = 0.31\%$ and $\chi^2 = 1.6$. This cell was derived from the DICVOL0413 solution of pattern 1 by doubling the a- and c-axes. It corresponds to the $P2_1$ cell projected as the parallelogram AEFBC in Fig. 4b and resembles the cell found in the single crystal measurements (pattern 5) if the c-axis of that cell is doubled (see Table 3). The two cells determined for Case-B and Case-C are related and have the same volume. Hence, the packing of the $\text{Bi}_6$-octahedra in the AEFBC $P2_1$ cell can easily be derived from the packing of the $\text{Bi}_6$-octahedra in the ABCD $P2_1_1$ structure.* Refinements of the positions of the transformed atoms (Case-B2) in the $\text{Bi}_6$-octahedra of the Case-C cell give $R_{\text{max}} = 26.6\%$, $R_F = 25.9\%$ and $\chi^2 = 7.9$. A similar calculation made using pattern 3 (Fig. 3b) showed that in both cases the best model could be obtained if the $\text{Bi}_6$-octahedra were patched into each other as in Case-B2.

**Case-D.** A monoclinic space group $C2/m$ gives $a = 13.7161(1)$, $b = 15.1943(1)$, $c = 10.2399(1)$ Å, $\beta = 98.586(1)^\circ$ and $V = 2110.1$ Å$^3$ with $R_{\text{max}} = 0.13\%$, $R_F = 0.19\%$ and $\chi^2 = 2.6$ with pattern 1 and the Le Baille type profile match fitting. The single crystal measurements made on the NSLS diffractometer at beam line X7B gave a $C2/m$ unit cell with $a = 13.716(3)$, $b = 15.176(3)$, $c = 10.225(3)$ Å, $\beta = 98.60(3)^\circ$ and $V = 2104.4$ Å$^3$. A structure solution using the direct method pack SHELXTL7 gave $\text{Bi}_6$-octahedra patched into each other. The mirror plane of the $C2/m$ space group generates a solution with octahedra centres at $y = 0$ and $y = \frac{1}{2}$. This obviously corresponds to a too high symmetry, and the model does not account for the two different types of ions in the structure, $[\text{Bi}_6\text{O}_4\text{(OH)}_2]^{3+}$ and $[\text{Bi}_6\text{O}_5\text{(OH)}_3]^{5+}$. The model has eight octahedra and six Bi site positions corresponding to 48 Bi-atoms or equivalently, four $(\text{Bi}_6)_6$(\text{Bi}_3)_3 clusters in the unit cell. The positions of the clusters in the unit cell correspond to the positions of the Bi-atoms in the ac- cell projection GHJ1 with the axes $a_{\text{GHJ1}}$ and $c_{\text{GHJ1}}$ as displayed in Fig. 4b. With scattering contributions from only the six Bi-atoms in a refinement using FullProf14 and pattern 1 this model results in $R_{\text{max}} = 23.7\%$, $R_F = 21.1\%$ and $\chi^2 = 7.2$. The Bi-coordinates of this refinement are listed in Table 5.

In summary, the reliability factors $R_F$ found for the FullProf refinements of the X-ray diffraction data in pattern 1 when considering the arrangements of disordered $\text{Bi}_6$-octahedra in four different space groups are: 18.3%, 52.7%, 30.5%, 25.9% and 21.1% for Case-A, -B1, -B2, -C and -D, respectively.

### 4.2. Relationship between the structure models described in the $P2_1$ and $R\bar{3}$ space groups

In section 3.2.2. it was concluded that the model structures found by Henry *et al.*11,10 had to be related, although originally described in two different space groups. Before testing the validity of this conclusion on the present batch-X material the geometrical arrangement of the Bi-atoms in the two models are examined in detail and compared to the unit cell parameters listed in Tables 1-4.

Fig. 4 displays a projection along the 010 direction of the Bi atoms in the monoclinic $P2_1$ model structure (called M1 below). It illustrates how the different Bi-atoms of the eight complex Bi-ions are placed. The atoms within the black parallelogram ABCD shows the original unit cell projection with volume $V = 4133.7$ Å$^3$ ($a_{\text{M1}} = 15.850(3)$, $b_{\text{M1}} = 14.986(3)$, $c_{\text{M1}} = 18.230(4)$ Å, $\beta_{\text{M1}} = 107.329(17)^\circ$). The projections on the ac-plane of three other parallelepipeds, which represent possible unit cells for $[\text{Bi}_6\text{O}_4\text{(OH)}_2]^{3+}$, are also indicated. They are the grey rectangle KLMN in Fig. 4a (orthorhombic O1) and in Fig. 4b, the light blue parallelogram AEFC (monoclinic $P2_1$) and the brown.
parallelogram GHJ (monoclinic C2/m). The volumes of these
cells are either the same (AECF) or half (GIHJ) that of the original
monoclinic cell. The lattice parameters and volumes calculated
from the original cellа are listed in italics in columns 2 to 5 in
Table 4 and can be compared to the corresponding values in bold
calculated from the data in Table 3. An obvious analogy to the
unit cells listed in Table 3 is easily recognized.

