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Optimized cesium and potassium ion-exchanged zeolites A and X granules for biogas upgrading†

Kritika Narang, Kristina Fodor, Andreas Kaiser and Farid Akhtar†

Partially ion-exchanged zeolites A and X binderless granules were evaluated for CO₂ separation from CH₄. The CO₂ adsorption capacity and CO₂-over-CH₄ selectivity of binderless zeolites A and X granules were optimized by partial exchange of cations with K⁺ and Cs⁺, while retaining the mechanical strength of 1.3 MPa and 2 MPa, respectively. Single gas CO₂ and CH₄ adsorption isotherms were recorded on zeolites A and X granules and used to estimate the co-adsorption of CO₂–CH₄ using ideal adsorbed solution theory (IAST). The IAST co-adsorption analysis showed that the partially ion-exchanged binderless zeolites A and X granules had a high CO₂-over-CH₄ selectivity of 1775 and 525 respectively, at 100 kPa and 298 K. Optimally ion-exchanged zeolite X granules retained 97% of CO₂ uptake capacity, 3.8 mmol g⁻¹, after 5 breakthrough adsorption-desorption cycles while for zeolite A ion-exchanged granules the reduction in CO₂ uptake capacity was found to be 18%; CO₂ uptake capacity of 3.4 mmol g⁻¹. The mass transfer analysis of breakthrough experimental data showed that the ion-exchanged zeolite X had offered a higher mass transfer coefficient, kₓ through the adsorption column compared to zeolite A; 0.41 and 0.13 m s⁻¹ for NaK₀.₄Cs₀.₃X and CaK₂.₅Cs₀.₂A, respectively.

Introduction

The combustion of biomass produces approximately the same amount of CO₂ with respect to its decomposition cycle, which leads to biomass carbon neutrality. In this respect, biomass conversion to biogas is a viable choice of a renewable fuel.¹ Biogas is produced from a large diversity of biomass feedstocks, such as sewage, industrial waste, agricultural waste, dairy manure, landfill waste, food processing byproducts, etc., via anaerobic digestion.² Methane is the primary component of raw biogas (45–75%) in addition to carbon dioxide (typically 25–55%) and other components like hydrogen sulde, ammonia, water and trace gas compounds like oxygen and hydrocarbons.³ In order to use biogas as vehicle fuel or its induction to existing natural gas grids, upgrading of biogas to biomethane with a CH₄ mole fraction over 96% is required to meet the standards laid out by respective industries.⁴ Several technologies have been developed to upgrade raw biogas via adsorption⁵ absorption,⁶ permeation⁷ and cryogenic technologies⁸ resulting in biogas with a content of CH₄ > 90%.⁹ Moreover, adsorption-based technologies offer advantages like low upgrading costs and ease of scalability with biogas production unit over other technologies.

Various microporous adsorbents have been explored during the last two decades in the field of biogas upgrading such as activated carbon, zeolites and metal–organic frameworks (MOFs).¹⁰ Zeolites A and X have many advantageous properties like flexibility in tailoring the pore opening, high CO₂ uptake capacity, chemical and thermal stability, hence these materials have been investigated for biogas and natural gas upgrading.¹¹⁻¹³ Analogues of zeolite A with 8-ring pore openings have pore apertures with the diameters similar to the kinetic diameters of CO₂ (0.33 nm), N₂ (0.364 nm) and CH₄ (0.38 nm).¹⁴ The aperture size for zeolite A depends on the extra framework cation present in the structure, thus it varies between 0.3–0.5 nm.¹⁵ Due to these characteristics, researchers have tailored the pore size using partial ion exchange process on zeolite A for CO₂ separation from gas streams.¹⁶ Liu et al., ion exchanged Na⁺ cations with K⁺ and reported ideal CO₂-over-N₂ selectivity of 172 with 17 atomic percentage (at%) K⁺ content in zeolite A.¹⁷ Bacsik et al., investigated NaKA zeolites for CO₂-over-CH₄ separation, and suggested that |Na₁₂₋ₓKₓ|-LTA, with x ranging between 1.8 ≤ x ≤ 3.2 (x being the number of ions in pseudocell) offers high CO₂-over-CH₄ selectivity.¹⁸ Cheung et al., reported a high CO₂-over-CH₄ selectivity, of around 1500 for |Na₁₀₋ₓKC₉ₓ|⁻⁻|-LTA, which was achieved by partial ion exchanging Na⁺ to K⁺, and then replacing some of the K⁺ with Cs⁺.¹⁹ Zeolite NaX has been studied extensively for CO₂ separation from flue-gas streams due to its superior CO₂ adsorption capacity and selectivity over N₂.²⁰⁻²¹ Harlick and Tezel showed that NaX and NaY had the highest CO₂ adsorption capacities and proposed these zeolites as best candidates for CO₂ separation,²² while Walton et al.,...
showed that in all cases X zeolites possess more CO₂ molecules per supercage than the Y by examining their Li, K, Na, Rb, and Cs ion exchanged derivatives. Next to this, Cavenati et al., conducted a study of high pressure adsorption of CO₂, CH₄ and N₂ on zeolite NaX, and concluded that the adsorbent was highly selective to CO₂ thus rendering it suitable for purification purposes.

