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Modelling of temporal and spatial evolution of sulphur oxides and sulphuric acid under large, two-stroke marine engine-like conditions using integrated CFD-chemical kinetics

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Abstract
In this work, three-dimensional computational fluid dynamics (CFD) studies of sulphur oxides (SOx) and sulphuric acid (H2SO4) formation processes in a large, low speed two-stroke marine diesel engine are carried out. The current numerical study aims to investigate the conversion of sulphuric dioxide (SO2) to sulphuric trioxide (SO3) and the possibility of H2SO4 condensation which are the prerequisites to better understand the corrosion-induced wear phenomenon. This is achieved with the aid of the implementation of a multicomponent surrogate model, which comprises a skeletal n-heptane mechanism and a reduced sulphur
subset mechanism. In the present work, performance of the coupled CFD-chemical kinetic model is evaluated using both qualitative and quantitative methods. The modelling results show that the temporal and spatial evolutions of SO$_x$ predicted by the skeletal model are similar to those by the base mechanism. Predictions of the variations of SO$_x$ and the associated SO$_2$ to SO$_3$ conversion in response to the change of fuel sulphur content, swirl velocity, start of injection, scavenge pressure and humidity qualitatively agree with numerical and experimental results from the literature. The model is further evaluated using the measured SO$_2$ to SO$_3$ conversion levels in a low load, low scavenge pressure case and a low load, high scavenge pressure case. The absolute values of simulated and measured conversion levels are close, although the former appear to be higher. The current results show that the flame impinges at the cylinder liner near top dead centre. The gas is cooled rapidly by the wall temperature and H$_2$SO$_4$ is produced in the region where the local temperature is less than 600 K. Based on the flue gas correlation, the acid dew point temperature is higher than the wall temperature, suggesting that acid condensation may begin early at the top part of the cylinder liner. The predicted distribution corresponds well with the distribution of corroded parts observed in service engines. The model is expected to serve as an important tool to simulate the rates of SO$_2$ absorption into lubricating oil film and H$_2$SO$_4$ condensation in this combustion system.

**Keywords**: combustion; heavy fuel oil; sulphuric oxides; sulphuric acid; marine engine

### 1 Introduction

The majority of the world trade is carried out by the international shipping industry. The de-facto standard propulsion technology for large commercial vessels, for instance container ships, bulk carriers and tankers, is the large, low speed two-stroke marine diesel engine. The
two-stroke concept offers a thermal efficiency of above 50% despite the fact that the commonly used fuel, heavy fuel oil (HFO), is of low quality. Sulphur is generally present as an impurity in HFO. During the in-cylinder combustion process where air is in excess, most of the sulphur is oxidised to sulphuric dioxide (SO₂). The absorption of SO₂ into the engine lubricating oil film may play a role in cylinder wear [1]. Meanwhile, a fraction of SO₂ is subsequently oxidised to sulphuric trioxide (SO₃) [2] and SO₃ reacts with water vapour (H₂O) to form sulphuric acid vapour (H₂SO₄). The latter condenses as aqueous sulphuric acid on engine cylinder liners where the local temperature is low. This promotes corrosive wear on the cylinder liner. The present solution is to apply lube oil which contains limestone additives to neutralise the acid and hence to impede corrosion on liner surfaces. This however increases the operational costs. Also, the rate of acid condensation is dependent on engine operating conditions and fuel sulphur content. Practical evaluations of acid reaction on cylinder liners are therefore not straightforward and optimising the lube oil treatment becomes complicated. In order to prolong the engine lifespan with minimal expenses on lubrication, an improved understanding of the formation of sulphur oxides (SOₓ) in HFO combustion as well as the subsequent H₂SO₄ formation, condensation, and corrosion processes is essential.

While the influences of H₂SO₄ on the physical and chemical behaviour of marine diesel engine lube oils and piston ring were investigated [3,4], engine-out measurements of SOₓ from large, low speed two-stroke marine engines, to date, remain rare [5]. The experimental investigations of emissions have been focusing on nitrogen oxides (NOₓ) and/or particulate matters [6-9]. Even though Tsukamoto et al. [9] measured the conversion rate of sulphur in fuel to sulfate in particulate matter in their two-stroke marine diesel engine experiment, their study concentrated more on the effects of sulphur on particulate formation but not explicitly the formation of SOₓ [9]. The most relevant experimental work was carried out by Cordtz et al. [10] who investigated the tailpipe SO₃ formation of HFO in a medium...
speed four-stroke test engine. A series of SO$_3$ measurements were carried out in the exhaust
gas produced by a single-cylinder test engine with a rated speed of 1500 revolution per min
under steady-state conditions, wherein start of injection (SOI) timing, engine speed and air-
fuel ratio were varied to alter the combustion history. In another study, Engel et al. [11]
investigated exhaust gas compositions sampled from five large diesel engines over a range of
e engine operating conditions using fuels with 0.05% to 0.8% sulphur. The influences of fuel
sulphur contents and engine operating conditions on SO$_3$ formation were studied. In both
studies, variation of the SO$_3$ production with respect to the change of operating condition and
fuel sulphur content was indicated by the conversion of SO$_2$ to SO$_3$ ($\varepsilon$), calculated using Eq.

\[
\varepsilon = \frac{[SO_3]}{[SO_2] + [SO_3]}
\]

This expression assumes the H$_2$SO$_4$ concentration is lumped with the SO$_3$ concentration.

Both studies suggested that the conversion levels varied within the range of 1.0 to 8.0%.

Other investigations on the SO$_x$ formation in marine diesel engines rely mostly on
theoretical models [5,12]. For these numerical studies, the fuel oxidation model is different
from the typical pure hydrocarbon oxidation model used in gasoline or diesel engine
simulations. Instead, accurate high temperature sulphur chemistry is required to be coupled
with the fuel oxidation model. Previous research on sulphur kinetics in flames has provided
an overall understanding of the general aspects of the associated high temperature chemistry
[13-17]. However, early models suffered from a lack of accurate thermodynamics and kinetic
data. Glarborg and co-workers [2,16,17] proposed a detailed hydrogen/sulphur/oxygen
(H/S/O) reaction mechanism, using laboratory reactor experiments and theoretical predictions
to support the model formulation. Although the validation of the H/S/O mechanism was
carried out under atmospheric pressure, it would be expected to extrapolate well to higher
pressure levels. Cordtz et al. [5] and Andreasen et al. [12] combined the mechanism with a
multi-zone model for the investigation of SOx formation under large, two-stroke marine
diesel engine conditions. In their work, the mechanism did not account for the decomposition
or oxidation of hydrocarbons. Solely the post flame phenomena were simulated and chemical
reactions were initiated by equilibrating the species at stoichiometric conditions. One of the
main limitations of these studies [5,12] or in general multi-zone models [18] was the absence
of detailed information of the temperature and combustion product distributions. In addition
to this, a mixing constant had to be calibrated for different engine speeds [5].

