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Dual-polarization nonlinear Fourier transform-based optical communication system

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New services and applications are causing an exponential increase in Internet traffic. In a few years, the current fiber optic communication system infrastructure will not be able to meet this demand because fiber nonlinearity dramatically limits the information transmission rate. Eigenvalue communication could potentially overcome these limitations. It relies on a mathematical technique called “nonlinear Fourier transform (NFT)” to exploit the “hidden” linearity of the nonlinear Schrödinger equation as the master model for signal propagation in an optical fiber. We present here the theoretical tools describing the NFT for the Manakov system and report on experimental transmission results for dual polarization in fiber optic eigenvalue communications. A transmission of up to 373.5 km with a bit error rate less than the hard-decision forward error correction threshold has been achieved. Our results demonstrate that dual-polarization NFT can work in practice and enable an increased spectral efficiency in NFT-based communication systems, which are currently based on single polarization channels.

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1. INTRODUCTION

Fiber optics telecommunication is the currently established backbone infrastructure for most of the information flow across the world [1]. However, the demand for an always increasing transmission rate, which for the existing channels is necessarily associated with an increment of the launched signal power to minimize the optical signal-to-noise ratio (OSNR) degradation, has been predicted to be asymptotically limited by the distortion induced by the optical fiber nonlinearity [2,3]. It is a well-known fact that light propagation in fiber optics is governed by the nonlinear Schrödinger equation (NLSE) [4] where the nonlinearity arises due to the Kerr effect. Nonlinearity is a problem for transmitting information with the currently used modulation formats in fiber optics communications. Indeed, as the power is increased, the signal is more distorted by the nonlinear crosstalk, thus limiting the capability of the receiver in recovering the transmitted information. It is therefore necessary to mitigate the nonlinear effects to compensate for the distortions and to provide novel approaches for communication over the nonlinear fiber-optic channel. Two main paths have been followed up to now to counteract this problem: the first approach consists of mitigating the nonlinear effects through a wealth of techniques such as optical phase-conjugation [5] or digital back-propagation [6]; the second path, more ambitiously, aims at encoding information into the eigenmodes of the nonlinear channel, whose evolution is linear upon spatial propagation. This second approach, originally called eigenvalue communication, has been proposed by Hasegawa and Nyu [7] and it is now, with various modifications, growing as a new paradigm in optical communications [8].

This method exploits the exact integrability of the NLSE through the inverse scattering transform (IST) [9] as the master evolution equation of the electric field propagating in single-mode fiber (SMF). Integrability of the NLSE was demonstrated by Zakharov and Shabat back in 1972 [10], who found an associated spectral problem related to a set of ordinary linear differential equations. Following this approach, it is possible to identify the eigenvalues, which can be considered to be analogous to the frequencies in the classical Fourier transform, and the so-called scattering coefficients, complex amplitudes associated to the eigenvalues. The application of the IST to fiber optics communications allows the use of various and flexible modulation formats [8]. Due to integrability, in the lossless and noiseless limit, nonlinearity is not a detrimental factor anymore, but on the contrary, it is a constitutive element of the transmission system itself. The parallelism between the linear Fourier transform method used to solve linear initial value problems and the IST used to solve nonlinear ones [9] has driven some authors to rename the IST as the nonlinear Fourier transform (NFT) [11], which is the
name currently used in the engineering communities (see [8] for a recent review including historical details). The nonlinear Fourier spectrum of a signal consists of a set of eigenvalues and the respective associated scattering coefficients. The eigenvalues belong either to a so-called discrete spectrum or to a continuous spectrum; the first describes the solitonic components of the signal, while the second is associated with dispersive waves and reduces to the classical Fourier spectrum in the limit of low power.

Communications channels based on both discrete or/and continuous spectrum modulations have been extensively studied and experimentally demonstrated up to now for the scalar (single polarization) NLSE (see e.g., [12–16] to cite just a few).

A series of key challenges that need to be met in order for NFT-based communication to exit the labs and operate in real-world infrastructures has been described recently [8]. One of those challenges consists indeed of endowing the eigenvalue communication approach with polarization division multiplexing, which allows information to be encoded on both orthogonal polarization components supported by SMFs. The description of the light propagation, accounting for its polarization dynamics, can be described, under specific conditions that apply to modern communications fiber links, by the Manakov equations [17]. In a milestone paper of nonlinear science, Manakov showed that those equations can be solved analytically by the IST [18]. Detailed investigations of the solutions of the Manakov equations especially concerning soliton and multisoliton dynamics in the presence of noise and polarization mode dispersion (PMD) in optical communications, as well as their connection with optical rogue waves formation, are present in the literature [19–25].

