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Crovetto, Andrea

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Estimating complete band diagrams of non-ideal heterointerfaces by combining ellipsometry and photoemission spectroscopy

Andrea Crovetto$^{1,2,a}$

1) DTU Nanotech, Technical University of Denmark, DK-2800 Kgs. Lyngby, Denmark
2) SurfCat, Department of Physics, Technical University of Denmark, DK-2800 Kgs. Lyngby, Denmark

In this work, we show that spectroscopic ellipsometry can be combined with photoemission spectroscopy to obtain complete interface band diagrams of non-ideal semiconductor heterointerfaces, such as interfaces between thin-film polycrystalline materials. The non-destructive ellipsometry measurement probes the near-interface band gap of the two semiconductors (including the buried semiconductor) after the interface has formed. This is important in the non-ideal case where chemical processes during interface growth modify the electronic properties of the two separated surfaces. Knowledge of near-interface band gaps improves accuracy in conduction band offset measurements of non-ideal interfaces, and it sheds light on their device physics. Both of those positive outcomes are demonstrated in the Cu$_2$ZnSnS$_4$/CdS interface used here as a case study, where the band gap of both materials decreases by up to 200 meV from the bulk to the near-interface region. This finding reveals a preferential electron-hole recombination channel near the interface, and it yields corrected values for the interfacial conduction band offset.

I. INTRODUCTION

Conduction band offset measurements of semiconductor heterointerfaces are typically based on a set of direct photoemission spectroscopy measurements. Those measurements are sensitive to the energy position of the valence band maximum at the semiconductor surface, that is, within a depth of 1-20 nm depending on the excitation wavelength (UV light or x-rays). To access the conduction band positions, two possibilities exist. The first is simply to measure the bulk band gap of each semiconductor by an optical technique, such as UV-visible transmission/reflection spectroscopy. The second is to perform two complementary inverse photoemission spectroscopy measurements (IPES), which yield the energy position of the conduction band minima of the two semiconductor surfaces with an analysis depth of a few nm. In the first case, the bulk (surface) band gaps of the two semiconductors are added to the valence band offset to determine the conduction band offset.

However, formation of a polycrystalline semiconductor heterointerface often results in considerable interdiffusion of chemical species across the interface. Various authors have reported significant interdiffusion at interfaces of interest for thin-film heterojunction solar cells, such as CdTe/CdS, Cu(In,Ga)Se$_2$/CdS, Cu$_2$ZnSn(S,Se)$_4$/CdS, and Cu$_2$O/ZnO. Interdiffusion may be enhanced by heating the interface during or after growth, by energetic particle bombardment during growth, by the presence of grain boundaries as a preferential diffusion channel, and by the presence of voids and extended defects in the polycrystalline films. Due to the diffusion and lattice incorporation of elements from the foreign semiconductor, the band structure of each semiconductor in the near-interface region may be significantly different from the respective bulk and near-surface band structure.

In this paper, we apply spectroscopic ellipsometry to non-destructively measure the near-interface band gaps of two heterojunction semiconductors after interface formation, including the near-interface band gap of the buried semiconductor. Conduction band offsets can then be derived by adding the measured interface band gaps to the valence band offset determined with a standard photoemission-based method. Besides improving the accuracy of a conduction band offset measurement, knowledge of the interface band gaps of a semiconductor heterojunction can help understand its device physics. In fact, both band gap widening and band gap narrowing at the interface can have major consequences at the device level.

II. SAMPLE PREPARATION

Cu$_2$ZnSnS$_4$/CdS (CZTS/CdS) interfaces processed at different temperatures were employed as a case study for the proposed experimental method. The reason for choosing this particular interface is the ease of Cd diffusion from CdS to CZTS, as reported by many authors. The resulting Cu$_2$(Zn,Cd)SnS$_4$ solid solution present in the region of interdiffusion is expected to have a lower band gap than pure CZTS, so the CZTS/CdS interface is an ideal system to test the proposed experimental method for detecting near-interface band gap changes. CZTS thin films (about 100 nm) were deposited on a soda lime glass substrate by pulsed laser deposition from a single target with CZTS stoichiometry. Careful control of the laser fluence enabled deposition of nearly amorphous CZTS precursors with the desired stoichiometry.

