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Early age fracture properties of microstructurally-designed mortars

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Abstract

This paper compares the fracture properties as well as crack initiation and propagation of real and equivalent mortars. The development of the elastic modulus, tensile strength, and fracture energy at different hydration stages were determined by inverse analysis of load-displacement curves obtained by the compact tension test (CTT). Further, the impact of the moisture content on the aforementioned material properties was also tested on oven-dried equivalent mortars. Digital image correlation (DIC) was used to follow the crack initiation and propagation. The elastic modulus, tensile strength, and fracture energy support the validity of the equivalent mortars approach. The load-displacement curves obtained by the CTT were also compared to those simulated by finite element method showing excellent correlations. DIC revealed the formation of similar crack patterns at comparable load levels between the two mortars. At early age, the moisture content has a considerable influence on the tensile strength and the fracture energy.

Keywords: fracture properties; early-age cracking; compact tension test; inverse analysis; mortar

1. Introduction

Transportation agencies strive to minimize the risk of cracks in structural concrete, as damaged structures accelerate deterioration resulting in increased maintenance costs and reduced service life [1, 2]. Cement-based materials are particularly susceptible to cracking at early-ages, when the

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material properties are still developing and the rate of shrinkage and thermal deformations is high 
[3, 4]. A precise knowledge of the mechanical properties, and in particular of the fracture 
properties, is at the basis of virtually every approach for modeling crack initiation and 
propagation. Indeed, advanced modelling approaches taking into account the formation of cracks 
as well as their propagation necessarily require several time-dependent material properties to be 
known, such as e.g., tensile strength, elastic modulus, Poisson’s ratio, and volumetric 
deformations as well as fracture properties [5, 6].

While most of the aforementioned properties can be more or less easily measured as a function of 
time, the determination of the early-age volumetric deformations such as drying shrinkage, creep, 
and/or relaxation at a given hydration degree is more complicated [7]. Indeed, at early-age the 
microstructure of cement-based materials is continuously evolving due to hydration, which may 
interfere with an accurate determination of such long-term properties [7]. Further, even in the 
case in which the testing time required to measure material properties, such as e.g. the elastic 
modulus or the tensile strength, is short enough to neglect microstructural changes due to 
hydration, additional limitations may be encountered at early-age. For example, the assessment of 
the dependency of material properties on the moisture content or changes in temperature at early-
age is challenging. In fact, the introduction or the withdrawal of water as well as a change in 
temperature at early-age may result in a change in the microstructure evolution.

Recently, a technique based on the replacement of unreacted binder by quartz to produce 
equivalent systems at given hydration stages has been presented [8]. Starting from the knowledge 
of the volume fractions of unreacted binder as a function of time, a new mixture is prepared in 
which the amount of unreacted binder is replaced with an equal volume of non-reactive quartz 
filler [8]. The new mixture (or equivalent mixture) has exactly the same porosity and the same 
volume fraction of the hydration products and reproduces the microstructure of the original 
mixture at a given hydration stage [8]. Once all the remaining binder has completely reacted, the 
equivalent mixture represents a static system, whose microstructure does not change over time 
and/or testing [8]. In the equivalent systems, the binder is assumed to have completely reacted 
after 3 months of curing in moist conditions [7]. The volume fractions of unreacted binder to be 
replaced as a function of time are determined from the real mixture, for example through 
quantitate X-ray diffraction using Rietveld analysis. In this study, five hydration stages are 
investigated, corresponding to five hydration ages (namely 1, 3, 7, 28, and 91 days). At those 
ages, the volume fraction of the unreacted cement was calculated from the real mixtures. More
details regarding the determination of the volume fractions can be found in [8]. Afterwards, five corresponding new equivalent mixtures were prepared.

A comprehensive and systematic comparison between the real systems and the equivalent systems has been recently published [7]. This study, including both mechanical properties (compressive strength, flexural strength and elastic modulus) as well as degree of hydration and calcium hydroxide content by thermogravimetric analysis (TGA) and pore structure by mercury intrusion porosimetry (MIP), supported the validity of the equivalent systems approach [7]. In the present paper, the validation of the approach is extended to the fracture properties.

While the most straightforward method to determine the fracture properties of cement-based materials is represented by the direct tension test, it bears several disadvantages. For example, the direct tension test is more sensitive to eccentricities, rotational boundary conditions, and possibility of multiple cracking formations [5, 9]. Hence, more often, the materials properties are estimated by indirect test methods such as the three-point bending test, the wedge-splitting test or the compact tension test (CTT) [10-12].