The test refinement made in section 3.3.1. with pattern 1 and the
R3 unit cell using only scattering contributions from the Bi atoms
gave Rф = 18.3%, which is comparable to the above mentioned result
(21.1%) obtained for the C2/m (case-D) monoclinic cellа.
The volume of the R3 cell is 3164.1 Å³, or about 50% larger than
the volume of the monoclinic C2/m cell (V = 2110.1 Å³). The
volumes of the cells used in Case-B1 (-B2) and -C are 4219.8 Å³
and 4218.5.0 Å³, which is at least 100% larger than the volumes of
the other monoclinic cells listed in Table 3.

Fig. 5 displays a simplification of the R3 model structureа (a, c = αx, c') with only one pair of Bi6-octahedra (Bi1a and Bi1b
atom sites). Fig. 5a and 5b show the projections along the 110- and 001-directions (OPQR in yellow), respectively. Two other unit
cells are also displayed. The first is an orthorhombic cell (O2).
marked STUV in 5a and STÆØ in 5b. It is chosen with
a0 = αx, b0 = 2αx cos(30°) and c0 = c' and has a cell volume of
6263.7 Å³.а The other is a P21 monoclinic cell (M2) with
a volume two thirds that of the orthorhombic O2. It is shown as
the parallelepiped XYZW (light green) in Fig. 5a. The unit cell
parameters and volumes for the case-A trigonal structure (Table
3) and the derived O2 and M2 structures are listed in columns
6 to 8 of Table 4. For comparison, the corresponding cell values
calculated from the model structureа are listed in italics in the
same columns. The analogies to the unit cells listed in Table 3
and the unit cells calculated for the monoclinic unit cell of Ref. 9
(columns 2 to 5) are easily recognized.

Hence, the packing of Bi-atoms displayed in Fig. 4 and Fig.
5 shows a great similarity with respect to the packing of the
Bi6 octahedra and from a purely packing point of view it may
be argued that the two structures, the monoclinic P21 and
the trigonal R3 structures, are related. However, the Bi6 octahedra
in the two structure models have different symmetries defined by
the symmetry of the two space groups. The P21 structure has twenty-
four different Bi atom site positions. Twelve of these Bi atoms
form two of the complex ions [Bi6O5(OH)3]5+, and the remaining
twelve Bi atoms form two of the complex ions [Bi6O5(OH)3]5+
This is illustrated by the red, green, blue and violet octahedra in
Fig. 4a. It is important to note that there are neither symmetry
relations between the Bi-atom positions within a given octahedron
or within the four independent octahedra. The P21 structure has
an ordered packing of these two types of complex ions illustrated
by the hydrogen bonds between the complexesа.

The trigonal R3 structureа has two different Bi atom site
positions Bi1a and Bi1b and each Bi6 octahedron is formed by
three symmetry related Bi atoms of type Bi1a and three
symmetry related Bi atoms of type Bi1b, forming the complex
ion [Bi6O5(OH)3]5+, or the complex ion [Bi6O5(OH)3]5+, illustrated
by the red and green Bi atoms in Fig. 5. Stacking faults can be
introduced in this structure via two additional Bi atom site
positions Bi2a and Bi2b, forming the same type of complex ions
[Bi6O5(OH)3]5+ and [Bi6O5(OH)3]5+, and this is the only way the
R3 structure can be realized as an acceptable structure model for
the pattern 1 X-ray data.

Introducing stacking faults in the P21 structure model in Fig. 4,
as was done in the model calculation case-B2, illustrates that the
pattern 1 data can possibly be modelled in the P21, space group.
It is thus possible that the correct unit cell and space group for
the sample batch-X would be a = 15.84042(2), b = 15.19821(1), c =
18.3122(1) Å, β = 106.829(1)°, V = 4219.8 Å³, see Table 3. Although
it was identified for the twinned crystal of Henry et al.,а this larger
unit cell was neither observed in the present indexing of pattern
1, nor in the measurements of the two sets of single crystal X-ray
data. It was only identified via systematic tests of possible space
groups using FullProf and thus clearly illustrates the problems
mentioned above in handling X-ray data for heavy atom structures.
To truly confirm the existence of this large monoclinic cell, better
single crystal data would be necessary because the available single
crystal data sets collected within the smaller unit cells 3160.2 Å³
and 2104.4 Å³ cannot be transformed to complete data sets for
the larger unit cells and corresponding space groups.