To the best of our knowledge, the NFT dual-polarization problem has never been tackled at the level aimed to demonstrate a working communication system, and only very preliminary theoretical works are present in the literature on this topic [26,27].

In this paper, we present the mathematical framework underlying the dual-polarization NFT, and we show an extension of our recent results on the first experimental demonstration of a dual-polarization nonlinear frequency division multiplexing (DP-NFDM) fiber optics communication system [28]. We have transmitted up to 373.5 km at the hard-decision forward error correction (HD-FEC) bit error rate (BER) threshold of 3.8 × 10^−3, with information encoded in the quadrature phase shift keying (QPSK)-modulated scattering coefficients associated with two eigenvalues belonging to the Manakov system discrete spectrum, for both orthogonal polarization components supported by a SMF.

The structure of the paper is as follows: in Section 2 we define the NFT for the dual-polarization case, and we describe the mathematical tools— the Darboux transformation (DT)— needed to generate the waveforms associated with a desired nonlinear spectrum for both field polarizations. In Section 3 we discuss the details of a DP-NFDM system. Finally, in Section 4, we present a detailed account of the experimental transmission results, followed by a discussion of the results and conclusions in Section 5.

2. MATHEMATICAL FRAMEWORK

A. Channel Model

The evolution of the slowly varying complex-valued envelopes of the electric field propagating in a SMF exhibiting random birefringence and whose dispersion and nonlinear lengths are much larger than the birefringence correlation length is described by the averaged Manakov equations [17,29],

\[
\frac{\partial E_j}{\partial t} = -i\beta_2 L_j \frac{\partial^2 E_j}{\partial z^2} + i\gamma \left(|E_j|^2 + |E_2|^2\right) E_j,
\]

where \( \beta_2 \) is the dispersion coefficient, and \( \gamma \) is the nonlinearity coefficient.

In order to remove any dependency from a specific channel, it is common to work with the normalized version of Eq. (1). The normalized Manakov system (MS) [18,30,31] is obtained by performing the change of variable,

\[ q_j = E_j \sqrt{P}/L_j, \quad t = \frac{\tau}{T_0}, \quad z = -\frac{\ell}{L}, \]

where \( P = |\beta_2|/\left(\gamma T_0^2\right), L = 2 T_0^2/|\beta_2|, \) and \( T_0 \) is a free normalization parameter, leading to

\[
\begin{align*}
\frac{i \partial q_1}{\partial z} &= \frac{\Delta q_1}{\Delta z} + 2(|q_1|^2 + |q_1|^2) q_1, \\
\frac{i \partial q_2}{\partial z} &= \frac{\Delta q_2}{\Delta z} + 2(|q_1|^2 + |q_2|^2) q_2,
\end{align*}
\]

where \( \Delta x \) and \( \Delta t \) represent the normalized space and time variables, respectively. In this study, we have considered the anomalous dispersion regime (\( \beta_2 < 0 \)), since it is the one that supports solitons and corresponds to the regime of currently deployed SMFs.

In realistic systems, the field amplitude is attenuated upon spatial propagation at a rate \( \alpha/2 \), where \( \alpha \) is the attenuation coefficient of the fiber. This breaks the integrability of Eq. (1). However, it is possible to suitably redefine the fields \( E_{1,2} \rightarrow \sqrt{\gamma} e^{-\alpha z/2} E_{1,2} \) in such a way that they obey a lossless equation with an effective nonlinearity coefficient

\[ \gamma_{eff} = \gamma (1 - e^{-\alpha z})/(\alpha L), \]

where \( L \) is the length of one optical fiber span. The evolution equation with the modified nonlinear term can be considered the leading approximation of the lossy system when we account for the periodic signal boosts due to the erbium-doped fiber amplifier (EDFA). This is the so-called lossless path-averaged (LPA) model [32–34], which is in general valid when the amplifiers’ spacing is smaller than the soliton period, and it has been used across all the present study.