In this paper, the material properties prior to cracking and the fracture properties of one real (at five stages of hydration) and five respective equivalent mortar mixtures were obtained by inverse analysis of load-displacement curves obtained from the CTT. Specifically, the material properties were obtained by inverse analysis based on the hinge model [10, 13]. The results obtained by the inverse analysis were afterwards verified by means of FEM simulations using the commercial finite element package TNO DIANA. For further validation of crack initiation and propagation, digital image correlation techniques were applied on a sequence of pictures acquired during testing. This non-destructive approach based on the comparison of consecutive digitized images taken during deformation allows for the derivation of the full-field surface displacement and strains of objects under load [14, 15]. Finally, the material properties deduced by means of inverse analysis i.e., elastic modulus, tensile strength, and fracture energy of the real and equivalent mortar mixtures, were compared and their difference statistically evaluated through the analysis of variance (ANOVA) [16] to validate the equivalent-systems technique. Additionally, differences between the equivalent and real systems regarding the peak points on the load-displacement points (peak force and crack mouth opening) were statistically evaluated using multivariate ANOVA (MANOVA).

Afterwards, the equivalent approach is employed for the first time to investigate the effect of the moisture content on the elastic modulus, tensile strength, and fracture energy at early-age.
2. Materials, mix proportions and curing

One real and five equivalent mortar mixtures were compared in this study. The real mortar mixture was prepared using an ordinary Portland cement (OPC) CEM I 52.5N with a density of 3.13 g/cm$^3$. The following mineralogical composition (by mass) was measured by quantitative X-ray diffraction: 61.2% C$_3$S, 16.2% C$_2$S, 6.6% C$_3$A, 10.5% C$_4$AF and 1.8% CaSO$_4$. The oxide composition of the OPC is shown in Table 1.

The sand used to prepare the mortar mixtures had a density of 2.65 g/cm$^3$, average grain size D$_{50}$ of 312 µm, maximum size of 650 µm, and water absorption of 0.2%. The water-to-solid ratio used was equal to 1.6 by volume (ranging from 0.56 to 0.51 by mass according to the age investigated), while the amount of sand corresponded to 50% of the total mortar volume. It should be noted that the word solid here refers to the sum of the cement and the quartz, the latter used in place of the unreacted cement. Due to the difference in density between cement and quartz the w/s was calculated in volume base.

Five equivalent mortar mixtures were prepared to mimic five different hydration ages of the real mortar mixture, namely 1, 3, 7, 28, and 91 days. In the equivalent mortar mixtures, different volume fractions of the OPC were replaced by quartz (replacement calculated on volume base) with a density of 2.65 g/cm$^3$ and a particle size distribution comparable to that of the cement [7]. The water-to-solid ratio and sand volume were kept constant at each equivalent age and were identical to those of the real mortar mixture. The cement and sand used to prepare the equivalent mortar mixtures are the same as for the real mortar system. The mixture proportions (by volume) of the real and equivalent mortars are shown in Table 2.

Both real and equivalent mortars were mixed in a Hobart mixer in accordance with NF EN 196-1 [17]. The cement and the quartz filler (the latter used only in the equivalent mortars) were mixed for 30 s at low speed with water in the mixing bowl. While still mixing at low speed, the sand was added to the mixing bowl within 30 s, followed by 30 s of mixing at higher speed. After 90 s rest, the mortar was again mixed for final 60 s at high speed. The mortar was cast into a customized formwork ($125 \times 150 \times 10$ mm$^3$) equipped with two insertions to accommodate the two rods for the tensile load transmission during testing (Figure 1).

After 24 hours the samples were demolded. The equivalent mortar samples were wrapped in wet towels and sealed in plastic bags for at least three months of curing in an environmental chamber at 20 °C and 100% RH. Similar to the equivalent mortar samples, real mortar samples were
wrapped in wet towels and sealed in plastic bags, except for the 1 d sample that was directly tested after demolding. The remaining samples were cured in an environmental chamber at 20 °C and 100% RH until testing at 3, 7, 28, or 91 days of age.

At each testing age, three mortar samples were tested both for the equivalent and the real systems. It should be noted that the real specimens were tested at the indicated curing age, while the equivalent specimens were tested after 3 months of curing. Three months correspond to the minimum time needed to simulate the hydration age of the real systems.