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$^a$Electronic mail: ancro@fysik.dtu.dk
were further sulfurized at 550°C for 10 min. Process details and film characterization are available elsewhere. Three Cds thin films (20–40 nm) were then grown on nominally identical glass/CZTS substrates by chemical bath deposition at 55°C, 75°C, and 95°C. Chemical bath deposition is the standard technique used in the highest efficiency CZTS solar cells. After Cds deposition, each of the three samples was cut in two halves, and one half of each sample was post-annealed for 20 minutes at 300°C in an Ar atmosphere. A total of six samples was therefore available for the present study. As will be shown in the next section, simultaneous treatment of the data measured on several, slightly different samples (multi-sample analysis) can considerably improve the reliability of ellipsometry results.

III. MEASUREMENT OF NEAR-INTERFACE BAND GAPS

A. Theory

In an ellipsometry measurement in reflection mode with incidence angle \( \theta \), the polarization state of the incident beam can be described by the amplitude and phase of the two polarization components \( s \) (perpendicular to the plane of incidence) and \( p \) (contained in the plane of incidence). One can then define \( r_s(E) \) and \( r_p(E) \) as the complex reflection coefficients of the sample as a function of photon energy for the \( s \) and \( p \) polarization components respectively. By measuring the polarization state of the reflected beam and comparing it to the known polarization state of the incident beam, the ellipsometer determines the complex ratio \( r_p(E)/r_s(E) \) of the two reflection coefficients. That ratio is typically expressed by the two real numbers \( \Psi(E) \) and \( \Delta(E) \), where

\[
\frac{r_p(E)}{r_s(E)} = \tan[\Psi(E)] e^{i\Delta(E)} \tag{1}
\]

For a sample consisting of a number of stacked flat layers, each with a known thickness \( d \) and dielectric function \( \varepsilon(E) \), the overall reflection coefficients \( r_p(E) \) and \( r_s(E) \) at a given incidence angle \( \theta \) can be determined by theory using the Fresnel equations to obtain the reflection coefficient of each interface and a correction factor to account for interference effects due to the finite thickness of each layer (Fig. 1(a)). Therefore, \( \Psi(E) \) and \( \Delta(E) \) spectra can be completely determined by theory as a function of the thicknesses and dielectric functions of all layers. If the problem is inverted, that is, if some of the thicknesses and dielectric functions involved are unknown, they can in principle be determined by regression analysis through least-squares fitting of the measured \( \Psi(E) \) and \( \Delta(E) \) spectra using the unknown quantities as fitting parameters. This is the principle of spectroscopic ellipsometry.

The goal of this work is to determine the band gaps of CZTS and Cds near the CZTS/Cds interface, where they are potentially modified by chemical processes with respect to the bulk. Based on the discussion above, this can be done by spectroscopic ellipsometry with the following procedure. (i) Acquiring \( \Psi(E) \) and \( \Delta(E) \) spectra from a glass/CZTS/Cds sample; (ii) modeling the CZTS and Cds layers as several sub-layers, each of which has an independent dielectric function (thus an independent band gap, Fig. 1(a)); (iii) parameterizing the dielectric function of each layer with a number of fitting parameters which, together with the unknown layer thicknesses, are used to fit the measured \( \Psi(E) \) and \( \Delta(E) \) spectra (Fig. 2); (iv) extracting the band gap value of each layer based on the shape of the fitted imaginary part of the dielectric function near the absorption onset (Fig. 3(a)).

B. Experimental details and analysis method

\( \Psi(E) \) and \( \Delta(E) \) spectra were acquired in reflection mode with a rotating compensator ellipsometer (M-2000, J.A. Woollam Co.). The spot size was about 200 \( \mu \)m \( \times \) 300 \( \mu \)m and the photon energy range was \( 0.78 \text{ eV} \leq E \leq 3.50 \text{ eV} \). The measurement was repeated at six different incidence angles \( \theta \) for each sample (\( 45^\circ \leq \theta \leq 70^\circ \)) to provide a large dataset for more robust fitting. The CompleteEase software package (version 5.06 - J.A. Woollam Co.) was used for fitting work.