B. Direct NFT

In order to compute the NFT of a signal \( q_1(t) \), it is first necessary to associate to the MS Eq. (3) a so-called spectral problem. This is known for the case of the NLSE as the Zakharov–Shabat spectral problem (ZSP), while for the Manakov equations we can call it the Manakov–Zakharov–Shabat spectral problem (MZSP). The MZSP is defined by the following system of linear ordinary differential equations:

\[ \frac{\partial v}{\partial t} = (\lambda A + B)v \]

being
A = \begin{pmatrix} \ i & 0 & 0 \\ 0 & i & 0 \\ 0 & 0 & i \end{pmatrix}, \quad B = \begin{pmatrix} 0 & q_1 & q_2 \\ -q_1^* & 0 & 0 \\ -q_2^* & 0 & 0 \end{pmatrix},

where \( v \) is a solution, and \( \lambda \) is a spectral parameter.

Assuming the vanishing boundary conditions for the signal, i.e., \( |q_j(t)| \to 0 \) for \( t \to |\infty| \), it is possible to find a set of canonical solutions to Eq. (5) called Jost solutions defined as [30]

\[
\phi^N(t, \lambda) = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} e^{j \lambda t}; \quad \tilde{\phi}^N(t, \lambda) = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} e^{j \lambda t} \to -\infty, 
\]

\[
\phi^P(t, \lambda) = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} e^{j \lambda t}; \quad \tilde{\phi}^P(t, \lambda) = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} e^{j \lambda t} \to +\infty. 
\]

(6a)

\[
\{\phi^P(t, \lambda), \tilde{\phi}^P(t, \lambda)\} \text{ and } \{\phi^N(t, \lambda), \tilde{\phi}^N(t, \lambda)\} \text{ are two bases for the eigenspace associate to } \lambda. \text{ One can write } \phi^N(t, \lambda) \text{ and } \tilde{\phi}^N(t, \lambda) \text{ as a linear combination of the basis vectors } \{\phi^P(t, \lambda), \tilde{\phi}^P(t, \lambda)\} \text{ as}
\]

\[
\phi^N(t, \lambda) = \phi^P(t, \lambda) b(\lambda) + \tilde{\phi}^P(t, \lambda) a(\lambda), 
\]

(7a)

\[
\tilde{\phi}^N(t, \lambda) = \phi^P(t, \lambda) \tilde{a}(\lambda) + \tilde{\phi}^P(t, \lambda) \tilde{b}(\lambda), 
\]

(7b)

with coefficients \( a(\lambda), b(\lambda), \tilde{a}(\lambda), \text{and } \tilde{b}(\lambda) \), where \( a(\lambda) \) is a scalar, \( \tilde{a}(\lambda) \) is a \( 2 \times 2 \) matrix, \( b(\lambda) \) is a two-entry column vector, and \( \tilde{b}(\lambda) \) is a two-entry row vector. These coefficients are called scattering coefficients. From the knowledge of the scattering coefficients, it is possible to reconstruct the signal \( q_j(t) \) uniquely.

Analogously to the case of the NLSE [11], we can define the NFT continuous and discrete spectral amplitudes for the MS as

\[
Q_{\lambda}(\lambda) = b(\lambda) a(\lambda)^{-1} \quad \lambda \in \mathbb{R}, 
\]

(8a)

\[
Q_{\lambda, j}(\lambda) = b(\lambda) a(\lambda)^{-1} \quad \lambda_{1, \ldots, n} \in \mathbb{C} \setminus \mathbb{R},
\]

and

\[
\mathcal{A}(\lambda) = \frac{d}{d \lambda} |_{\lambda=\lambda_{1, \ldots, n}} \in \mathbb{C} \setminus \mathbb{R} \text{ such that } a(\lambda) = 0.
\]

Although these spectral amplitudes are commonly used, it is more convenient to work directly with the scattering coefficients \( a(\lambda) \) and \( b(\lambda) \) [35]; hence, when throughout the whole paper we will refer to the nonlinear spectrum, we will implicitly mean the eigenvalues and the associated scattering coefficients. The scattering coefficients are time independent, and their spatial evolution is given by [30]

\[
a(\lambda, z) = a(\lambda, 0), \quad \tilde{a}(\lambda, z) = \tilde{a}(\lambda, 0), 
\]

(9a)

\[
b(\lambda, z) = b(\lambda, 0) e^{-k z} \quad \tilde{b}(\lambda, z) = \tilde{b}(\lambda, 0) e^{k z}.
\]

(9b)