Table 1. Chemical composition of CEM I 52.5 N [mass %].

<table>
<thead>
<tr>
<th></th>
<th>SiO₂ %</th>
<th>Al₂O₃ %</th>
<th>Fe₂O₃ %</th>
<th>CaO %</th>
<th>MgO %</th>
<th>K₂O %</th>
<th>Na₂O %</th>
<th>SO₃ %</th>
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<td>0.87</td>
<td>0.17</td>
<td>3.33</td>
<td>0.23</td>
<td>0.33</td>
</tr>
</tbody>
</table>

Table 2. Mixture proportions of the real and the five equivalent mortars [kg/m³].

<table>
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<tr>
<th></th>
<th>Real</th>
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<th>Equivalent 3d</th>
<th>Equivalent 7d</th>
<th>Equivalent 28d</th>
<th>Equivalent 91d</th>
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<td>245</td>
<td>357</td>
<td>428</td>
<td>496</td>
<td>528</td>
</tr>
<tr>
<td>Quartz</td>
<td>0</td>
<td>301</td>
<td>206</td>
<td>145</td>
<td>88</td>
<td>60</td>
</tr>
<tr>
<td>Sand</td>
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<td>1331</td>
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<td>1331</td>
<td>1331</td>
<td>1331</td>
</tr>
</tbody>
</table>

3. Experimental and analytical procedure

During the compact tension test, an eccentric tensile load (at constant displacement rate of 0.12 mm/min) was applied by means of two rods with a diameter of 20 mm to promote initiation and propagation of a single crack at the tip of the notch. The notch was introduced into the sample by water-cooled saw cutting to induce local stress concentrations and create the conditions for the initiation and propagation of a single crack. The notch thickness and length was 0.5 mm and 60 mm, respectively. The geometry of the sample is shown in Figure 1. The sample’s thickness was 10 mm which promotes plane stress conditions [14], while also reducing the time to reach mass equilibrium to investigate the effect of the moisture content (see section 4.6). The crack mouth opening displacement (CMOD) was measured using a clip gage that was placed on the notched surface of the sample.
Figure 1. a) Specimen’s geometry used for the CTT, the dimensions indicated are in (mm); b) setup for the CTT testing including the camera for DIC.

The experimentally-determined load-displacement curves from the CTT were employed to obtain the fracture material properties through inverse analysis based on the cracked hinge model (CHM). Ulfkjaer et al. [18] (with further improvements by Olesen [19]) presented a semi-analytical method for describing the fracture propagation for Mode-I, i.e., the cracked hinge model. The main advantage of the CHM consists in the fact that it yields analytical solutions for the entire load-crack opening curve. Later, Østergaard [10] proposed an inverse analysis algorithm based on the CHM to retrieve information from the wedge splitting test. However, in the CHM the derivation of an analytical solution including multi-linear softening material behavior remained troublesome. Skoček and Stang [13] extended the inverse analysis for wedge splitting tests based on the CHM including multi-linear softening behavior with the intent to increase the accuracy of test simulations. In the present study, inverse analyses including multi-linear softening behavior developed in [13] is employed to simulate the CTT results and to calculate the elastic modulus, tensile strength, and fracture energy. Figure 2 shows the implementation of the CHM, developed in [18] and [19], to the wedge splitting test geometry. The CHM simulates the area directly surrounding the propagating crack using the loading and deformation shown in Figure 2(b) and the stress distribution in Figure 2(c). The rigid boundaries
of the cracked hinge provide a joint to the bulk (uncracked) specimen, which is controlled by Hooke’s law. The comparison and minimization of differences between experimental results and outputs of the CHM via inverse analysis allows for the estimation of the concrete tensile strength, $f_t$, elastic modulus, $E$, and cohesive crack relationship, $g(w)$. Throughout the inverse analysis, the bulk specimen is assumed to behave linear elastically, whereas the cracked state is determined by a stress-crack opening relationship:

$$A = \begin{cases} \sigma_e(\varepsilon) = E\varepsilon & \text{pre-cracked state} \\ \sigma_w(w) = g(w)f_t & \text{cracked states} \end{cases}$$

where $E$ is the elastic modulus, $\varepsilon$ elastic strain, and $\sigma_w(w)$ stands for the stress-crack opening relationship (softening curve) with crack opening $w$. The multi-linear softening curve, $g(w)$, is defined as (for $N > 2$):

$$g(w) = b_i - a_i w \quad \text{with} \quad w_{(i-1)} < w < w_i$$

where $w_i$ corresponds to the intersection of $i$-th and $i + 1$-th line and has the form

$$w_i = \frac{b_i - b_{i+1}}{a_i - a_{i+1}}$$

for $i < N$ and

$$w_N = w_c = \frac{b_N}{a_N}$$

with $N$ equal to the number of lines in the softening curve.