Alternatively, three dimensional (3-D) computational fluid dynamics (CFD)
modelling of marine engines is a promising tool to provide a more comprehensive insight into
in-cylinder events [19,20]. Nonetheless, several issues have to be addressed beforehand. First
of all, the simulation has to initiate from fuel injection, followed by fuel evaporation, ignition
and combustion. An accurate yet compact surrogate model which describes both hydrocarbon
and sulphur oxidation has to be constructed. It is noteworthy that, although different reduced
mechanisms for sulphur oxidation have been proposed [5,21], they were not coupled with
hydrocarbon subsets or validated under engine-like conditions. Another challenge is to
simulate the thermal boundary layers on the cylinder wall liner during the high temperature
flame jet impingement where the temperature gradient is usually steep [22,23]. The peak
temperature in the flame jet can reach above 2700 K while the cylinder liner wall temperature
is much lower at approximately 400 K [19]. Based on the steady-state Reynolds-averaged
Navier–Stokes (RANS) simulation on heat transfer from combustion gaseous to the piston
surface in a large marine engine performed by Jensen and Walther [24], it was found that
both the magnitude and the distribution of the predicted wall heat transfer varied significantly
when different wall models were applied. This indicates that such calculation was strongly
dependent on the empirical models. The local temperature near the cold wall is however crucial for the computation of H$_2$SO$_4$ formation rates and has to be properly simulated. Set against these backgrounds, the objective of this work is to develop numerical models for the investigation of SO$_x$ and H$_2$SO$_4$ formation in a large, low-speed two-stroke marine engine. As aforementioned, a compact multicomponent surrogate model that accounts for SO$_x$ formation is not available from the literature. A reduced sulphur subset mechanism is first developed in the current work and is incorporated with the skeletal n-heptane model which was previously built [19]. Apart from this, the near wall spatial resolution is also carefully examined to ensure that the thermal boundary layers along the cylinder liner are properly resolved. The coupled CFD-chemical kinetic model is then evaluated using both qualitative and quantitative methods. Finally, temporal and spatial distributions of SO$_2$ and H$_2$SO$_4$ on the cylinder liner are investigated using the model.

The remainder of the paper is structured such that the formulation of the skeletal chemical mechanism and CFD models are next detailed. This is followed by the descriptions of the mesh configuration and initial conditions. The subsequent section of the paper outlines the comparison of the skeletal model and its base counterpart. In the consequent sections, model evaluation and numerical analyses of the in-cylinder events are presented. Key conclusions from the work are highlighted in the final section of the paper.

2 Numerical formulation and setup

2.1 Chemical kinetic mechanisms

In the development of the multicomponent surrogate model, the 30 species n-heptane model employed in the previous work [19] is used to describe the hydrocarbon oxidation in the HFO combustion. Radicals such as hydroxyl (OH), hydrogen atom (H) and oxygen atom (O), which are essential for the calculation of SO$_x$ formation rates, are included. The sulphur
chemistry is drawn from Hindiyarti et al. [16]. This subset, which comprises 18 species and 98 reactions, is coupled with the n-heptane model. In addition, a reaction (R6), which describes the H$_2$SO$_4$ formation from SO$_3$ and H$_2$O, is taken into account [5,25]. The rate constant for R6 ($k_6$) was obtained at 298 K. A more accurate representation of the reaction is $\text{SO}_3+\text{H}_2\text{O}+\text{H}_2\text{O} \leftrightarrow \text{H}_2\text{SO}_4+\text{H}_2\text{O}$ with $k_6 = 3.1\times10^7 \exp(6540/T)$ [26,27] and a sensitivity study on $k_6$ can be found in Section 3.1.2. The final mechanism consists of 51 species and 169 reactions. This mechanism is henceforth addressed as the full S-HC model for brevity, in which S and HC denote sulphur and hydrocarbon, respectively. It serves as a base model for mechanism reduction and comparison purposes.

Table 1. Reactions and the Arrhenius parameters of the skeletal sulphur model.

<table>
<thead>
<tr>
<th>No.</th>
<th>Reaction</th>
<th>$A$</th>
<th>$n$</th>
<th>$T_a$</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Fuel-S+O$_2$ $\rightarrow$ SO$_2$</td>
<td>Global step, fast</td>
<td></td>
<td></td>
<td>Present work</td>
</tr>
<tr>
<td>2</td>
<td>SO$_2$+O(+M) $\leftrightarrow$ SO$_3$(+M)</td>
<td>3.70E+11</td>
<td>0</td>
<td>850</td>
<td>[16]</td>
</tr>
<tr>
<td></td>
<td>low-pressure limit</td>
<td>2.40E+27</td>
<td>-3.6</td>
<td>2610</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Troe parameters 0.442, 316, 7442</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>low-pressure limit (N$_2$)</td>
<td>2.90E+27</td>
<td>-3.58</td>
<td>2620</td>
<td>[16]</td>
</tr>
<tr>
<td></td>
<td>Troe parameters (N$_2$) 0.43, 371, 7442</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>SO$_3$+H $\leftrightarrow$ SO$_2$+OH</td>
<td>8.40E+09</td>
<td>1.22</td>
<td>1670</td>
<td>[16]</td>
</tr>
<tr>
<td>4</td>
<td>SO$_2$+OH(+M) $\leftrightarrow$ HOSO$_2$(+M)</td>
<td>5.70E+12</td>
<td>-0.27</td>
<td>0</td>
<td>[16]</td>
</tr>
<tr>
<td></td>
<td>low-pressure limit</td>
<td>1.70E+27</td>
<td>-4.09</td>
<td>0</td>
<td>[16]</td>
</tr>
<tr>
<td></td>
<td>Troe parameters 0.10 1E-30 1E+30</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>N$_2$/</td>
<td>SO$_2$/</td>
<td>H$_2$O/</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>HOSO$_2$+O$_2$ $\leftrightarrow$ HO$_2$+SO$_3$</td>
<td>7.80E+11</td>
<td>0</td>
<td>330</td>
<td>[9]</td>
</tr>
<tr>
<td>6</td>
<td>SO$_3$ + H$_2$O $\leftrightarrow$ H$_2$SO$_4$</td>
<td>7.23E+08</td>
<td>0</td>
<td>0</td>
<td>[5,25]</td>
</tr>
</tbody>
</table>

Note: $A$, $n$ and $T_a$ represent the pre-exponential factor, the temperature exponent and the activation temperature in the Arrhenius temperature-dependent form, where $k = AT^n \exp(-T_a/T)$. The unit of $k$ (and $A$) is $\text{mol}^m \text{cm}^3 \text{molecule}^{-1} \text{s}^{-1}$, where $m$ is the overall order of the reaction; while $T_a$ is given in K.