The microporous zeolites are used in structured forms in adsorption-based separation technologies using pressure and/ or temperature cycling. The mechanically stable structured microporous materials are required to minimize the pressure drop, promote high gas flow and rapid mass transfer kinetics throughout the adsorption column in a swing adsorption process. The earlier reports on the partially ion-exchanged are focused on powdered zeolite. The processing of these partially ion-exchange powders to structured forms using clay binders (typically 25–45%) can influence the adsorption properties significantly. Moreover, the addition of clay binders to zeolites to achieve desired mechanical stability reduces the durability of the structured product. The reports on structuring of partially ion-exchange zeolites are sparse despite the fact that structuring is an important aspect of practical separation of CO₂ from methane for biogas upgrading using adsorption-based technologies. In this regard, current work reports a robust method to process partially ion-exchange binderless structured granules of zeolite CaA and NaX with reasonably high mechanical stability and adsorption performance for biogas upgrading. The binderless granules of zeolite CaA and NaX were subjected to partial ion-exchange with K⁺ and Cs⁺ cations to optimize the adsorptive properties for CO₂ separation from CH₄ in a pressure swing adsorption process. The evaluation of adsorption properties such as CO₂ uptake capacity, CO₂-over-CH₄ selectivity and cyclic performance of mechanically strong partially ion-exchanged zeolites A and X granules are reported. Cyclic breakthrough measurements and calculated mass transfer coefficients of zeolite NaX and CaA granules as well as their optimal ion exchanged derivatives are reported in this study to evaluate the performance.

### Experimental

#### Materials and methods

Commercially available zeolite NaX and CaA powder and binderless granules were purchased from Luoyang Jianlong Chemical Industrial Co. Ltd., Yanshi, Henan, China, with zeolite crystal size 2–4.5 µm. Potassium chloride (optical grade 99%) and cesium chloride (optical grade ≥99.5%) were purchased from Sigma Aldrich Chemie GmBH, Germany. The partial ion exchange is a simple and a robust method. The K⁺ and Cs⁺ ion exchange process for the granules was performed in two stages. First, the CaA and NaX zeolite granules were partially ion-exchanged by K⁺ cations and then the partially K⁺ exchanged zeolite granules (CaKA and NaKX) were collected and further ion exchanged with Cs⁺ cations. The detailed experimental description of the ion exchange process on the powders of zeolite NaX and CaA and their CO₂/CH₄ selectivities are provided in the ESI (Tables 1S and 2S† respectively). The optimum combination of CO₂ uptake capacity and CO₂/CH₄ selectivity obtained from the partially K⁺ and Cs⁺ ion exchanged powders of zeolite CaA and NaX was used as a guideline to prepare partially K⁺ and Cs⁺ ion exchanged granules of CaA and NaX to obtain optimum combination of CO₂ uptake capacity and CO₂-over-CH₄ selectivity as shown in Table 1.

#### Characterization

The elemental composition of the partial ion exchanged NaX and CaA powders as well as of granules were determined by energy dispersive spectroscopy (EDS) using JEOL JCM-6000Plus scanning electron microscope (SEM). The zeolites granules were crushed into powder and were spread onto a double-sided copper tape and examined at an accelerating voltage of 15 kV.