The inverse analysis to determine the tensile strength, Young’s modulus, and cohesive relation consists then of three steps that are repeated until convergence is reached. In the first step the Young's modulus is determined from the experimental data corresponding to the elastic loading. Once the Young's modulus is found, the tensile strength and the first descending branch of the softening curve $a_i$ are computed. Finally, $N - 1$ computations are performed to find $a_i$ and $b_i$, with $i = 2 \ldots N$ defining the multi-linear softening behavior. A sketch of the multi-linear softening curve is shown in Figure 2(d). Additional details on the CHM and the inverse analysis approach are available in the literature, see e.g. [10], [13], [18], and [19].
Figure 2. (a) The wedge split test specimen with the cracked hinge model applied (after [10]), (b) loading and deformation of the hinge (after [19]), (c) the assumed stress distribution (after [19]), and (d) sketch of the multi-linear softening curve (after [20]).

In addition to the clip gage measurements, digital images were repeatedly captured at 10 s intervals using a Nikon D800 36.3 megapixel (7360 × 4912 pixels) camera body with a 60 mm focal length macro lens (AF-S Micro Nikkor 60 mm f/2.8G ED). Prior to loading of the test specimens, three images were captured of the specimen surface and a fourth image including a scale. The lens was placed approximately 1000 mm from the specimen surface, resulting in images covering a region of application of approximately 65 × 65 mm², with each pixel representing 11.7 × 11.7 µm² of physical space. A LED ring flash was affixed directly to the lens to evenly light the specimen surface. Captured images were subsequently processed with a commercially-available software package [21], which utilized a stochastic speckle pattern to identify unique regions, called facets, on the specimen surface at each measurement time. The stochastic speckle pattern on the specimen surface was created prior to testing using black and white spray paint. The facet size within the commercially available software package was set to 15 × 15 pixels (175 × 175 µm²). The software tracked movements of the facets and utilized standard DIC techniques to compute deformations of the specimen surface. Additional information on the hardware used and the DIC technique is available in [15, 21-23].

Finally, a statistical evaluation of the differences between the real and equivalent material properties investigated in this study, i.e., elastic modulus, tensile strength, and fracture energy was performed by means of ANOVA. Specifically, a two-way analysis of variance was applied
taking into account two fixed factors; the five hydration ages and the two systems (real and equivalent). The null hypothesis of no significant difference was tested by comparing the p-value to the significance level $\alpha$ (assuming $\alpha = 0.05$). Similarly, MANOVA using the Pillai test [24] was performed for the peak points on the load-displacement curves experimentally obtained by CTT.

4. Results and discussion

4.1 Load-displacement curve

In Figure 3, the load-displacement curves obtained for the equivalent and real mortars are compared. For ease of illustration, the various testing ages are presented in two graphs. In Figure 3a, the equivalent ages of 1, 7 and 91 days are shown; while in Figure 3b the remaining results for the equivalent ages of 3 and 28 days are presented. The curves shown represent the average behavior of three repetitions of each test. It should be noted that the term equivalent refers to the equivalent mortars which were cured for a minimum of 91 days before being tested and reproducing a given hydration age. On the other hand, the real mortars were tested at the actual age indicated.

In general, the load-displacement curves as a function of the hydration age for all specimens tested show a similar shape, which is typical for quasi-brittle materials, i.e. they exhibit moderate strain hardening prior the attainment of the peak load, followed by rapid strain softening [25]. Nevertheless, the area below the curve increases as the hydration age increases. Similarly, the peak load is a function of the age: the highest peak load is obtained for 91 d old mortars (ranging between 310 and 340 N) while the lowest peak load was measured on the 1 d old specimens (approximately 140 N).