A skeletal subset for the sulphur chemistry is developed to reduce the computational costs. As aforementioned, the fuel sulphur is predominantly oxidised to form SO$_2$ in excess air combustion. In the skeletal model, the oxidation of fuel sulphur to SO$_2$ is assumed to be fast and irreversible (reaction (R1) in Table 1). To identify the key reactions for SO$_3$ formation, calculations are conducted for a perfectly stirred reactor (PSR) using CHEMKIN 4.1 [28]. Fixed temperature calculations are conducted at a pressure of 150 bar. Considering
that the formation of SO$_3$ is limited at temperatures of 2000 K and above [5], the tested
temperatures are fixed from 1200 K to 1800 K with an interval of 200 K. These are selected
to imitate the in-cylinder local temperature during volume expansion after the end of
combustion. The PSR simulations are performed for two fuel/air equivalence ratios ($\phi = 0.5$
and 1.0). Rate of production (ROP) analyses are carried out for a residence time of 0.2 s,
which is approximately the same order of magnitude as the duration from start of combustion
(SOC) to exhaust valve open for the targeted low speed marine engine. The mass fractions of
n-heptane and sulphur are set to 0.98 and 0.02, respectively.

Figure 1(a) depicts the ROP results. As seen, under both lean and stoichiometric
conditions, the recombination of SO$_2$ with atomic O (R2) is the controlling reaction for SO$_3$
formation. The SO$_3$ decomposition is predominantly governed by SO$_3$ + H (R3) and SO$_3$ +
HO$_2$ (R5b). Reaction (R5b) forms HOSO$_2$, which serves as an important intermediate species.
It is found that the important reactions are similar to those identified by Hindiyarti et al. [16]
at lower pressures. The reactions identified here as important constitute the skeletal sulphur
subset shown in Table 1. The reaction of SO$_2$ with HO$_2$ to form SO$_3$ + OH is only marginal
under the investigated conditions and this step is not included in the skeletal model. Figure
1(b) compares the SO$_3$ mole fraction computed using the full and skeletal S-HC mechanisms.
As shown, the skeletal model reproduces the SO$_3$ mole fraction reasonably well under most
of the tested conditions.

Based on the assumption that SO$_2$ formation from fuel sulphur is infinitely fast and
irreversible as well as the ROP results, the full sulphur subset mechanism is reduced to 4
species with 5 reactions. With the reduced counterpart, the multicomponent mechanism
consists of 37 species with 77 reactions. This is henceforth addressed as the skeletal S-HC
model for brevity and its performance is next assessed in 3-D CFD marine engine simulations.
2.2 CFD submodels

The current 3-D CFD simulations are performed in the unsteady RANS framework using the commercial code, STAR-CCM+ version 10 [29]. The Eulerian-Lagrangian framework is utilised to solve the two-phase flow of the fuel spray jet. Rosin–Rammler is applied to model the fuel droplet size distribution while the Kelvin Helmholtz–Rayleigh Taylor (KH–RT) is implemented to simulate the spray breakup. In addition, the Ranz–Marshall correlation is implemented to calculate the droplet heat transfer with the surrounding gas phase. The turbulent flow is modelled using the $k-\omega$ SST model. As highlighted in the introduction, both the magnitude and the distribution of the predicted wall heat transfer varied significantly when different wall models were applied [24]. The all $y^+$ wall model is employed in the current simulations, in which high and low $y^+$ wall models are determined based on the local $y^+$ [29]. When the near-wall mesh resolution is not consistent with the modelling assumptions, significant errors can result. Hence, at the vicinity of the cylinder liner where the corrosion-induced wear is observed, a sufficiently fine mesh is applied in order to ensure that the $y^+$ values are around unity [29]. With this, the low $y^+$ wall model is used to directly resolve the associated viscous sublayer and needs no explicit modelling to predict the flow at the vicinity of the wall boundary. The wall shear stress is computed as in laminar flows [30]. Otherwise, the high $y^+$ wall model i.e. the classic wall-function approach is used when the local $y^+$ is higher than 30 [29]. The chemical kinetic mechanisms developed in Section 2.1 are incorporated into the CFD code through the implementation of the DARS-CFD toolkit [29], where the well-stirred reactor (WSR) model is implemented. In turbulent flows, the diffusion process is mainly governed by the turbulent diffusivity. Salvador et al. [31] demonstrated that the evolutions of axial fuel concentration of non-evaporative diesel spray predicted by their model with the range of turbulent Schmidt numbers between 0.5 and 1 were identical. Hence,
the default turbulent Schmidt number of 0.9 is used in the simulations. More detailed
descriptions on model formulation can be found in the previous work [19].

2.3 Mesh configuration

The simulated engine is the 4T50ME-X test engine at MAN Diesel & Turbo [19,32]. The
ingine has a cylinder bore and stroke of 0.5 m and 2.2 m, respectively. The cylinder has 30
equally spaced scavenge ports with port angles of 20° with respect to the radial direction. The
simulations performed here consider only one engine cylinder and initiate from Top Dead
Centre (TDC). Two injectors are fitted at each side in the cylinder and each of the injectors
consists of four nozzle holes with diameter of 1.05 mm. The symmetry imposed by the two
identical injectors allows a 180° sector mesh to be used to represent half of the combustion
chamber. An illustration of the computation grid is provided in Fig. 2 while the main
specifications for the test engine and injectors can be found in Table 2.

Table 2. Main specifications for the 4T50ME-X test engine.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bore (m)</td>
<td>0.5</td>
</tr>
<tr>
<td>Stroke (m)</td>
<td>2.2</td>
</tr>
<tr>
<td>Connecting rod (m)</td>
<td>2.885</td>
</tr>
<tr>
<td>Number of scavenge ports (-)</td>
<td>30</td>
</tr>
<tr>
<td>Scavenge port angle (°)</td>
<td>20</td>
</tr>
<tr>
<td>Number of injectors (-)</td>
<td>2</td>
</tr>
<tr>
<td>Number of nozzle holes of each injector (-)</td>
<td>4</td>
</tr>
<tr>
<td>Nozzle hole diameter (mm)</td>
<td>1.05</td>
</tr>
</tbody>
</table>

Lube oil is injected in two-stroke service engines and lube oil films with a thickness
of at least a few micrometer are formed to protect the engine liner from corrosion [33]. The
H₂SO₄ and/or water vapour condense on the oil films and mix with the lube oil. Meanwhile,
the aqueous sulphuric acid reacts with the alkaline in the lube oil [3]. Multicomponent fluid
films with complex properties are then formed. Modelling of the fluid films is not taken into
consideration in the current simulations since the condensation process and the behaviour of these fluid films are beyond the present scope of work. The design of the mesh configuration is therefore not constrained by the fluid film thickness and is adapted to the predictions of SOₓ and H₂SO₄.