In order to not overburden the notation, we will drop the explicit space dependence as we did in the beginning of this section. The fact that the scattering coefficients are time invariant allows computing them at an arbitrary instant of time. For example, using Eq. (7a) and the boundary Jost solutions, they can be computed at \( t = +\infty \). At this instant, \( \phi^P(t, \lambda) \) is known. Moreover, it is possible to propagate \( \tilde{\phi}^N(t, \lambda) \) from \( t = -\infty \), where it is known, to \( t = +\infty \) by integrating Eq. (7a). Given the particular structure of the Jost solutions, it results that the scattering coefficients are given by

\[
a(\lambda) = \lim_{t \to +\infty} [\phi^N_j(t, \lambda) \tilde{\phi}^P_j(t, \lambda)^{-1}],
\]

(10a)

\[
b_1(\lambda) = \lim_{t \to +\infty} [\phi^N_j(t, \lambda) \phi^P_{j, 1}(t, \lambda)^{-1}],
\]

(10b)

\[
b_2(\lambda) = \lim_{t \to +\infty} [\phi^N_j(t, \lambda) \phi^P_{j, 2}(t, \lambda)^{-1}],
\]

(10c)

and using Eqs. (6) and (7a) gives

\[
a(\lambda) = \lim_{t \to +\infty} [\phi^N_j(t, \lambda) |e^{j \lambda t}|],
\]

(11a)

\[
b(\lambda) = \lim_{t \to +\infty} \left[ \phi^P_j(t, \lambda) \tilde{\phi}^P_j(t, \lambda) e^{-j \lambda t} \right].
\]

(11b)

It should be noted that, compared to the NLSE case, there is an additional scattering coefficient \( b_3(\lambda) \) that can be used to encode information, potentially doubling the system transmission rate.

C. Inverse NFT

The inverse nonlinear Fourier transform (INFT) is the mathematical procedure that allows construction of a time-domain waveform starting from a given nonlinear spectrum. In our work, we have performed the INFT at the transmitter by using an algorithm based on the DT [36]. The DT is a natural candidate to build time-domain signals, especially when the information is encoded only in the discrete nonlinear spectrum. The method consists of adding iteratively discrete eigenvalues to the nonlinear spectrum while simultaneously updating the signal in the time domain. The INFT based on the DT for eigenvalue communications was proposed in [37]. In our work, we have used the DT for the MS derived by Wright [38]. We summarize here how the DT for the MS works.

Let \( \bar{v} \) be a column vector solution of the MZSP spectral problem Eq. (5) associated with the MS for the signal \( q(t) \) and the eigenvalue \( \lambda \); then according to [38], a new solution of Eq. (5), \( \hat{v} \), is given by the following equation:

\[
\hat{v} = (\lambda I_3 - G_0) v,
\]

(12)

where \( I_3 \) is the \( 3 \times 3 \) identity matrix, and \( G_0 = \Theta M_0 \Theta^{-1} \) with

\[
\Theta = \begin{pmatrix} v_1 & v_2^* & v_3^* \\ \hat{v}_2 & -v_1^* & 0 \\ \hat{v}_3 & 0 & -v_3^* \end{pmatrix},
\]

(13)

where the matrix \( M_0 = \text{diag}(\lambda_0, \hat{\lambda}_0^*, \lambda_0^*) \), and \( \hat{v} = (\hat{v}_1, \hat{v}_2, \hat{v}_3)^T \) is a solution of Eq. (5) for the seed signal \( q_j f, j = 1, 2 \) and a fixed value of \( \lambda = \lambda_0 \). The DT gives the new signal waveforms in the time domain for both polarizations \( \hat{q}_{j, \lambda} = 1, 2 \) as a function of the old signals \( q_j \) of the auxiliary solution \( \hat{v} \) and of the new eigenvalue \( \lambda_0 \) we want to add to the nonlinear spectrum,

\[
\hat{q}_j = q_j + 2i (\lambda_0 - \lambda_0) u_j^* \left( 1 + \sum_{j=1}^2 |u_j|^2 \right) f, \quad j = 1, 2,
\]

(14)

where \( u_j = \hat{v}_{j+1}/\hat{v}_1 \).

Starting from the "vacuum" solution \( q_j(t) = 0, j = 1, 2 \), the procedure sketched in Fig. 1 can be repeated iteratively to generate the dual polarization time domain signal associated with a nonlinear spectrum containing an arbitrary large number of discrete eigenvalues.