#### Table 1  Ion exchange process description for NaX and CaA powder and granules

<table>
<thead>
<tr>
<th>Starting zeolite</th>
<th>Amount of NaX (g)</th>
<th>Amount of CsCl (g)</th>
<th>Amount of CsCl (g)</th>
<th>Amount of water (ml)</th>
<th>Stirring time (min)</th>
<th>Final zeolite composition</th>
</tr>
</thead>
<tbody>
<tr>
<td>NaX powder</td>
<td>5</td>
<td>1</td>
<td>—</td>
<td>500</td>
<td>30</td>
<td>NaK₃.5X</td>
</tr>
<tr>
<td>NaK₃.5X</td>
<td>1.2</td>
<td>—</td>
<td>0.02</td>
<td>120</td>
<td>30</td>
<td>NaK₃.25Cs0.15X</td>
</tr>
<tr>
<td>NaX granule</td>
<td>10</td>
<td>8</td>
<td>—</td>
<td>1000</td>
<td>60</td>
<td>NaK₄.5X</td>
</tr>
<tr>
<td>NaK₄.5X</td>
<td>5</td>
<td>—</td>
<td>0.20</td>
<td>500</td>
<td>60</td>
<td>NaK₄.3Cs0.3X</td>
</tr>
<tr>
<td>CaA powder</td>
<td>1</td>
<td>0.8</td>
<td>—</td>
<td>100</td>
<td>30</td>
<td>CaK₃.4A</td>
</tr>
<tr>
<td>CaK₃.4A</td>
<td>1.8</td>
<td>—</td>
<td>0.06</td>
<td>180</td>
<td>30</td>
<td>CaK₂.5Cs0.45A</td>
</tr>
<tr>
<td>CaA granule</td>
<td>5.1</td>
<td>4</td>
<td>—</td>
<td>1000</td>
<td>60</td>
<td>CaK₂.6A</td>
</tr>
<tr>
<td>CaK₂.6A</td>
<td>5.9</td>
<td>—</td>
<td>0.20</td>
<td>500</td>
<td>60</td>
<td>CaK₂.3Cs0.2A</td>
</tr>
</tbody>
</table>

a The final composition of the zeolite after ion-exchange was determined by EDS analysis.
The CO2, CH4 equilibrium adsorption isotherms were collected on a Gemini VII 2390 Surface Area Analyzer (Micromeritics, Norcross, USA). The CO2-over-CH4 selectivities of all zeolites were calculated using PANalytical’s X-ray diffraction pattern (PXRD) of NaX, CaA zeolites including its ion-exchange derivatives were analyzed using a Pressure Swing Adsorption PSA-300LC (L&C Science and Technology, Florida, USA). The CO2-over-CH4 selectivities of all zeolites were calculated using Henry’s Law constants (K_H) and ideal adsorbed solution theory. Prior to the measurements, the zeolite columns were degassed using Vac Prep 061 for 24 h at 573 K under a dynamic vacuum. All the adsorption measurements were done at 298 K within a pressure range of 1 to 90 kPa. The co-adsorption of CO2–CH4 was estimated using ideal adsorbed solution theory (IAST). Single gas adsorption data and Langmuir model were utilized to obtain the parameters needed to estimate the binary selectivity coefficients using IAST model for a mixed gas containing 50–50 mol% of CO2–CH4 at various total pressures. The equilibrium cyclic performance of the ion-exchanged zeolites was recorded on a Gemini VII 2390 Surface Area Analyzer (Micromeritics, Norcross, USA).