The 180° computational grid used in the previous work [19] is set as the reference mesh and the spatial resolution is re-examined. For the reference mesh, the minimum isotropic cell size is 2.5 mm at the vicinity of the injection tip and a larger cell size of 5.0 mm is used in the bulk gas region at TDC. Towards each wall boundary, the mesh resolution is designed to be finer in an exponential manner where cells adjacent to each wall have a thickness of approximately 5.0 μm. The computational grid consists of approximately 290,000 cells [19]. The sensitivity of the spatial resolution is evaluated based on two criteria. The first criterion is the SO₂ to SO₃ conversion up to 90 CAD ATDC while the second is the local cell temperature adjacent to the cylinder liner during flame impingement. For the first criterion, the cell size within the bulk gas region is set to 2.5 mm in all three x-, y- and z-directions. The associated number of cells escalates to approximately 1.35 million. This mesh configuration is used to examine if the temporal evolution of averaged SOₓ concentration results reaches grid independence, particularly at later CADs when the mesh is stretched in the axial direction. For the second criterion, twenty prism layers are constructed next to the cylinder liner to resolve the thermal boundary layers. This is essential to improve the prediction of local temperature and H₂SO₄ formation near the liner wall region. The minimum cell thickness is reduced by a factor of ten to 0.5 μm and the total number of cells increases to approximately 410,000. The summary of each mesh configuration can be found in Table 3. The sensitivities of the prediction of SO₂ to SO₃ conversion and local temperature/species formation near the liner wall region to different mesh configuration can be found in Section 3.1.1.
<table>
<thead>
<tr>
<th>Table 3. Summary of the mesh configurations investigated in the current work.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mesh</td>
</tr>
<tr>
<td>------</td>
</tr>
<tr>
<td>I</td>
</tr>
<tr>
<td>II</td>
</tr>
<tr>
<td>III</td>
</tr>
</tbody>
</table>

2.4 Initial conditions

The full load case presented in the previous work [19] is set as the reference case, but a fuel sulphur content of 2.0% (by mass) of the total HFO fuel mass delivered is taken into consideration. The engine speed is fixed at 123 rev/min. In the simulated uniflow scavenged large two-stroke marine engine, angled ports near the bottom of the cylinder function to generate swirling flow. At TDC, the maximum tangential velocity ($U_{0,max}$) is 21 m/s. The in-cylinder pressure at TDC ($P_{TDC}$) is set to 152 bar and a total fuel mass ($m_{fuel}$) of 44.6 g is delivered. The fuel is delivered for a duration of 20.8 crank angle degrees (CADs), where the SOI and end of injection (EOI) are set at 1.2 and 23 CAD after top dead centre (ATDC), respectively. A parametric study is carried out, where only one parameter is varied independently while others are fixed at the values used in the reference case. This is to ensure that the effects on combustion characteristics and SO$_2$ to SO$_3$ conversion in response to each variation can be clearly demonstrated.

As shown in Table 4, three different fuel sulphur content levels of 0.5%, 1.0% and 2.0% are investigated. Besides this, the tangential velocity and SOI timing are altered in order to evaluate effects of gas mixing and pressure rise on SO$_3$ formation, respectively. The pressure at TDC is also changed to investigate the coupling effects from the in-cylinder air mass and peak pressure. This is to imitate different compression pressure attributed by the change of scavenge pressure. The subsequent part of the parametric study varies the initial H$_2$O composition, with the aim to emulate different humidity levels in the service engine. In the last part, the model is used to simulate the SO$_2$ to SO$_3$ conversion in a low load, high
scavenge pressure and a low load, low scavenge pressure case. The computed SO$_2$ to SO$_3$ conversion in these cases is evaluated using both qualitative and quantitative methods.

Table 4. Operating conditions of the test cases.

<table>
<thead>
<tr>
<th>Fuel sulphur (% by mass)</th>
<th>SOI ATDC (CA$^\circ$)</th>
<th>P$_{TDC}$ (bar)</th>
<th>Initial H$_2$O (% by mass)</th>
<th>m$_{fuel}$ (g)</th>
<th>U$_{θ,max}$ (m/s)</th>
<th>Engine speed (rev/min)</th>
<th>Engine load</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>1.2</td>
<td>152</td>
<td>0</td>
<td>44.6</td>
<td>21</td>
<td>123</td>
<td>High</td>
</tr>
<tr>
<td>1.0</td>
<td>1.2</td>
<td>152</td>
<td>0</td>
<td>44.6</td>
<td>16/21$^*$</td>
<td>123</td>
<td>High</td>
</tr>
<tr>
<td>2.0</td>
<td>0</td>
<td>152</td>
<td>0</td>
<td>44.6</td>
<td>21/26</td>
<td>123</td>
<td>High</td>
</tr>
<tr>
<td>2.0</td>
<td>1.2</td>
<td>147/152/167</td>
<td>0</td>
<td>44.6</td>
<td>21</td>
<td>123</td>
<td>High</td>
</tr>
<tr>
<td>2.0</td>
<td>1.2</td>
<td>152</td>
<td>0</td>
<td>44.6</td>
<td>21</td>
<td>123</td>
<td>High</td>
</tr>
<tr>
<td>2.0</td>
<td>1.7</td>
<td>67/76</td>
<td>0</td>
<td>19.8</td>
<td>21</td>
<td>78</td>
<td>Low</td>
</tr>
</tbody>
</table>

* indicates the reference case which is the same in all the parametric studies.

3. Results and discussions

3.1 Sensitivity studies

3.1.1 Mesh resolution

The SO$_2$ to SO$_3$ conversion illustrated in Fig. 3(a) is computed using Eq. (1). As seen, the conversion level predicted using the reference mesh is close to that of the fine mesh, indicating that the reference mesh reaches grid independence. Next, two test cases with different cylinder liner wall temperatures are used to examine the near wall temperature distribution. Figure 3(b) provides the temperature distribution along a line probe for a distance of 20 μm from the wall liner at 30 CAD ATDC where the flame impingement is observed. As can be seen, the mesh with ten prism layers is insufficient to resolve the thermal boundary layers. The local temperatures adjacent to the wall are 573 K and 693 K in the cases.
with wall temperatures of 323 K and 523 K, respectively. With the use of the twenty-prism layer mesh, the local cell temperatures of the cell adjacent to the wall are approximately 353 K and 538 K, respectively. Considering that the temperature gradient is steep at this location, these values are satisfactorily close to their respective wall temperatures. The highest $y^+$ value at the cylinder liner remains below 1.9 for the tested conditions. It is concluded that the thermal boundary layers are sufficiently well resolved and the mesh configuration with twenty prism layers is hereafter applied in all the subsequent simulations.