In general, it can be observed from the presented results that the equivalent mortar specimens follow the load-displacement behavior exhibited by the real mortars as a function of time. Excellent agreement between the measured load-displacement curves are observed for mortars at 1 and 7 days. For the remaining test specimens, it should be noted that the equivalent mortars systematically show a reduced peak load. Such difference may be due to an underestimation of the degree of hydration in the real mortars, which will result in a higher replacement of cement binder with quartz in the equivalent mortars [7]. While on one hand the evaluation of the degree of hydration could be improved by increasing the number of samples measured or combining different techniques, it should be noticed that some inherent limitations may arise by the test
methods itself or the sample preparation (for example when stopping the hydration by isopropanol). Nevertheless, it should be emphasized that predicting a precise hydration age was not the goal of the equivalent systems, but having a microstructure that enables the investigation of time dependent and moisture dependent properties without changing in time or during testing.

It should be also emphasized that the slight deviation seen in the real specimen at 91 days at the beginning of the post-peak phase can be due to the testing method such as a shift of the clip gage.

Figure 3. Load-displacement curves comparison measured on the real and equivalent mortars at different hydration ages: a) 1 d, 7 d, and 91 d; b) 3 d and 28 d. The error bars represent the standard deviation calculated at the load peaks and the displacement measured on the different repetitions for each age.

Moreover, it should be noted that discrepancies between the real and equivalent mortars as seen in Figure 3 also arise from the reproducibility related to the CTT method itself. To illustrate this point, Figure 4 shows the load-displacement curves of all tested specimens for one real and one equivalent age, i.e., 3 days. To analyze this issue, the peak points of the curves (i.e., simultaneously the peak forces and the crack mouth opening corresponding to the peak forces) were compared between the real and equivalent systems using two-way MANOVA (with age and type of system as crossed factors). No statistically significant differences (at significance level of
0.05) were found in this case between real and equivalent systems (the P-value according to the Pillai test was 0.66), whereas the specimen age was found to be a significant factor (P-value below 0.01).

The actual differences between the real and the equivalent mortars will be discussed more in detail with regard to the materials properties investigated (elastic modulus, tensile strength, and fracture energy) by means of ANOVA in the following section.

4.2 Inverse Analysis

Results of the inverse analysis are shown in Figure 5, in which experimental and modelled load-displacement curves are compared to each other. For the sake of brevity, only results of equivalent mortars at the equivalent age of 3 and 91 days are shown, including three repetitions for each equivalent age. As can be seen from the presented results, excellent agreement between load-displacement curves determined by inverse analysis and experimentally determined load-displacement curves is obtained. For example the three experimental load-displacement curves at 91 days directly overlap with the simulated ones.
Figure 5. Comparison of the measured and the computed load-displacement curves for the a) 3 d equivalent mortars and b) 91 d equivalent mortar samples.

Figure 6 (a through c) shows the comparison of the material properties between the equivalent and the real mortars in terms of the elastic modulus, tensile strength, and fracture energy obtained by inverse analysis. Error bars represent the standard deviation.

As evident from Figure 6, the elastic modulus and the tensile strength increase with age and reduction of porosity, as expected. Similarly, the fracture energy increases with time due to the increase in number of bonds forming in the mortar as cement hydration proceeds [12, 26].

Comparable results in terms of elastic modulus and fracture energy were found for the real and the equivalent mortars (Figures 6a and 6c). Most of the determined values fall within one standard deviation of the mean except for the results of the mortar specimens with an equivalent age of 7 d, for which the results clearly diverged. It should be noted that only two repetitions were available with regard to the 7 d real mortar, as one sample broke during demolding. While at 7 d the tensile strength results obtained by inverse analysis for the real and the equivalent mortars are similar, erroneous values were returned by the inverse analysis in terms of elastic modulus and more obviously in terms of fracture energy. This is also shown by the experimental load-displacement curve (in Figure 3a), where the OPC real 7 d curve rapidly approaches zero already at a crack mouth opening of approximately 0.14 mm, hence resulting in a reduced fracture energy. Further, the initial slope is much steeper compared to the other results. No data are available for the real mortar at 28 days as all samples inadvertently broke during handling.
The tensile strengths of the real and the equivalent mortars are also comparable, ranging approximately from 1 to 2.5 MPa for the equivalent ages investigated in this study. The two-way analysis of variance on the test results obtained by inverse analysis taking into account the whole evolution of the elastic modulus, tensile strength and fracture energy showed that no statistically significant differences (at significance level of 0.05) exist between the real and the equivalent mortars, hence supporting the validity of the equivalent method approach. The P-values for the considered factor (real or equivalent system) were: 0.15, 0.26, 0.12, for the fracture energy, tensile strength and E-modulus, respectively.