The generic auxiliary solution \( \hat{v}^{(k)} \) that satisfies the MZSP for the eigenvalue \( \lambda_k \) reads:

\[
\hat{v}^{(k)} = \left( A^{(k)} e^{-i k \lambda} \right)^T \hat{v}^{(k)} \left( B^{(k)} e^{i k \lambda} \right)^T \left( C^{(k)} e^{-i k \lambda} \right)^T \quad \text{for some initialization constants}.
\]

Hence after adding \( \lambda \) eigenvalues, the auxiliary solutions are modified according to the following chain of matrix multiplications:

\[
\hat{v}^{(k)} = \left( A^{(k)} e^{-i k \lambda} \right)^T \hat{v}^{(k)} \left( B^{(k)} e^{i k \lambda} \right)^T \left( C^{(k)} e^{-i k \lambda} \right)^T \quad \text{for some initialization constants}.
\]
In this section, the basic structure of a DP-NFDM system using the discrete spectrum will be described. The digital signal processing (DSP) chain will be introduced first and then the experimental setup will follow.

### A. Transmitter and Receiver Digital Signal Processing

At the transmitter, the data bits are mapped to the scattering coefficients pairs \( \{b_1(\lambda_i), b_2(\lambda_i)\} \) for \( i = 1, 2 \), where the eigenvalues \( \{\lambda_1 = 0.3, \lambda_2 = 0.6\} \) are used for each symbol. We will refer to these sets of coefficients and equivalently to the associated time domain waveform as a DP-NFDM symbol. The scattering coefficients associated with the first eigenvalue can assume values drawn from a QPSK constellation of radius 5 and rotated by \( \pi/4 \), while those associated with the second eigenvalue are drawn from a QPSK constellation of radius 0.14 as shown in Fig. 2. This particular structure of the constellations was chosen to reduce the peak-to-average power ratio (PAPR) of the signal at the transmitter in order to limit the performance losses due to the limited resolution of the digital-to-analog converter (DAC) and due to the nonlinear characteristic of a Mach–Zehnder modulator (MZM) and electrical amplifiers (see Supplement 1 for a detailed explanation).

The waveform associated to each DP-NFDM symbol is generated using the DT described in the previous section followed by the denormalization as in Eq. (2) with normalization parameter \( T_0 = 47 \) ps. This choice of \( T_0 \) allows fitting the waveform in a time window of 1 ns (1 Gb/d) with enough time guard band among successive DP-NFDM symbols to satisfy the vanishing boundary conditions required to correctly compute the NFT. The power \( P_{\text{tx}} \) of the digital signal thus obtained is later used to set the power of the corresponding transmitted optical signal.

The channel is assumed to be a link of standard SMF with EDFA lumped amplification, as in the experiment. In order to take into account the presence of the losses, the LPA approximation is used in the normalization and denormalization steps of the waveform before computing the NFT and after computing the INFT, respectively.

At the receiver, the digital signal output by the digital storage oscilloscope (DSO) is first rescaled so that its power is \( P_{\text{tx}} \) (the power of the transmitted optical signal). Then an ideal rectangular filter with bandwidth equal to the 99% power bandwidth of the signal is used to filter out of band noise. At this point, cross-correlation-based frame synchronization using training sequences is performed in order to optimally align the DP-NFDM symbol to the processing window. For each DP-NFDM symbol, first the eigenvalues are located using the Newton–Raphson search method employing the one-directional trapezoidal method, and then the coefficients \( b_{1,2}(\lambda_i) \) are computed on the found eigenvalues using the forward-backward trapezoidal method (see Supplement 1 for more details). The homodyne configuration of the receiver allows us to avoid having a frequency offset...
between the transmitter laser and the coherent receiver local oscillator (LO), but given the non-zero combined linewidth of the two lasers (~1 kHz), their coherence length is limited to about 90 km. This implies that the received constellations are affected by phase noise when the transmission distance exceeds the coherence length of the laser, causing errors in the detection of the symbols. The phase noise is removed by applying the blind phase search algorithm in the NFT domain to each constellation individually. Finally, the scattering coefficients are rotated back to remove the phase factor acquired during the transmission (Eq. [9b]), and the decision on the symbols is taken using a minimum Euclidean distance decoder over the scattering coefficients.