3.1.2 Physical and chemical models

The sensitivity of the turbulence model is evaluated based on SO$_x$/H$_2$SO$_4$ formation in a high load case (baseline) and a low load case (low load, low scavenge pressure). The results can be found in Fig. 4(a). The realizable $k$-$\varepsilon$ model is used as an alternative model here. The SO$_2$ formation is independent from the turbulence model used. Although the SO$_2$ to SO$_3$ conversion is higher with the use of the realizable $k$-$\varepsilon$ model, the percentage point of the conversion remains within 0.6% in both the high and low load cases.

On the other hand, it is noteworthy that the rate constant of reaction (6) which describes the formation of H$_2$SO$_4$ from SO$_3$ and H$_2$O was determined at room temperature and pressure. To the authors’ knowledge, there are no data available under engine-like conditions. The alternative H$_2$SO$_4$ formation reaction as proposed in [26,27] is investigated here. Fig. 4(b)(i) shows that the averaged H$_2$SO$_4$ concentration predicted by both H$_2$SO$_4$ formation reactions have very small differences. The sensitivity study is next extended to high load cases with different initial H$_2$O levels as depicted in Fig. 4(b)(ii). Similar to the previous observation, the difference is not pronounced. For all the test conditions, the relative difference remains within 5%.
3.2 Comparisons of full and skeletal S-HC models

3.2.1 Spatial evolution

Figure 5 depicts the distribution of the mass fraction of SO₂ and H₂S on two perpendicular planes created across the spray combustion region at 10 CAD ATDC. As illustrated by Fig. 5(a), SO₂ is the principal SOₓ within the flame jet when the skeletal model is applied. Comparisons between Figs. 5(a) and (c) show that spatial distribution of SO₂ predicted using the skeletal and full S-HC models has minor discrepancies. When the latter is used, formation of H₂S dominates at regions with high equivalence ratio i.e. fuel-rich regions. The spatial distribution of total SO₂ and H₂S mass fractions shown in Fig. 5(b) is found to be closer to that of SO₂ predicted using the skeletal model. Yet, the associated total mass fraction is lower since the oxidation of fuel sulphur is slower when the finite rate chemistry is used. This is further discussed using the species temporal evolution profiles in Section 3.2.2. Based on the present CFD results, SO₃ is formed at the vicinity of the diffusion flame where atomic O is formed. A further elucidation is provided below.

Figure 6 demonstrates the distribution of SO₃ mass fraction within the temperature-equivalence ratio map. When a noticeable amount of SO₃ is formed, the flame has impinged at the wall and the SO₃ has also been broadly distributed by convection. In order to provide a clearer illustration, only cells with significant of production rate of SO₃ (from SO₂) is plotted. The temperature-equivalence ratio map shows that SO₃ formation is limited above 2000 K. The formation SO₃ is increasingly favoured as the in-cylinder temperature reduces during expansion. As shown in Figs. 6(c) to (d), the primary SO₃ formation takes place within the temperature range from 2000 K to 1200 K. It should also be noted that the SO₃ formation occurs mainly within the stoichiometric and fuel lean regions. The temperature-equivalence ratio maps and SO₃ spatial distributions predicted by the full and skeletal S-HC models are
identical. As such, the prediction of $H_2SO_4$ formation is also expected to be similar when the
gas containing $H_2O$ and $SO_3$ are cooled upon contact with the cylinder wall liner surface.

3.2.2 Temporal evolution at different fuel sulphur levels

The temporal evolutions of averaged $SO_x$ and $H_2SO_4$ concentrations calculated using the
skeletal and full S-HC mechanisms are compared in Fig. 7. When the fast, irreversible
reaction is used to describe $SO_2$ formation from fuel sulphur, the averaged $SO_2$
concentrations increase at a faster rate. Otherwise, the conversion depends on the overall
burning rate. Based on a separate ROP analysis (not shown), the governing species in the
oxidation of sulphur to $SO_2$ include $S_2$, SH, SO and $H_2S$, in which $H_2S$ is produced under fuel
rich conditions. Figure 7(a) depicts that as the relevant species and reactions are integrated
into the skeletal model, the temporal evolution of $SO_2$ is akin to the full S-HC results. Figure
7(a) also demonstrates that the $SO_2$ produced by the full S-HC model increases almost
linearly with the fuel sulphur content. The averaged $SO_2$ concentrations at 90 CAD ATDC
are 119, 243 and 485 parts per million by volume (ppmv) for fuel sulphur content of 0.5%,
1.0% and 2.0%, respectively. The averaged $SO_2$ concentrations at 90 CAD ATDC predicted
by the full S-HC model are approximately 6% lower as compared to those calculated using
the fast, irreversible reaction in the skeletal model. The difference is caused by the $H_2S$ which
is not fully oxidised. As shown earlier in Fig. 5(d), $H_2S$ is produced and starts to dwell on top
of the piston surface where the region is fuel rich. Its concentration gradually decreases due
to oxidation. However, the oxidation rate of $H_2S$ decreases significantly at approximately 45
CAD ATDC, attributed to the absence of $O_2$ at the vicinity. Besides this, it is worth
mentioning that the WSR model is used in the current simulations, where the sub-grid
turbulence chemistry interaction is not accounted for. This may also lead to the rapid
consumption of oxidiser in the earlier stage. Hence, a small amount of H$_2$S it not oxidised and remains until 90 CAD ATDC.

Despite of the difference in SO$_2$ prediction, Fig. 7(b) shows that the averaged SO$_3$ concentrations calculated using the skeletal S-HC model are close to those of the base mechanism for all fuel sulphur levels. SO$_3$ formation is relatively slow and favoured only when the temperature decreases during cylinder expansion. It takes approximately 70 CAD to reach 90% of the final conversion level. Due to the accurate prediction of the SO$_3$ profiles, the averaged H$_2$SO$_4$ concentrations are also reproduced using the skeletal S-HC model.

Figure 7(d) shows the conversion for the three fuel sulphur contents. When the skeletal model is used, Eq. (1) is used to compute the conversion factor. As the full model is utilised, a certain amount of H$_2$S is predicted in the early stage and its concentration is taken into consideration. As seen, the final conversion factors vary within a range of 5.0% to 6.5%. The conversion from SO$_2$ to SO$_3$ depends on the availability of free radicals, mainly atomic O. When the fuel sulphur content is low relative to the fuel amount, there are more radicals available. The conversion hence increases inversely with the fuel sulphur content. This agrees qualitatively with experimental results presented by Engel et al. [11].