4.3. Structure model determined from powder neutron diffraction
data

As mentioned above, a detailed structure analysis using the
available X-ray and neutron powder patterns can only give average
structures. However, within the accuracy of the present data, the
large P21 monoclinic cellа has too many adjustable atomic
parameters and the smaller monoclinic cell model using the space
group C2/m (Table 5) can not distinguish between the two complex
Bi6-ions because of the higher space group symmetry. Therefore,
structure analysis was made in the space group R3 using only
the neutron powder diffraction pattern, which gives more accurate
between the two complex Bi₆⁻ ions.

Based on the published structure are shown in Fig. 6. The start model used in the calculations was refined with occupancies could be obtained. The difference pattern for this converged and a preliminary set of positional parameters and refinements the following distance constraints were applied: Bi–...O...1.25 Å. The lattice parameters, zero offset and profile parameters were those obtained in the Le Bail profile fitting and quoted in the caption of Fig. 2. The background was initially described by 50 points determined by FullProf and manually adjusted as the refinement progressed. The final background is shown as the grey curves in Fig. 6a and d. The positional parameters and occupancies were first refined for the two complex Bi ions, followed by positional parameters and occupancies for the nitrate ions. Attempts to include the refinement of isotropic temperature factors for the different atoms failed (no convergence, unrealistically large or negative B-factors). However, when using two different fixed isotropic B-factors, B₃₆ = 1.0 Å² and B₅₈ = 2.0 Å², the refinement converged and a preliminary set of positional parameters and occupancies could be obtained. The difference pattern for this refinement with $R_{\text{Bragg}} = 44.4\%$, $R_p = 37.9\%$ and $\chi^2 = 6.8$ is shown in Fig. 6c. Obviously this is not a good fit and the difference plot indicates clearly that the calculated intensity is underestimated at low angles and over estimated at high angles. In order to improve the model, the B-overall parameter ($BOV$) in FullProf was allowed to vary and the refinement quickly converged for $BOV = 2.5$ with insignificant changes of the positional parameters and occupancies. A similar refinement of the X-ray data (pattern 1) using the same atom coordinates and occupancies, and allowing the scale factor and $BOV$ to vary, resulted in $R_{\text{Bragg}} = 31\%$, $R_p = 24\%$ and $\chi^2 = 9.1$ for $BOV = 2.4(1)\AA^2$.

The $BOV$ was introduced as an additional parameter, which may hide the principal uncertainties in the assumed structural model as listed below:

(a) The disordered packing of the two Bi-complexes, which have almost the same composition.

(b) The disorder of the hydrogen atoms, because it was only possible to locate the H-atoms at half of the O-atoms. The remaining H-atom positions were found by packing considerations, and the positions were fixed by constraining the distances.

(c) The use of the $R\bar{3}$ space group, while the space group of the structure is possibly monoclinic as discussed in section 4.2. Therefore, this model is an average model, and many of the parameters are strongly correlated, but the suggested model is the best achievable one with data available.

A final refinement was made with fixed $BOV = 0$ and adjustable $B_{\text{Bi}}$ and $B_{\text{other}}$, which resulted in $B_{\text{Bi}} = 3.6(1)\AA^2$ and $B_{\text{other}} = 4.4(1)\AA^2$, which agrees well with the results for $B_{\text{Bi}} + BOV$ found for the refinement above. The results of this final refinement with $R_{\text{Bragg}} = 16.9\%$, $R_p = 15.4\%$ and $\chi^2 = 2.5$ is shown as the black calculated curve in Fig. 6a and the corresponding difference pattern in Fig. 6b. The atomic coordinates and occupancies are listed in Table 6 and the chemical composition of the sample derived from these results was found to be $[\text{Bi}_2\text{O}_3(\text{OH})_4]_{1.16(1)}[\text{Bi}_2\text{O}_3(\text{OH})_2]_{0.46(1)}(\text{NO}_3)_5(\text{H}_2\text{O})_{13(1)}$. The inter-atomic distances in the two complex ions are listed in Table 7.