The layer model employed in this study is shown in
The dielectric function of the bottom layer into five separate sub-layers of equal thickness (Fig. 1(a)). To model the depth-dependent dielectric function, we slice the CZTS layer into several sub-layers with varying dielectric function due to interdiffusion. To model a depth-dependent dielectric function parameterized with a Kramers-Kronig-consistent b-spline function with three nodes/eV, corresponding to 10 fitting parameters, and the largest possible number of independent parameters, and the largest possible number of independent spectra should be fitted simultaneously against a consistent model. For this reason, the 36 $\Psi(E)$ spectra and the 36 $\Delta(E)$ spectra measured in this work (6 samples times 6 angles of incidence) were all fitted simultaneously, as detailed later in the article as well as in the Supplementary Material.

The CZTS layer ("A") has unknown thickness $d_A$ (fitting parameter) and unknown, possibly depth-dependent dielectric function due to interdiffusion. To model a depth-dependent dielectric function at the smallest possible expense of fitting parameters, we slice the CZTS layer into five separate sub-layers of equal thickness (Fig. 1(a)). The dielectric function of the bottom layer $\varepsilon_{A1}(E)$ is parameterized with a Kramers-Kronig-consistent b-spline function with three nodes/eV, corresponding to 10 fitting parameters in the measured range 0.78 eV $\leq E \leq 3.50$ eV, similarly to previous ellipsometry work on CZTS. The possible band gap change from the bottom layer (bulk CZTS) to the top layer (near-interface CZTS) is modeled by allowing the b-spline node located at 1.68 eV to vary linearly from the bottom layer to the top layer. All other nodes are kept constant through the layers. A linear gradient in the b-spline node, corresponding to a linear band gap gradient across the CZTS layer, is chosen under the assumption that the band gap changes in CZTS are mostly caused by Cd interdiffusion and that the Cd content in CZTS decreases steadily with increasing distance from the CdS interface, with a decay length comparable with the CZTS film thickness. Such assumptions are compatible with the existing knowledge of interdiffusion processes at the CZTS/CdS interface, which is summarized in a review paper. Note that, independently of the number of sub-layers used to model band gap grading in CZTS, the b-spline node at 1.68 eV in the dielectric function $\varepsilon_{A5}(E)$ of the top CZTS layer is the only additional fitting parameter with respect to the case of a depth-independent dielectric function. As the Cd content in CZTS is expected to decay smoothly (instead of abruptly) with depth, the CZTS layer should in principle be modeled with an infinite number of sub-layers. In practice, we noticed that a number of sub-layers higher than five did not improve the goodness of the fit further and did not change the best-fit parameters (see the Supplementary Material).

The dielectric function $\varepsilon_{B1}(E)$ of the CdS layer ("B") could also be depth-dependent in principle. However, slicing CdS into two sub-layers with varying dielectric function only led to marginal improvement of the mean squared error (MSE) of the fit, from 11.0 to 10.8 (Supplementary Material). With two CdS sublayers, we also observed poor reproducibility of the best-fit parameters upon variation of the initial guess, as well as an increase in the error bars of the CdS band gap by an average of 68%. This may indicate that the band gap of CdS is roughly depth-independent up to a few tens of nm away from the interface with CZTS, or that a depth-dependent dielectric function is difficult to capture for such a thin layer, due to overparameterization. CdS is thus modeled as a single layer with unknown thickness $d_B$ and unknown dielectric function $\varepsilon_{B1}(E)$. The imaginary part of $\varepsilon_{B1}(E)$ is parameterized with one simplified Tauc-Lorentz oscillator and one pole in the ultraviolet, and the real part of $\varepsilon_{B1}(E)$ is derived by subsequent Kramers-Kronig integration. The parameters of a Tauc-Lorentz oscillator are the amplitude $A$, broadening $B$, and energy $E_g$ of a Lorentzian function, plus a band gap energy parameter $E_g$ and a high-frequency dielectric function parameter $\varepsilon_\infty$. Enforcing the conditions $\varepsilon_\infty = 1$ and $E_\infty = E_g$ does not have noticeable effects on the MSE of our study. This limits the number of fitted parameters for the Tauc-Lorentz oscillator to 3. The additional node in the ultraviolet has amplitude $A_{uv}$ and energy $E_{uv}$ as fitting parameters.