3.2.3 SO$_2$ and H$_2$SO$_4$ formation on cylinder liners

The full and skeletal S-HC mechanisms are next used to predict SO$_2$ and H$_2$SO$_4$ concentrations on the cylinder liner. Figure 8(a) shows that the maximum SO$_2$ mass fraction at the cylinder liner calculated using the skeletal S-HC model is approximately 0.004 which is about 1.5-fold higher than that predicted using the base counterpart. As discussed earlier, the difference is attributed to the H$_2$S which is formed within the fuel rich region but is yet to be oxidised to SO$_2$. On the other hand, Fig. 8(b) displays that the maximum H$_2$SO$_4$ mass fraction predicted by both the S-HC mechanisms has no significant difference. Subsequently,
effects of the wall temperature on SO$_2$ and H$_2$SO$_4$ formation at the wall liner are investigated. The liner wall temperature is increased from 323 K to 523 K, in which the latter is the maximum temperature measured in this marine test engine [32]. When the wall temperature is increased to 523 K, the maximum H$_2$SO$_4$ mass fraction is marginally lower and the averaged H$_2$SO$_4$ concentration at 90 CAD ATDC is reduced by 0.2 ppmv.

This section demonstrates that the skeletal S-HC model is capable of replicating the important characteristics in SO$_x$ formation. With the use of four 64-bit Intel Ivy Bridge Xeon E5-2650 v2 8-core CPUs running at 2.60 GHz [34], the computational runtime consumed by the skeletal S-HC mechanism is approximately 160 hours, which is 1.8-fold shorter than that of the full S-HC mechanism. This indicates that implementation of the skeletal model achieves a good compromise between accuracy and computational efficiency. The numerical model is next evaluated through a parametric study at different engine operating conditions.

3.3 Model evaluation

3.3.1 Parametric study under the full load condition

All the simulations presented in this section are carried out at a fuel sulphur content of 2.0% by mass while the liner wall temperature is fixed at 323 K. The maximum tangential velocity is first varied. This serves to study the influence of different swirl velocity levels in the combustion chamber. Figure 9(a)(i) shows that the peak pressure is lower by approximately 5 bar when the maximum tangential velocity is reduced from 26 m/s to 16 m/s. In these test cases, the SO$_2$ formation is similar. As seen in Fig. 9(a)(ii), the onsets of SO$_2$ to SO$_3$ conversion are the same for three cases but the conversion in the low swirl case starts to diverge at approximately 15 CAD ATDC. The top view of resampled volume of O radicals at 10 CAD ATDC is provided in Fig. 10 to elucidate the phenomena. The outline of Fig. 10 represents the edge of the cylinder, while the centreline is the cyclic boundary where the 180°
domain is revolved to full cylinder to illustrate the in-cylinder event. It is apparent that the flame is more rapidly transported by the stronger swirling flow in the high swirl cases. A greater amount of O radicals are entrained into the flame jet at the opposite side. The earlier flame interaction allows the O atoms to react earlier with SO$_2$, promoting a higher level of SO$_2$ to SO$_3$ conversion. For all the cases, the swirling flow weakens in the later phase of the expansion stroke. The turbulence intensity and hence the mixing rate reduce correspondingly. The conversion remains lower in the low swirl case, as illustrated in Fig 9(a)(ii). It should also be highlighted that the micro-mixing at molecular level is not considered here since the WSR model is applied in the current simulations. Yet, this trend somewhat agrees with the multi-zone results presented by Cordtz et al. [5], which showed a decrease in SO$_3$ level when the gas mixing constant is reduced.

The second parameter investigated is the SOI timing. The SOI timing is advanced to TDC and retarded to 2.4 CAD ATDC, while keeping the injection duration, the mass flow rate and the fuel amount unchanged. In the SOI sweep, the in-cylinder temperatures at SOI in these test cases are similar due to the minor variation. Also, since the adiabatic flame temperature ($T_{ad}$) is not significantly influenced by the in-cylinder pressure [19], both the peak and mean $T_{ad}$ values in these cases are identical. Fig. 9(b)(i) depicts that the SOC is delayed with the SOI. Corresponding to this, the associated temperature increases at a later CAD and the peak pressure drops. As it may be expected, the onset of SO$_2$ is delayed with the SOI. Since the oxidation of fuel-S to SO$_2$ is a fast reaction, the averaged concentration eventually increases to a similar level to that of the early injection case. However, the associated SO$_2$ goes through the oxidation process later in the retarded injection cases. As a result, the SO$_2$ to SO$_3$ conversion at 90 CAD ATDC drops when the SOI timing is delayed. This is depicted in Fig. 9(b)(ii). The same trend is observed in the measurements performed by Cordtz et al. [10] in the medium speed four-stroke engine.
The in-cylinder $P_{TDC}$ is varied next, with the aim to emulate a change of scavenge pressure. Figure 9(c)(i) shows that the peak pressures are lower at decreased in-cylinder pressures but the SOC in these cases are identical due to such high pressure conditions. As aforementioned, the peak $T_{ad}$ is not strongly affected by the in-cylinder pressure at SOI. It is also noticed that the flame interaction begins at a similar CAD. Hence, it is deduced that the in-cylinder air mass plays an important role in determining the SO$_2$ to SO$_3$ conversion here. As the trapped air mass is reduced in the lower $P_{TDC}$ but the total amount of fuel delivered remains the same, the associated global air to fuel ratio decreases. As a consequence, the formation rates of SO$_3$ and the associated conversion decrease. This variation, seen in Fig. 9(c)(ii), agrees qualitatively with the measurements reported by Cordtz et al. [10].

The last parameter varied is the initial H$_2$O level. 0.5%, 2.0% and 4.0% of H$_2$O (by mass) is introduced in the initial condition while the O$_2$ concentration is kept unchanged. As shown in Fig. 9(d)(i), the peak pressure levels in all four cases do not vary. The SOC, flame interaction timing and in-cylinder air mass are also identical. Nonetheless, the presence of the water vapour increases the O/H radical pool that promotes the SO$_2$ oxidation. The averaged OH concentration is found to increase with the increase of initial H$_2$O levels. Under these conditions, SO$_3$ is formed mainly by the sequence through reactions 4 and then 5 in their forward direction [16]. As a result, the SO$_2$ to SO$_3$ conversion increases with the humidity.

To date, SO$_2$ to SO$_3$ conversion measurements under the full load condition is not available. However, the simulation results presented in this section demonstrate that variation of the conversion with respect to the change of operating parameters predicted by the CFD-chemical kinetic model qualitatively agrees with numerical and experimental results from the literature [5,10,11,16]. The model is next applied to simulate the SO$_2$ to SO$_3$ conversion under the low load condition. The simulated results are compared against the measurements obtained from the same research engine.
3.3.2 Comparison with engine measurements under low load condition

As shown in Fig. 11(a), the peak pressures in both of the low load cases are captured, although a maximum relative difference of 6.2% is observed in terms of peak pressure. In the experiments, the salt method was used to analyse the SO$_2$/H$_2$SO$_4$ content in the exhaust gas [35,36]. This was then used to calculate the conversion levels. Eleven measurements were carried out for the low load, low scavenge pressure case. The conversion varies within a narrow range of 4.2% to 4.7%, showing that the reproducibility of the salt method is acceptable. When the salt method was used for the low load, high scavenge pressure case, a higher conversion level of 5.4% was recorded. These values are plotted in Fig. 11(b) for comparison purposes. It is found that the experimental trends are reproduced by the model as well, even though the predicted conversion is consistently higher.