The mechanical strength of the granules was determined by performing a compression test between the steel plates in a 1 kN load cell on Zweck Z050 universal test machine. A pre-load of 5 N was used. The test was carried out on five identical granules of each type to obtain a statistically significant data distribution. Mercury intrusion porosimetry of the zeolite granules was performed on a Micromeritics AutoPore III-9400 (Norcross, GA, USA) over a wide range of pressures (0.03–420 MPa). The pore size distributions were obtained from the Washburn equation using 0.485 N m–1 surface tension and 130° contact angle of mercury. To investigate the biogas upgrading, cyclic breakthrough measurements on NaX, CaA granules as well as their potassium and cesium ion exchange analogues were obtained using a Pressure Swing Adsorption PSA-300LC (L&C Science and Technology, Florida, USA) system. Prior to the measurement, the zeolite granules were regenerated at 200 °C in helium gas passing through the column at a flow rate of 20 ml min–1 for 12 h. Moreover, the dew point of –15 °C was used as a benchmark to mark the drying of the zeolite column. A binary mixture of CO2/CH4 (45 mol%/55 mol%) gas was passed in the fixed bed of length 100 mm and 15 mm in diameter to study the adsorption performance of zeolites and its optimum ion exchange derivatives at 2 bar and 293 K up to 5 cycles. The flow rate was set to 19 ml min–1 and 15 ml min–1 for CO2 and CH4 gases respectively. The amount of the adsorbent in the PSA column were 4.96 g, 5.30 g, 4.28 g, 4.70 g for NaX, CaA, optimal ion exchanged NaX, optimal ion exchanged CaA zeolites, respectively. For the cyclic measurements, the zeolite column was regenerated by evacuation. A pressure of 0.01 bar was chosen to be reached in the columns for regeneration in the cyclic measurements.

Results and discussion

The zeolite granules, 1.6 mm in diameter, in Fig. 1 consist of primary zeolite particles with a size distribution of 2.5 to 4.0 microns for CaA granules and 2.5 to 4.5 microns for NaX granules. The partial ion-exchanged derivatives of zeolites CaA and NaX granules with K+ and Cs+ were prepared following the adsorptive properties and energy dispersive spectroscopy analysis of elemental composition of partial ion exchange of CaA and NaX powders with varying fraction of K+ and Cs+ cations (ESI, Table 3S†). The compositions of the optimal ion exchange zeolite A and X granules determined from energy dispersive spectroscopy (EDS) analysis were CaK2.5Cs0.2A, CaK2.5Cs0.2Na, NaK4.5Cs0.5X and NaK4.5Cs0.5X, respectively. The microstructure and X-ray diffraction data in Fig. 1 and ESI (Fig. 1S and 2S†) confirms that the optimal ion exchanged zeolite A and X crystals preserve the morphology and crystallinity after the ion exchange process.

In [Fig. 2a], the uptake capacities of CO2 of zeolite CaA and ion-exchanged CaK2.5Cs0.2A granules are 4.5 mmol g–1 and 4.3 mmol g–1, respectively. In [Fig. 2b], the uptake capacity of CO2 for zeolite NaX and NaK4.5Cs0.5X granules are 5.6 mmol g–1 and 5.1 mmol g–1, respectively. The CO2 uptake capacity of binderless granules of CaA and NaX is comparable to the structured zeolite A and X monoliths prepared without addition of binders.25,26,28 Moreover, it has been established that the binderless structured adsorbents offer advantages of high CO2 adsorption capacity and durability over traditional adsorbents structured using inorganic clay binders up to 45% to achieve the mechanical strength.27,31 After partial ion-exchange, the binderless zeolite granules show small decrease in the uptake capacities, which is attributable to the presence of extra framework cations. The charge density decreases in order of Na > K > Cs, resulting in a decrease of electrostatic interaction between the extra frameworks cations and the permanent quadruple moment of CO2 and hence the reduction in CO2 capacities is observed for the optimal ion-exchanged granules. Similar decrease in the CO2 uptake capacity was shown by the partially ion exchange CaA and NaX powders (ESI, Fig. 3S†). This result agrees with studies of Walton et al., who showed that the CO2 capacity increased with the small alkali cations in X and Y zeolites.23 Similar results have been reported in the literature on alkali exchanged faujasite zeolites.32 The CO2 uptake capacities for the ion exchanged zeolite granules are higher than the previously reported ion exchanged zeolites,33 3D-printed NaX and CaA zeolite monoliths39 while maintaining the high CO2/CH4 selectivity of the granules.