Surface roughness has a strong influence on the $\Psi(E)$ and $\Delta(E)$ spectra and can complicate ellipsometry analysis if it exceeds a few nm. Roughness was minimized in the sample preparation phase by intentionally grow-
ing relatively thin (100 nm) CZTS layers. In the fitting phase, the roughness layer is modeled by means of Bruggeman’s effective medium theory assuming a 50%/50% mix of air and CdS in the roughness layer.\textsuperscript{15} This requires 1 fitting parameter \(d_l\) for the thickness of the roughness layer (Fig. 1(a)). The roughness values determined by ellipsometry were double checked by measuring the root mean square roughness for each sample by atomic force microscopy (AFM), with reasonable agreement between the two techniques (see the Supplementary Material). The dielectric function of the glass substrate was determined from a separate ellipsometry measurement on bare glass and is kept fixed when fitting CZTS/CdS ellipsometry spectra. The thickness of the glass substrate does not influence the \(\Psi (E)\) and \(\Delta (E)\) spectra, because opaque tape was applied to the back side of the glass to suppress back-side reflection.\textsuperscript{20}

To further reduce the chance of overparameterizing the fitting problem, the \(\Psi (E)\) and \(\Delta (E)\) spectra from the six samples investigated in this work are all fitted simultaneously, using an approach known as multi-sample analysis.\textsuperscript{15,21} The parameters that are expected to vary significantly from sample to sample are fitted independently in each sample. Those 6 parameters are \(d_A, d_B, d_e, E_o,\) as well as the nodes of \(\varepsilon_A1(E)\) and \(\varepsilon_A5(E)\) at 1.68 eV. Conversely, the parameters that are expected to be roughly constant from sample to sample are forced to have the same best-fit value across samples. Those 13 parameters are \(A, B, A_{uv}, E_{uv},\) and the 9 remaining nodes of \(\varepsilon_A1(E)\).

C. Results

While the multi-sample analysis approach yields a somewhat higher MSE (11.0) compared to separate fitting of each sample, it also results in a dramatic decrease of the error bars of the best-fit parameters, which are defined based on 90% confidence intervals. As detailed in the Supplementary Material, the error bars of the layer thicknesses are roughly ±1%; the error bars of the \(E_o\) parameter, related to the CdS band gap, are roughly ±0.1%; the error bars of the \(\varepsilon_A1(1.68)\) node, related to the CZTS bulk band gap, are roughly ±1%; and the error bars of the \(\varepsilon_A1(1.68) - \varepsilon_A5(1.68)\) quantity, related to the CZTS near-interface band gap, are between ±1% and ±10%. The best-fit values of all fitting parameters are shown in the Supplementary Material, together with all the retrieved dielectric functions, the cross-correlation coefficients between parameters, and the residuals of the fit. Knowledge of the best-fit values of the dielectric function parameters for the two materials allows derivation of their band gaps. Band tailing in CZTS absorbers is a well-known issue, which hinders accurate determination of the band gap by standard Tauc plots.\textsuperscript{22} Band tails are clearly visible in Fig. 3(a) as the imaginary part of the CZTS dielectric function does not go to zero below the expected band gap energy. The shape of the real and imaginary part of the CZTS dielectric functions extracted in this work (shown in the Supplementary Material) and the intensity of their band tails are in quantitative agreement with previous measurements.\textsuperscript{23} The very large band tails are most likely caused by a combination of sub-band gap absorption of CZTS due to potential fluctuations,\textsuperscript{24} as well as to the presence of low band gap secondary phases which are difficult to avoid in a quaternary compound with a small single-phase region.\textsuperscript{22} Since secondary phases are often located preferentially at the back of the CZTS films, they may be included in the optical model at the expense of several fitting parameters,\textsuperscript{25} and this may remove some of the CZTS band tails. We simply estimate the bulk- and near-interface band gap of CZTS (\(E_{gb,A}\) and \(E_{gb,A}\) respectively) by extrapolating the imaginary part of the corresponding dielectric function (\(\varepsilon_A1\) and \(\varepsilon_A5\) respectively) with a straight line, as shown in Fig. 3(a). For consistency, the same procedure is applied to determine the bulk band gap of CdS (\(E_{gb,B}\)) from \(\varepsilon_B\), and the near-interface band gap of CdS (\(E_{gb,B}\)) from \(\varepsilon_{B1}\). This simple approach has two advantages: (i) it yields bulk band gaps in good agreement with the CZTS band gap as determined by quantum efficiency analysis of a complete solar cell (1.56 eV versus 1.53 eV);\textsuperscript{12} (ii) it removes part of the ambiguity in the extrapolation of the dielectric function near the absorption onset, since the band tail is easily distinguished from the band gap (Fig. 3(a)). Note that the quantity \(\varepsilon_B\), and therefore the bulk band gap of CdS, is obtained from a separate ellipsometry measurement of a CdS film grown on ITO-coated glass. A shown in Figs. 4(a), 4(b), the general trend for both materials is band gap narrowing in the near-interface region.\textsuperscript{9} Especially the band gap of CZTS decreases by several hundred meV from bulk to the interface, as expected from Cd interdiffusion. This effect alone can have serious consequences at the device level.\textsuperscript{9}