As the engine operates at different loads, the in-cylinder pressure, engine speed and total amount of fuel delivered are varied. Variation of these parameters has opposite effects on the overall conversion [5,10]. The competing effects among these parameters is investigated by converting the full load (reference) case to the low load, high scavenge pressure case in a step-wise manner (not shown). It should be mentioned that this parametric study is solely used to examine the competing effects among the engine parameters on the conversion and the intermediate operating conditions are not feasible in the test engine. At the lower engine load, the in-cylinder pressure is lower and hence the SO$_2$ to SO$_3$ conversion decreases. By reducing the in-cylinder pressure by a factor of two (from 152 bar to 76 bar), the conversion level at 90 CAD ATDC is decreased by a factor of four. Apart from the in-cylinder pressure, the engine speed also reduces to 78 rev/min in the low load case. A longer period is available for gas mixing, promoting the SO$_2$ to SO$_3$ conversion. The effect of the engine speed, however, is less pronounced. An increase by approximately 0.32 percentage point is observed when the engine speed is reduced from 123 to 78 rev/min. Lastly, the total
fuel amount delivered is reduced by approximately 50% in the low load case as compared to
that under the full load condition. This increases the global air to fuel ratio and consequently
increases the conversion level by a factor of four. As the total fuel amount delivered is scaled
with in-cylinder air mass, the global fuel to air ratio becomes similar. The resulting
conversions for low and full load conditions do not vary significantly. A one percentage point
increase is observed for the estimated conversion at 90 CAD in the low load, high scavenge
pressure case. The simulated averaged SO\textsubscript{x}/H\textsubscript{2}SO\textsubscript{4} concentrations at 90 CAD ATDC for all
the test cases are summarised in Table 5.

### Table 5. Averaged SO\textsubscript{x}/H\textsubscript{2}SO\textsubscript{4} concentrations at 90 CAD ATDC in all the test cases.

<table>
<thead>
<tr>
<th>Engine parameters</th>
<th>Species concentrations [ppmv]</th>
<th>( \text{SO}_2 )</th>
<th>( \text{SO}_3 )</th>
<th>H\textsubscript{2}SO\textsubscript{4}</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Fuel sulphur (% by mass)</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.5</td>
<td>125.9</td>
<td>8.9</td>
<td>0.2</td>
<td></td>
</tr>
<tr>
<td>1.0</td>
<td>254.0</td>
<td>16.0</td>
<td>0.4</td>
<td></td>
</tr>
<tr>
<td>2.0</td>
<td>512.2</td>
<td>28.1</td>
<td>0.7</td>
<td></td>
</tr>
<tr>
<td><strong>U\textsubscript{\text{\text{\text{\text{a}}}max} (m/s)</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>16</td>
<td>514.5</td>
<td>26.5</td>
<td>0.6</td>
<td></td>
</tr>
<tr>
<td>21</td>
<td>512.2</td>
<td>28.1</td>
<td>0.7</td>
<td></td>
</tr>
<tr>
<td>26</td>
<td>510.9</td>
<td>28.7</td>
<td>0.7</td>
<td></td>
</tr>
<tr>
<td><strong>SOI ATDC (CA\textdegree)</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>510.8</td>
<td>29.2</td>
<td>0.7</td>
<td></td>
</tr>
<tr>
<td>1.2</td>
<td>512.2</td>
<td>28.1</td>
<td>0.7</td>
<td></td>
</tr>
<tr>
<td>2.4</td>
<td>512.9</td>
<td>28.5</td>
<td>0.6</td>
<td></td>
</tr>
<tr>
<td><strong>Initial H\textsubscript{2}O (% by mass)</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>512.2</td>
<td>28.1</td>
<td>0.7</td>
<td></td>
</tr>
<tr>
<td>0.5</td>
<td>511.1</td>
<td>28.6</td>
<td>0.9</td>
<td></td>
</tr>
<tr>
<td>2.0</td>
<td>510.2</td>
<td>29.5</td>
<td>1.2</td>
<td></td>
</tr>
<tr>
<td>4.0</td>
<td>509.4</td>
<td>29.9</td>
<td>1.6</td>
<td></td>
</tr>
<tr>
<td><strong>P\textsubscript{TDC} (bar)</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>147</td>
<td>529.5</td>
<td>27.3</td>
<td>0.7</td>
<td></td>
</tr>
<tr>
<td>152</td>
<td>512.2</td>
<td>28.1</td>
<td>0.7</td>
<td></td>
</tr>
<tr>
<td>167</td>
<td>463.4</td>
<td>29.3</td>
<td>1.0</td>
<td></td>
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<tr>
<td>67\textdegree</td>
<td>455.1</td>
<td>28.9</td>
<td>1.1</td>
<td></td>
</tr>
<tr>
<td>76\textdegree</td>
<td>433.0</td>
<td>29.5</td>
<td>1.1</td>
<td></td>
</tr>
</tbody>
</table>

* indicates low load cases

#### 3.4 In-cylinder phenomena

The temporal evolution of SO\textsubscript{x} and H\textsubscript{2}SO\textsubscript{4} mass fractions at the liner wall under the low load,
low scavenge pressure condition are investigated. In this case, the flame impingement starts
at 6 CAD ATDC and small patches of H$_2$SO$_4$ are observed on the cylinder liner surface. The flue gas correlation as expressed by Eq. (2) is used to estimate the dew point temperature, $T_{DP}$ (in the unit of Kelvin) and to assess the probability of acid condensation.

$$
T_{DP} = [2.276 \times 10^{-3} - 2.943 \times 10^{-5} (\ln p_{H_2O}) - 8.58 \times 10^{-5} (\ln p_{H_2SO_4}) + 6.2 \times 10^{-7} (\ln p_{H_2SO_4})(\ln p_{H_2SO_4})]^{-1}
$$

$p$ in Eq. (2) is the partial pressure in millimetre in mercury (mmHg) of each participating species [37].

As shown in Fig. 12(a), the highest dew point temperature appears to be 502 K at 6 CAD ATDC for the current case. This indicates that the acid condensation may start early at the upper part of the cylinder liner. The results are consistent with practical experience of large two-stroke engines where corrosion-induced wear is pronounced in the top of the liner around the ring pack position at TDC [38]. The region with high dew point temperatures becomes broader at 10 CAD ATDC and its distribution covers majority of the engine liner at 15 CAD ATDC. These distributions are illustrated in Figs. 12(b) and (c), respectively.