In [Fig. 2a], the CH4 adsorption capacities of zeolite CaA and optimal ion-exchanged CaK2.5Cs0.2A granules are 0.74 mmol g–1 and 0.69 mmol g–1, respectively and in (Fig. 2b), the uptake capacity of CH4 for zeolite NaX and NaK4.5Cs0.5X granules are 0.67 mmol g–1 and 0.46 mmol g–1, respectively. The reduction in CH4 uptake is connected to the hindrance to the percolation of CH4 due to enhanced diffusion barrier in ion-exchanged cages.24 The partial ion exchange of the CaA and NaX powders shows the similar reduction in CH4 adsorption capacities (ESI, Fig. 4S†). Moreover, linear isotherms were obtained in case of...
CH₄ adsorption due to the absence of a quadrupole moment in CH₄ giving rise to weak interaction primarily via dispersion-repulsion forces exist between CH₄ molecules and the adsorbent. CO₂ cyclic adsorption isotherms for the optimal ion exchange derivatives of CaA and NaX granules are reported in (Fig. 2c and d) respectively. The cyclic stability was investigated over up to 4 cycles. For the first cycle, the zeolite granules were regenerated at 300 °C under vacuum and for the further cycles, the zeolites were regenerated under vacuum at room temperature.

In (Fig. 2c and d), the reduction in the CO₂ adsorption capacity is observed after cycle 1. The reason for this reduction is attributed to chemisorption of CO₂. No further reduction is observed in the following cycles. For the CaK₂.₅Cs₀.₂A granules, 15% of the reduction in the CO₂ uptake is noticed from 1st cycle to 4th cycle, while the reduction of 7.9% is observed in the case of NaK₄.₅Cs₀.₃X granules. However, after the first cycle, the CaK₂.₅Cs₀.₂A and NaK₄.₅Cs₀.₃X granules keep the CO₂ adsorption capacity.

The textural properties and the CO₂-over-CH₄ selectivity of zeolites granules and the optimal ion exchange derivatives are shown in Table 2. The specific surface areas of granulated CaK₂.₅Cs₀.₂A and NaK₄.₅Cs₀.₃X are 351 m² g⁻¹ and 474 m² g⁻¹, respectively. The decrease in the surface area is observed with the increase of cation size (Na < K < Cs), as reported earlier. The external surface area and the micropore volume of the NaK₄.₅Cs₀.₃X granules were 33 m² g⁻¹ and 0.25 cm³ g⁻¹ and for CaK₂.₅Cs₀.₂A granules were 64.2 m² g⁻¹ and 0.16 cm³ g⁻¹ respectively. There is no significant decrease in micropore volume and external surface area for the zeolites with its corresponding optimal ion exchange derivatives. These results suggest that the ion-exchange process of zeolite granules did not result in surface contamination of the zeolite particles and the granules. The reduction in the total surface area is mainly determined by the reduction in micropore area due to size difference of the cations. Similar observations have been reported for ion exchanged zeolite powders. The calculated CO₂-over-CH₄ selectivities in Table 2, using Langmuir adsorption model and ideal adsorbed solution theory (IAST), show higher values for optimal ion-exchanged zeolites CaA and NaX with K⁺ and Cs⁺ cations (ESI, Table 4S† for Langmuir parameter and the Henry’s constant for the powders and granules). The CO₂-over-CH₄ selectivity increases with partial exchange of K⁺ cations. It is also noticed, that the CO₂-over-CH₄ selectivity increased with the addition of Cs⁺ in the structure. The role of the Cs⁺ in the structure is determined to be two-fold. First, due
to its size it is expected to reduce the pore opening of the super cage to achieve molecular sieving effect, however the significant size difference of Cs⁺ compared to Na⁺ ion will generate a stronger interaction for the bigger cation, because the molecular shielding from the surrounding oxygen atoms is less, thus the interaction with CH₄ will not be limited, as it is the case with the Na⁺.

Furthermore, it is deduced that two factors will affect the selectivity of the potassium and cesium ion-exchanged zeolite granules: (a) steric selectivity, due to the reduced pore opening and pore volume and (b) the difference in the interactions of CO₂ and CH₄ gases with the individual cations. Even though zeolite NaX contains cations at all sites, position I and I' are within the sodalite cages and these are usually not reachable for

**Table 2** Textural properties of CaA and NaX zeolites and their optimal ion exchange derivatives, including the IAST selectivities