B. Experimental Setup

The experimental setup and the block diagrams of the DSP are depicted in Fig. 3. At the transmitter, a fiber laser (FL) with sub-kilohertz (kHz) linewidth is modulated using an integrated dual polarization I/Q modulator driven by an arbitrary waveform generator (AWG) with 20 GHz analog bandwidth and 64 GSa/s. Before uploading it to the AWG, the signal generated by the INFT is predistorted using the ideal inverse transfer function of the MZM (asin(·)). This predistortion is required in order to have a good trade-off between signal-to-noise ratio (SNR) at the output of the MZM and signal distortions caused by its nonlinear transfer function. Nonetheless, given the still high PAPR of the optimized waveform considered (see Supplement 1), this predistortion is not optimal, and advanced methods can be employed to improve further the quality of the transmitted signal [41]. The channel is a fiber link composed of up to 9 spans of SMF fiber with dispersion $D = 17.5 \text{ ps/nm/km}$, nonlinear coefficient $\gamma = 1.25 \text{ W}^{-1} \text{ km}^{-1}$, attenuation $\alpha = 0.195 \text{ dB/km}$, and PMD coefficient $<0.1 \text{ ps/km}^{1/2}$. Two different span lengths of $L = 41.5$ km and $L = 83$ km were employed. Considering these channel parameters, the complex baseband signal generated by the INFT with LPA and denormalized has the following properties: 99% of its power contained within a bandwidth $W = 12.7 \text{ GHz}$, a PAPR of 9.49 dB, and an average power $P_{\text{av}}$ of 5.30 dBm and 7.70 dBm for the span lengths $L = 41.5$ and 83 km, respectively. Given these channel and signal parameters, we have that the soliton period, defined as $(\pi/2)\omega_s$, with $\omega_s = (W/\beta_2)^{1/2}$ the dispersion length [8,42], is 436 km. Being this much larger than the typical birefringence correlation length, which is on a scale of few tens of meters [29], guarantees the applicability of the Manakov averaged model.

In order to properly match the transmitted signal to the channel, the gain of the EDFA at the transmitter is tuned in such a way to set the power of the optical signal to $P_{\text{av}}$. The optical signal is then transmitted through the channel.

At the receiver, the signal is first sent through a 0.9 nm optical band pass filter (OBPF), and then a polarization controller (PC) was used to manually align the polarization of the signal to the optical front end. The use of the PC was required to avoid the use of polarization tracking algorithms for the NFT signals, which were not available at the time of the experiment. In the future it could be possible to use modulation-independent polarization tracking algorithms, as an example, employing independent components analysis [43]. The signal is then detected by using a standard coherent receiver (33 GHz analog bandwidth, 80 GSa/s) in a homodyne configuration where the transmitter laser is used as LO. The acquired digital signal consisting of five blocks of $10^7$ DP-NFDM symbols is then fed to the receiver DSP chain described previously.

4. EXPERIMENTAL RESULTS

The system was initially tested in a back-to-back (B2B) configuration, where the transmitter output has been directly connected to the receiver, in order to obtain the best performance achievable by the system in the sole presence of the intrinsic transceiver distortions (e.g., transmitter front-end distortion, detector noise, 

![Fig. 4. System performance in terms of BER as a function of the OSNR in a back-to-back configuration. The BER of the individual constellations are shown by the violet (Polarization 1) and green (Polarization 2) curves and are grouped per eigenvalue ($\lambda_1 = 0.3$, $\lambda_2 = 0.6$). The black curve represents the average BER over the four constellations.](image-url)
The four experimental constellations of the scattering coefficients \( b_i, i = 1, 2 \) associated with the two eigenvalues \( \lambda_1 = i0.3, \lambda_2 = i0.6 \) are shown at the transmitter side (left) and after 373.5 km (right). Polarization 1 and Polarization 2 are on a violet and green background, respectively.

5. CONCLUSIONS

We have demonstrated experimentally, for the first time to the best of our knowledge, an eigenvalue-based optical communication system employing two orthogonal modes of polarization. We encoded 8 bits/DP-NFDM symbol and demonstrated transmission up to 373.5 km. Furthermore, we have shown that a powerful, but rather abstract mathematical technique, the Darboux transformation, can indeed have a far-reaching impact in applied nonlinear optics, namely, in fiber-based telecommunications. Our results pave the way toward doubling the information rate of NFT-based fiber optics communication systems. Although more research work needs to be done in this direction, by...
demonstrating the possibility of using dual-polarization NFT channels, we have indeed successfully met one of the key challenges that were explicitly highlighted in a recent review of this research field [8] as necessary steps in order to bring eigenvalue communication from a pioneering stage to be a working infrastructure for optical communications in the real world. Furthermore, the demonstration of polarization division multiplexing is a significant step toward a fair comparison of the NFT-based channels with the currently used linear ones where polarization division multiplexing is an established practice.

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See Supplement 1 for supporting content.

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