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**Fig. 6** Neutron powder diffraction pattern of a batch-X sample recorded at 25 °C. (a) The results of the final refinement ((○) observed and (---) calculated). Details about the refinement procedure are given in section 4.3. and the refined parameters are listed in Table 6. (b) The difference pattern (red curve) between the observed and calculated patterns in (a) using refined isotropic temperature factors $B_{\text{Bi}} = 3.6$ and $B_{\text{other}} = 4.4$ and $BOV = 0$. (c) The difference pattern (magenta curve) obtained when using fixed isotropic temperature factors $B_{\text{Bi}} = 1$ and $B_{\text{other}} = 2$ and $BOV = 0$. The fat grey curve in (a) and (d) shows the background.
The interatomic distances \((R_3, a = b = 15.1865(1) \text{ Å}, c = 15.8416(1) \text{ Å})\). The complex molecules are formed by the atoms Bi1a, Bi1b, O11, O12, O2, O1 and Bi2a, Bi2b, O21, O22, O2, O1, respectively.

<table>
<thead>
<tr>
<th>Atoms</th>
<th>Distance/Å</th>
<th>Atoms</th>
<th>Distance/Å</th>
</tr>
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<tr>
<td>Bi1a–O11</td>
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<td>N3–O31</td>
<td>1.24(2)</td>
</tr>
<tr>
<td>Bi1a–O12</td>
<td>2.40(1)</td>
<td>N3–O32</td>
<td>1.25(2)</td>
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<tr>
<td>Bi1a–O2</td>
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<td>N3–O33</td>
<td>1.21(2)</td>
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<tr>
<td>Bi1b–O11</td>
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<td>N4–O41</td>
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<tr>
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<td>N4–O42</td>
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<td></td>
<td></td>
<td>O22–H22</td>
<td>1.01(2)</td>
</tr>
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</table>

Fig. 7 shows a drawing of the two complex Bi-ions using the coordinates listed in Table 6. In the model calculation it was not possible to distinguish between O-atoms and OH-groups on the surfaces of the two complex Bi-octahedra. The atoms Bi1a, Bi1b, O11, and O12, plus O1 and O2 form one of the complex Bi molecules. The atoms Bi2a, Bi2b, O21, and O22, plus O1 and O2 form the other complex Bi molecule. The first of these ions has average Bi–Bi distances of 3.66 Å, and must correspond to the ion with the largest number of OH-groups, which is \([\text{Bi}_6\text{O}_4(\text{OH})_4]^{6+}\). The other of these complex ions has average Bi–Bi distances of 3.50 Å, and must correspond to the ion with the largest number of O-groups, which is \([\text{Bi}_6\text{O}_5(\text{OH})_3]^{5+}\).

5. Summary and conclusion

The structure found in the present work is described in the space group \(R_3\) is build of a disordered packing of the two complex ions \([\text{Bi}_6\text{O}_4(\text{OH})_4]^{6+}\) and \([\text{Bi}_6\text{O}_5(\text{OH})_3]^{5+}\). In a 1:1 ratio of the ions the formula would be \([\text{Bi}_6\text{O}_4(\text{OH})_4]^{6+} [\text{Bi}_6\text{O}_5(\text{OH})_3]^{5+}(\text{NO}_3)^{5.5-}\). Disorder in the structure was also observed in diffuse X-ray scattering reported previously.\(^a\) The structure investigation of \([\text{Bi}_6\text{O}_4(\text{OH})_4]^{6+}\) \((\text{NO}_3)^{5.5-}\) assumed a 1:1 ratio of the two complex Bi ions, so a correct formula assignment for that sample\(^a\) should rather have been \([\text{Bi}_6\text{O}_4(\text{OH})_4]^{6+} [\text{Bi}_6\text{O}_5(\text{OH})_3]^{5+}(\text{NO}_3)^{5.5-}\) or \([\text{Bi}_6\text{O}_4(\text{OH})_4]^{6+} [\text{Bi}_6\text{O}_5(\text{OH})_3]^{5+} [\text{NO}_3]^{5.5-}\), where the former indicates the existence of the two forms of ions while the latter just gives the average.

The present investigation suggests a ratio slightly different from the 1:1 ratio, and the composition of the sample investigated was thus \([\text{Bi}_6\text{O}_4(\text{OH})_4]^{6+} [\text{Bi}_6\text{O}_5(\text{OH})_3]^{5+}(\text{NO}_3)^{5.4(1)}\). The deviation from the 1:1 ratio is possible as the two complex ions are an acid base pair where the equilibrium between the ions is pH dependent. Experimental conditions can be selected to produce either purely \([\text{Bi}_6\text{O}_4(\text{OH})_4]^{6+}\) or purely \([\text{Bi}_6\text{O}_5(\text{OH})_3]^{5+}\) containing basic Bi-nitrates, see Table 1, or both the ions are present as in this investigation.

It is not often that a structure contains two complex ions with almost the same composition, but with different ionic charges. In the present compound the two complex ions have almost the same composition, different charges and almost the same three dimensional shapes of the ions, which may explain the disordered packing of the ions in the fast growth mode.

References