To justify the validity of the optical model employed in this study, we compare it to alternative models. Detailed fitting results of the alternative models are shown in the Supplementary Material. Here, we focus on the main conclusions. A simpler model would neglect band gap grading in CZTS and treat CZTS as a homogeneous material, thus eliminating one fitting parameter (\(\varepsilon_A5(1.68)\)) per sample. The MSE of this simplified model is 12.1, compared to 11.0 for the model including band gap grading. Besides the appreciable MSE improvement, the best-fit results for the model with band gap grading are in qualitative agreement with the theoretical prediction of near-interface band gap narrowing in CZTS due to Cd interdiffusion. The additional fitting parameter results only a marginal increase (7%) of the average error bar for the parameter \(\varepsilon_A1(1.68)\), related to the bulk band gap of CZTS. An alternative way to model Cd interdiffusion could be to define a new layer between CZTS and CdS using the effective medium approximation (EMA).
for the simpler, linearly graded model. Finally, we have tested a model where the region of band gap grading only covers the top half of the CZTS layer. This would be an appropriate model if the region of interdiffusion was limited to a depth of 30-40 nm. Without changes in the total number of fitted parameters compared to our original model, the MSE of the fit is 11.3 versus 11.0 for the original model. In addition, unexpected features appear in some CZTS dielectric functions similarly to the case of exponential grading. We therefore conclude that the optical model employed in this study achieves a reasonable compromise between an oversimplified model and an overparameterized model.

IV. MEASUREMENT OF VALENCE BAND OFFSETS

To determine the conduction band offsets of the six samples using the near-interface band gaps measured by ellipsometry, valence band offsets must also be measured. An established experimental technique based on x-ray photoelectron spectroscopy (XPS) was employed, using a Thermo Scientific K-Alpha instrument with a monochromatized Al Kα x-ray source and a spot size of roughly 400 μm. The binding energy scale was calibrated with the Fermi level of an in-situ-cleaned Au sample, and confirmed by the position of the adventitious C 1s peak on as-prepared samples. The different CZTS/CdS samples were progressively etched with low-energy Ar⁺ ions and photoemission spectra of the valence band region were recorded after each etching step (Fig. 1(b)). The valence band difference method has been applied to CZTS/CdS interfaces before and it involves deconvoluting the CZTS valence band signal from the to-
The combination of ellipsometry- and XPS measurements makes it possible to determine conduction band offsets from valence band offsets using the relevant band gaps for the problem, i.e., the near-interface band gaps. As shown in Fig. 4(c), the measured conduction band offsets (CBO) across the six samples span over a 0.4 eV range, partially due to differences in their near-interface band gaps. It can be interesting to compare the CBO values determined by the present method to the values that would be obtained by more established methods. For the present method (XPS+ellipsometry):

$$\text{CBO} = \text{VBO} + E_{gi,B} - E_{gi,A}$$  \hspace{1cm} (2)

For a method based on the XPS-determined valence band offset and bulk band gaps:

$$\text{CBO} = \text{VBO} + E_{gb,B} - E_{gb,A}$$  \hspace{1cm} (3)