Scatter plots of the H$_2$SO$_4$ molar concentration against the distance from the wall are constructed for gas with different temperature ranges. These plots are provided in Fig. 13 and are used to inspect the H$_2$SO$_4$ boundary layer. At 15 CAD ATDC, the in-cylinder temperature is still high and the temperature gradient is steep towards the cylinder wall. For instance, at the Point A indicated in Fig. 12(c), a variation of approximately 2000 K is observed within a distance of 0.2 mm. The formation of H$_2$SO$_4$ is hence very close to the wall where the temperature is low. The reaction zone has a thickness of approximately 0.02 mm and the production rate significantly falls at temperatures above 600 K (not shown). At this CAD, the gas containing high H$_2$SO$_4$ molar concentration is mainly observed in the region 0.1 mm from the wall. It appears to be approximately five-fold thicker than the region where H$_2$SO$_4$ is produced, suggesting that the H$_2$SO$_4$ boundary layer thickness is influenced by convection.
At the later CADs, the in-cylinder temperature reduces due to volume expansion. The local temperature at the region adjacent to the wall decreases correspondingly and the H$_2$SO$_4$ boundary layer thickness increases since these low temperature regions favour for H$_2$SO$_4$.

The scatter plots given in Figs. 13(b) to (d) are used to illustrate the development of the boundary layer during the expansion stroke.

On the other hand, a noticeable amount of SO$_2$ has yet to be converted to SO$_3$ and reaches the cylinder liner. This is similar to the previous observation in the high load case as discussed in Section 3.2.3. Under the low load condition, SO$_2$ appears at the liner at 6 CAD ATDC alongside the flame impingement (not shown). The SO$_2$ distribution becomes broad at 15 CAD ATDC and it lasts until approximately 25 CAD ATDC. During this period, SO$_2$ may absorb into the engine lubricating oil film and potentially contribute to cylinder wear [1].

The numerical model, which has been developed and evaluated in the present work, is expected to serve as an important prerequisite for further studies related to the corrosion-induced wear phenomenon in the large two stroke marine engines. For instance, together with a fluid film model, the H$_2$SO$_4$ condensation rate on the lube oil film and the associated condensed mass can be investigated [39]. Similarly, the investigation of the SO$_2$ absorption rate into the engine lube oil film on the cylinder liner can also be carried out. An improved understanding of these processes is crucial to address the corrosion-induced wear issue and hence to prolong the marine engine lifespan with minimal expenses on lubrication.

4 Conclusions

This work presents 3-D CFD modelling of SO$_x$ and H$_2$SO$_4$ formation in the HFO combustion under the large, low speed two-stroke marine diesel engine-like conditions. A HFO surrogate model, namely skeletal S-HC mechanism is constructed by integrating a reduced sulphur mechanism and a skeletal n-heptane mechanism. The final surrogate fuel model which
considers fuel and small hydrocarbon oxidation, thermal NO production as well as SOx and
H2SO4 formation consists of 37 species and 77 reactions. It is shown in the current work that
although the associated averaged SO2 concentration at 90 CAD ATDC is higher than that
predicted using its base counterpart, the maximum relative difference remains within 6%.
Besides this, the predicted temporal evolution of SO3 and H2SO4 using both mechanisms are
identical. With the use of the skeletal S-HC model, the following conclusions can be drawn:

- Variation of the conversion in response to the change of fuel sulphur content, swirl
  velocity, SOI timing, scavenge pressure, humidity and engine load estimated by the
  model is in good qualitative agreement with the numerical and experimental results
  from the literature.
- The key factor influencing the difference in high and low load cases is the global air to
  fuel ratio which depends on the in-cylinder mass of the trapped air and the total fuel
  amount delivered.
- The simulated SO2 to SO3 conversion is close to the measurements recorded from the
  same marine engine.
- Acid condensation could begin at approximately 6 CAD ATDC when the flame hits the
  top part of the engine liner, corresponding well with the distribution of corroded parts
  observed in the engine cylinder.
- Relatively large amount of SO2 are also found to dwell at the cylinder liner, suggesting
  that SO2 may absorb into the engine lubricating oil film and potentially contribute to
  cylinder wear.

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Fig. 1. (a) Rate of production for SO$_3$ reactions and (b) comparisons of SO$_3$ mole fraction calculated using the skeletal and full S-HC models at (i) $\phi = 0.5$ and (ii) $\phi = 1.0$ for P = 150 bar. Note for Fig. 1(b): Solid lines represent the skeletal model results while dotted lines denote the full model results.
Fig 2. (a) Side view and (b) top view of the computational grid used in the marine engine simulations (Adopted from [19]).
Fig. 3. Comparisons of (a) SO$_2$ to SO$_3$ conversion using two different mesh sizes in the bulk gas region and (b) local temperatures using different number of prism layers near the wall region.
Fig. 4. Comparisons of (a) SO$_2$ to SO$_3$ conversion using two different turbulence models at various engine loads and (b) averaged H$_2$SO$_4$ concentrations using different rate constants at various (i) engine loads and (ii) initial H$_2$O levels (by mass).
Fig. 5. Distributions of (a)-(d) species mass fraction and (e) equivalence ratio at 10 CAD ATDC.
Fig. 6. Local temperature-equivalence ratio distributions at (a) 10, (b) 30, (c) 50 and (d) 70 CAD ATDC for regions where the SO$_2$ to SO$_3$ conversion is significant.
Fig. 7. Temporal evolution of the (a) averaged SO$_2$ concentrations, (b) averaged SO$_3$ concentrations, (c) averaged H$_2$SO$_4$ concentrations and (d) SO$_2$ to SO$_3$ conversion for fuel sulphur contents of 0.5%, 1.0% and 2.0% by mass.
Fig. 8. Temporal evolution of the maximum (a) SO$_2$ and (b) H$_2$SO$_4$ mass fraction at the liner wall calculated using different chemical mechanisms and wall temperatures.
Fig. 9. Comparisons of (i) averaged in-cylinder pressure and (ii) SO₂ to SO₃ conversion for different (a) swirl velocity, (b) start of injection timing, (c) pressure at TDC as well as (d) initial H₂O mass fraction.
Fig. 10. Comparisons of atomic oxygen (O) evolutions in the (a) $U_{\theta,\text{max}} = 16$ m/s and (b) $U_{\theta,\text{max}} = 26$ m/s cases.
Fig. 11. Comparisons of (a) averaged in-cylinder pressure and (b) SO$_2$ to SO$_3$ conversion for the low load, high scavenge pressure case and the low load, low scavenge pressure case.
Fig. 12. Spatial distributions of the calculated dew point temperature on cylinder liner at (a) 6 (b) 10 and (c) 15 CAD ATDC.
Fig. 13. Local H$_2$SO$_4$ molar concentration at (a) 15, (b) 30, (c) 45 and (d) 60 CAD ATDC. The computational cells are grouped based on the local gas temperature.