<table>
<thead>
<tr>
<th>Granules</th>
<th>BET surface area (m² g⁻¹)</th>
<th>Micropore area (m² g⁻¹)</th>
<th>External surface area (m² g⁻¹)</th>
<th>Micropore volume (cm³ g⁻¹)</th>
<th>IAST selectivity (CO₂/CH₄)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CaA</td>
<td>436</td>
<td>370</td>
<td>66.6</td>
<td>0.21</td>
<td>542</td>
</tr>
<tr>
<td>CaK₂.6A</td>
<td>354</td>
<td>304</td>
<td>50.1</td>
<td>0.17</td>
<td>906</td>
</tr>
<tr>
<td>CaK₂.5Cs₀.2A</td>
<td>351</td>
<td>287</td>
<td>64.2</td>
<td>0.16</td>
<td>1773</td>
</tr>
<tr>
<td>NaX</td>
<td>496</td>
<td>461</td>
<td>35</td>
<td>0.26</td>
<td>329</td>
</tr>
<tr>
<td>NaK₃.9X</td>
<td>458</td>
<td>425.4</td>
<td>32.8</td>
<td>0.24</td>
<td>384</td>
</tr>
<tr>
<td>NaK₄.5Cs₀.3X</td>
<td>474</td>
<td>441.4</td>
<td>33</td>
<td>0.25</td>
<td>525</td>
</tr>
</tbody>
</table>
most adsorbate molecule (ESI, Fig. 5S†). The non-accessibility of certain sites due to the size difference of the cations leads to a significant decrease in CH$_4$ uptake of the cesium and potassium ion exchanged zeolites, generating only a slight reduction in the CO$_2$ uptake. This difference in the amount of reduction in the CH$_4$ and CO$_2$ uptake capacities give rise to high CO$_2$-over-CH$_4$ selectivity. The interaction between the cations and the CO$_2$ is higher as compared CH$_4$ due to the stronger polarizability and quadrupole moment of CO$_2$.41

The use of zeolites in industrial applications requires a strong macroscopic structure with good mechanical stability and hierarchical porosity which can provide a low pressure drop and rapid mass transfer kinetics.42 High mechanical strength is crucial for the adsorbents as they undergo large and rapid pressure and thermal variations.27,48 Table 3 shows that the mechanical strength of the optimal ion-exchanged granules is comparable to pure CaA and NaX granules. Nevertheless, a drop in the mechanical strength has been noticed for the optimal cesium ion exchanged granules. Optimal cesium exchanged granules underwent two times the ion exchange process which may result in erosion and dissolution of contact points/bridges between the zeolite crystals in the granules and reduce the mechanical strength.24 The mechanical strength of ion-exchanged binderless CaA and NaX granules (Table 3) is higher than the mechanical strength reported for conventional structured CaA and NaX zeolite monoliths.25 The retention of mechanical strength after the ion-exchange process is related to the binderless nature of the zeolite granules. It has been reported that the addition of clay binders to the zeolites results in significant reduction in the mechanical durability of the structured body on exposure to acidic and basic aqueous media.27

Fig. 3 shows the differential pore size distribution of the CaA, NaX and its optimal ion exchange derivative, measured by mercury porosimetry. The macroporosity of the zeolites is listed in Table 3. The CaA and the NaX zeolite granules show a homogeneous pore size distribution with a maximum centered at 0.4 μm. The peak corresponds to interparticle voids between the zeolites particles in the binderless granules. Such large pores are required for efficient mass transfer of gas molecules to the adsorption sites in the zeolite crystals.

Fig. 4 shows the cyclic breakthrough experiments on adsorption column of binderless CaA and NaX granules and their optimum ion exchanged derivatives to evaluate and compare the performance. In breakthrough curve, $C/C_0$ implies relative concentration of CO$_2$, where $C$ and $C_0$ represent the concentration at the outlet and the inlet of the fixed bed respectively. The first part of the breakthrough curve in which the relative concentration ($C/C_0$) is zero implies that all the CO$_2$ gas molecules are being adsorbed. The second part of the curves with a steep increase in relative concentration implies that the adsorbent is saturated, and an increasing concentration of CO$_2$ gas molecules is slipping (through the column). The zone between zero to one is described as mass transfer zone (MTZ). The fixed bed is completely saturated when $C/C_0$ is equal to one.