Even though no IPES measurements were performed in this study, we can assume based on previous work that the combination of IPES and XPS would yield a CZTS surface band gap close to $E_{gb,A}$ and a CdS surface band gap close to $E_{gi,B}$ when measuring on a thin CdS layer deposited on CZTS. Therefore, for a method based on the XPS-determined valence band offset and the IPES-determined surface band gaps, we estimate:

$$\text{CBO} = \text{VBO} + E_{gi,B} - E_{gb,A}$$  \hspace{1cm} (4)

Fig. 4(c) compares the CBOs determined by Eqs. 2-4. The underestimation of the CBO by the XPS+IPES method (Eq. 4) can be explained by the fact that the XPS+IPES method captures near-interface band gap narrowing in CdS, but not in CZTS. The less severe CBO underestimation by the XPS method with separately determined bulk band gaps (Eq. 3) can be explained by error cancellation, since band gap changes of both CZTS and CdS near the interface are in the same direction (i.e., towards band gap narrowing).

Finally, detailed interface band diagrams can be drawn based on the quantities measured in this work, as illustrated in Fig. 5(a). Taking the interface band diagram of the sample with a CdS deposition temperature of 55°C and post-annealing as an example (Fig. 5(b)), interesting features that influence the physics of the resulting device are found. The flat conduction band offset is a beneficial feature for electron transport across the interface and minimization of interface recombination. The downwards band bending from CZTS to CdS is also a beneficial feature, as it drives electrons and holes towards their respective contacts. Band gap narrowing in CZTS is, however, a detrimental feature, as it decreases the barrier to recombination in the near-interface region, thus potentially decreasing the maximum achievable solar cell open-circuit voltage. Understanding the specific chemical mechanisms responsible for band gap narrowing and their dependence on process conditions is not straightforward and will thus require a separate study. Here we simply note that near-interface band gap narrowing of CZTS and CdS is observed consistently in all samples, regardless of their different processing conditions.
VI. METHOD LIMITATIONS

Our proposed experimental method certainly has a number of limitations. First of all, any effect that modifies the band gaps of the materials only in a very shallow region of a few nm across the interface is very difficult to detect by ellipsometry, since the effect of dielectric function changes on \( \Psi(E) \) and \( \Delta(E) \) spectra for very thin layers can be indistinguishable from thickness changes.\(^{28}\) Hence, the present method is only sensitive to "near-interface" band gap changes (tens of nm), which can be related, e.g., to relatively deep interdiffusion or to phase segregation after post-annealing. This is the reason for the expression "near-interface band gap" used throughout this article. Since ellipsometry is a model-based indirect technique, the quality of the ellipsometry results strongly depends on the correctness of the layer model and on careful selection of fitting parameters, which is a trade-off between an oversimplified and an overparametrized model.\(^{15}\) Finally, the sample preparation phase is critical. Polycrystalline materials with relatively large, micron-sized grains can result in unacceptable high surface roughness, which renders ellipsometry analysis impossible.\(^{15}\) This issue can be circumvented by depositing thin layers of materials or by polishing the layers after deposition.

VII. CONCLUSION

We have proposed an extension to a standard photoemission-based method for obtaining detailed interface band diagrams of semiconductor heterojunctions where chemical processes during interface growth or post-annealing modify the interface electronic properties with respect to the bulk or to the bare surface. For the particular heterointerface selected to demonstrate the method (\( \text{Cu}_2\text{ZnSnS}_4/\text{CdS} \)), a band gap decrease of several hundred meV from bulk to interface was observed on both sides of the interface. The resulting device physics is significantly influenced by the band gap narrowing phenomenon. Adding the near-interface band gaps to the valence band offsets measured by photoemission spectroscopy significantly improves the accuracy of a standard conduction band offset measurement.

VIII. SUPPLEMENTARY MATERIAL

See the Supplementary material for more details about possible optical models used to fit ellipsometry spectra, the best-fit values of all fitting parameters, plots of the experimental versus modeled ellipsometry spectra of all the investigated samples, a table with cross-correlation coefficients between fitted parameters, plots of the retrieved dielectric functions, and comparison between the roughness values extracted by ellipsometry and by atomic force microscopy.

IX. ACKNOWLEDGEMENTS

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\(^{15}\) H. Fujiwara, Spectroscopic Ellipsometry - Principles and Applications (Wiley, 2007).