Figure 6. Comparison of the real and equivalent mortars: a) elastic modulus, b) tensile strength, and c) fracture energy as a function of the equivalent age.
As to further validate the elastic modulus results obtained by the inverse analysis, in Figure 7 the elastic moduli evolution as a function of the equivalent age obtained by inverse analysis are compared to the statically and dynamically determined elastic modulus measurements on companion specimens, as presented in [7]. The static and dynamic elastic moduli were measured on 40 × 40 × 160 mm³ mortar prisms (see [7] and [27] for details on the experimental methods). The elastic moduli of the real and equivalent mortars obtained by inverse analysis of the CTT results are closer to the corresponding statically-determined elastic moduli, this is expected considering the similar time spans of both tests. An exception is the real mortar with an equivalent age of 7 days, for which the elastic modulus falls in between the experimentally-measured dynamic and static elastic modulus. For the equivalent mortars (Figure 7b), excellent agreement between the statically-determined elastic moduli and elastic moduli determined by means of the inverse analysis is found for the equivalent ages of 1, 7, and 91 d. For equivalent ages of 3 and 28 d, the results are still within one standard deviation of the mean elastic modulus.

Figure 7. Comparison of the elastic modulus results obtained by inverse analysis and measured on companion specimens by means of static and dynamic techniques.

4.3 FEM Simulation of the CTT load-displacement curve
To further validate the data obtained by inverse analysis, the tensile response of the CTT was modeled using the commercial finite element package TNO DIANA. The CTT was simulated by
means of a 2D model assuming plane stress conditions and consisted of 9550 three-node triangular isoparametric plane stress elements with 4932 nodes representing the concrete, steel, and crack domains (see Figure 8a). Fillets were used at the tip of the notch to reduce artificial stress intensities in this region (see Figure 8b). The crack path was predefined and modelled by means of zero-thickness two-node interface elements assuming Mode-I fracture. Tension softening of the material was described based on a cohesive discrete cracking model in which multi-linear softening relations are adopted from [10]. A nonlinear solution of the system of equations was obtained using a standard Newton–Raphson method with a displacement-controlled convergence criterion.

To investigate the impact of varying mesh sizes on the solution of the problem, a range of interface discretization were studied for the 91d equivalent mortar system. The number of zero-thickness interface elements along the predefined crack path (see Figure 8) was varied between 10 and 100 elements. The input parameters determined by inverse analysis of CTT results are presented in Table 3. For the investigation of the effect of varying mesh sizes on the solution, the results of the surface crack width predicted by the FEM model for the various mesh sizes were normalized to the results obtained with 100 elements discretizing the predefined crack path. Results of the mesh analysis, given in Figure 9, indicate that the influence of the crack interface discretization was negligible (<0.1% difference between the different mesh sizes) for more than 20 crack interface elements. Accordingly, the crack interface was discretized with 100 elements for all solutions.

The input data, i.e., elastic modulus, tensile strength, and cohesive relations, were obtained from the inverse analysis of experimentally determined load-displacement curves at the different hydration ages; see Section 4.1 - Load-displacement curve. While the Poisson’s ratio ν was assumed to be 0.2, it has no influence on the results, due to the geometry that is close to plane stress conditions. An overview of the input parameters for all simulations is provided in Table 3.
Table 3. Input parameters for FEM simulations.

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<tr>
<th>Equivalent system</th>
<th>( E )</th>
<th>( f_t )</th>
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<th>( b_1 )</th>
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<th>( b_2 )</th>
<th>( a_3 )</th>
<th>( b_3 )</th>
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</tbody>
</table>

Abbreviations:  \( E \) – Young’s modulus (GPa),  \( f_t \) – tensile strength (MPa),  \( a_i \) and  \( b_i \) – parameters defining multi-linear softening curve (see also Section 3), and  \( N_{st} \) – applied displacement scenario in FEM model.