After the first cycle, the reduction in the breakthrough point for further cycles is due to the chemisorbed CO$_2$ molecules, as observed in cyclic experiment in (Fig. 2c and d) also, that could not be released through regeneration by evacuation. Both of the optimal ion exchange zeolite granules show stability in the adsorption capacity after three cycles. The amount of CO$_2$ adsorbed by the zeolites until the breakthrough point for pure NaX and CaA zeolites were determined to be 4.6 mmol and
3.3 mmol of CO₂ per g of the zeolite, respectively, for the final cycle. NaK₄.₅Cs₀.₃X shows the adsorption capacity of 3.8 mmol g⁻¹ in the final cycle and is higher than the CaK₂.₅Cs₀.₂A zeolite, which adsorbs 3.4 mmol of CO₂ per g of zeolite. The CO₂ uptake rate was 2.8 mg of CO₂ per g per s for NaK₄.₅Cs₀.₃X and 2.5 mg of CO₂ per g per s for CaK₂.₅Cs₀.₂A granules. The amount of CO₂ adsorbed in breakthrough experiment is less than the amount adsorbed in the equilibrium gas adsorption experiment shown in Fig. 2. The sharp front in the breakthrough curve as shown in Fig. 4 implies that the zeolite granules have low mass transfer resistance and the fluid flow distribution is even within the granules. The mass transfer coefficient which corresponds to the speed of the molecules to diffuse and amount adsorb within the adsorbent can be derived from eqn (1) which was adapted from Klinkenberg⁴⁴ and was fitted to the experimental breakthrough.

\[
\frac{C}{C_0} = \frac{1}{2} \times \text{erfc} \left( 7\sqrt{\frac{\xi}{\tau}} \right) \quad (1)
\]

where \(\xi\) is the dimensionless length given by eqn (2) and \(\tau\) is the dimensionless time given by eqn (3).

\[
\xi = \kappa K_z ((1 - \epsilon)/\nu)\tau
\]

\[
\tau = \kappa \left( t - \frac{\epsilon x}{\nu} \right)\tau
\]

\[
v = \frac{Q_v x}{S} \quad (4)
\]

In above equations, \(\kappa\) is mass transfer coefficient, \(K\) is Henry constant of the adsorbate, \(\epsilon\) is the total void fraction, \(x\) is the bed length, \(t\) is the time in minutes, \(v\) is interstitial velocity which is given by eqn (4), where \(Q_v\) is the volumetric flow rate of the gas and \(S\) is the cross-sectional surface area of the bed. The simulated mass transfer coefficient \(\kappa\) is 1.01 and 0.6 m s⁻¹ for pure NaX and CaA granules, respectively. High mass transfer indicates rapid diffusion of CO₂ molecules into the adsorbent. The mass transfer is fast in NaX due to relatively large pore size (0.74 nm) in the zeolite framework. The mass transfer coefficient was reduced to 0.41 and 0.13 m s⁻¹ for NaK₄.₅Cs₀.₃X and CaK₂.₅Cs₀.₂A granules respectively. Due to the presence of extra framework cations in the zeolite, the diffusion of CO₂ molecules is slower in the adsorbents and hence resulted in the relatively low mass transfer coefficient. The mass transfer coefficients for pure and ion-exchanged derivates are comparable to laminated NaA zeolites prepared by freeze casting.³⁸

**Conclusions**

The optimal ion exchange of CaA and NaX zeolites and their adsorption properties were studied. The optimal concentration
was determined according to the performance of the ion exchange zeolites by evaluating the CO$_2$-over-CH$_4$ selectivity using IAST theory. The CaKCSa with the 2.5 (at%) K$^+$ and 0.2 (at%) Cs$^+$ content and NaKCsX with the 4.5 (at%) K$^+$ and 0.3 (at%) Cs$^+$ content gives the CO$_2$ uptake value of 4.3 mmol g$^{-1}$ and 5.1 mmol g$^{-1}$ respectively with high CO$_2$-over-CH$_4$ selectivity as compared to pure CaA and NaX. The optimal ion exchanged CaA and NaX zeolites shows high mechanical strength of 1.3 MPa and 2 MPa respectively. The breakthrough curves suggest low mass transfer resistance for both NaX and CaA granules including its optimal ion exchanged derivatives. NaX ion exchange granules have shown better performance as compared to CaA ion exchange zeolite, by having a CO$_2$ uptake rate of 2.8 mg of CO$_2$ per g per s while achieving the stability after few cycles with a mass transfer coefficient of 0.41 m s$^{-1}$.

Conflicts of interest

There are no conflicts to declare.

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