In Figure 10, the experimentally-determined load-displacement curves of the equivalent mortars at different equivalent ages are compared to the results from the finite-element calculations. As can be seen from the presented results, numerically determined load-displacements curves are in excellent agreement with the experimental data for all equivalent ages except 28 d, which confirms the validity of the inverse analysis results. The difference observed at 28 days could be due to the fact that the crack was not really straight rising from a mixed-mode behavior, or that the crack did not initiate at the notch, or brached. Results of the digital image correlation for the equivalent mortar at 28 days, see Figure 11, clearly indicates a ‘bending’ of the crack, i.e. the crack does not follow the predefined crack path in the FEM model, which may explain the differences observed between the experimental data and FEM predictions.
Figure 8. a) CTT specimen simulated by means of a 2D model assuming plane stress conditions using the commercial finite element package TNO Diana; b) Fillets used at the tip of the notch to reduce artificial stress intensities.

Figure 9. Normalized surface crack width as a function of the number of interface elements.
4.5 Digital Image correlation

A sequence of pictures was taken during the CTT at intervals of 10 s. Digital image correlation techniques were applied to identify crack initiation and propagation and more importantly whether cracking behavior was comparable at different load levels for the equivalent and real mortar samples.

Figure 10. Comparison of the measured and the simulated load-displacement curves for the a) 1 d, 7 d, and 91 d equivalent mortars and b) 3 d and 28 d equivalent mortar samples.

Figure 11. Digital image correlation results for the equivalent mortar at 28 days: crack propagation.
In Figure 12, the evolution of the crack initiation and propagation during CTT for two different hydration ages is shown by means of an example. The comparison of the real and equivalent mortar behavior at ages of 1 d and 3 d is shown in Figure 12a and Figure 12b, respectively.

In Figure 12, the displacement interpolated at the facets overlay on top of the documented area is also shown. However, it should be noted that the facets overlay is here solely used to better visualize the crack initiation and propagation.

To directly compare the crack initiation and propagation in the real and equivalent mortars during testing, four different stages of the load-displacement curve are reported. For each hydration age, the first three stages are marked in the corresponding load-displacement curves. Stages 1 and 2 represent available strain fields right before and after cracking has occurred. During propagation (stage 3), one picture for the real and one for the equivalent mortars were selected at approximately similar loads. Finally, stage 4 was selected as the last strain field before the sample completely split. Stage 4 is not marked in the respective load-displacement curve, but it is shown in the respective pictures sequence.

The cracks are generally straight, starting at the tip of the notch and propagating to the opposite edge without signs of branching. This observation further reinforces the applicability of the applied inverse analysis and FEM approach to determine the fracture and the mechanical properties of the real and equivalent mortar systems. Besides the shape of the crack, it should be noted that in stage 3 a direct comparison of the real and equivalent mortar suggest a similar crack opening for the applied load.

Further, this analysis extends the validity of the equivalent approach. Indeed, besides the similarity of the materials properties investigated in this study and the previous one [7], the equivalent systems also show a similar cracking behavior.

In light of the excellent agreement of the material properties investigated in this paper between the real and equivalent mortars and the similarity of the crack patterns at comparable load levels, the equivalent system approach further confirms the results shown with regards to the material properties investigated in the previous sections as well as the evaluation and conclusions reported in [7]. This powerful technique can therefore be used to investigate several hydration-dependent properties such as drying shrinkage, creep/relaxation, early-age cracking, and transport properties at early age. Recently, the early-age ultimate drying shrinkage of cement-based mortars was investigated through the use of the equivalent systems [28].
a) Splitting force [N] vs. Crack mouth opening [mm]

- Point 1
- Point 2
- Point 3

Real point 1: Before cracking initiation
Real point 2: After cracking initiation
Real point 3: Cracking at ~50% the peak load
Real point 4: Cracking right before splitting

 OPC real 1d
 OPC equiv. 1d

DIC area
Figure 12. Sequence of frames showing the crack patterns on the surface of the specimens at different loading levels. Comparison between real and the equivalent mortars at a) 1 d and b) 3 d of hydration. The Real point 4 and the Equiv. point 4 (not marked in the top images: Splitting force versus Crack mouth opening) represent the last strain field before the sample completely split.

4.6 Early-age fracture properties as a function of moisture content

In general, in real field conditions concrete is subjected to drying as soon as exposed to the environment (once the curing period is over). The investigation of the materials properties at
early age such as the elastic modulus becomes of paramount importance. Thus, besides allowing
for the simulation of different stages of the evolution of the microstructure with unchanging
systems, the equivalent approach allows also to study the same system at different stages of
drying in regard for example to elastic modulus, tensile strength, and fracture energy. In real
cement based materials, it is possible to investigate the effect of moisture content only on mature
samples, since the drying process takes several days to months to complete and rapid drying may
lead to (micro)cracking and deterioration of the mechanical properties.

Equivalent mortar samples reproducing the equivalent ages of 1, 7, and 91 d with the geometry
shown in Figure 1 were prepared. Three specimens repetition at each equivalent age were tested.
Those ages were chosen as the microstructure and hence the material properties are quite
different.

After 3 months curing, the samples were placed in an oven at 50 °C for about 1 month. It should
be noted that due to the reduced thickness employed to measure the load-displacement curve, the
drying of the samples was obtained in a reduced time (equilibrium was reached within
approximately 3 weeks), while minimizing possible cracking due to occurrence of moisture
gradients (self-restraint). The mass loss of the sample was monitored over time (every 48 h) and
equilibrium was assumed to be reached once the mass difference between two consecutive
measurements was below 0.1%. Further, the temperature of 50 °C was chosen to minimize
possible microstructural damage such as crack formation due to differential shrinkage, and
possible temperature-induced microstructural changes [29]. For example, ettringite starts to
decompose above 60 °C [29, 30].

Figure 13 (from a through c) shows the comparison between the elastic modulus, tensile strength,
and fracture energy results for the equivalent systems in saturated and dried conditions. The error
bars represent the standard deviation.

While the elastic modulus does not seem to be affected by the moisture content, the tensile
strength appears to be dependent on the moisture content, which confirms the results of previous
studies [31]. For each of the equivalent ages investigated, the tensile strength of the dried
specimens is approximately two times higher. This is in accordance with the general strength
reduction observed in cementitious material at higher moisture contents [32, 33]. Similar trends
are observed for the fracture energy, which also increases for lower moisture contents; however,
it should also be noted that the standard deviation associated with the results from the dried
specimens is much higher.
It should be noted that in real field exposures, especially at early age when the concrete is more susceptible to cracking, drying will induce on one hand the shrinkage and hence an increased cracking potential in restrained conditions, but on the other hand drying will also increase the tensile strength of the skin concrete.

Figure 13. Comparison equivalent mortars in saturated and dry conditions a) elastic modulus b) tensile strength and c) fracture energy as a function of the equivalent age.

5. Conclusions
In this paper, the validation of the equivalent system technique applied to OPC mortars has been extended to the determination of fracture properties. The elastic modulus, tensile strength, and
fracture energy, obtained by inverse analysis of the load-displacement curves for the real and equivalent mortar mixtures, were compared. The differences between the real and the equivalent mortars were statistically quantified by means of ANOVA. Further, the crack initiation and propagation in the real and equivalent mortars was monitored by means of DIC.

The experimentally-determined load-displacement curves obtained by means of the CTT for real and equivalent mortars showed excellent agreement. The elastic modulus, tensile strength, and fracture energy results determined by inverse analysis based on the hinge model also supported the hypothesis of similarity between the real and equivalent mortars. The statistical analysis through ANOVA and MANOVA showed that no statistically significant difference (at significance level of 0.05) was observed for the material properties investigated.

To validate the accuracy of the results obtained by the inverse analysis, a FEM model simulating the sample tested in CTT was built. Excellent agreements between experimentally determined and computed load-displacement curves were found for all mortar systems. Further, the elastic modulus results obtained by inverse analysis were compared to static and dynamic elastic moduli measured on companion specimens. Good agreements between results obtained by inverse analysis for both the real and equivalent mortars with the statically determined ones were obtained for most of the test specimens.

Finally, the DIC technique revealed that crack initiation and propagation evolved similarly in the two systems at similar load levels.

Experimental results suggest that the equivalent approach is a powerful method to investigate hydration-dependent and/or moisture-dependent properties. The use of the equivalent approach indeed allows investigations at early age that are otherwise difficult or impossible to perform because of the ongoing hydration while on the other hand moisture-dependent testing requires drying.

To this end, the effect of the moisture content on the elastic modulus, tensile strength, and fracture energy at early-age was investigated. The tensile strength at all ages appears to be the most sensitive to the presence of moisture, increasing systematically upon drying. Despite a less pronounced difference, also the fracture energy seems to increase as the moisture level decreases. On the other hand, the elastic modulus does not seem to be affected.
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