A Physically-Based Equivalent Circuit Model for the Impedance of a LiFePO4/Graphite 26650 Cylindrical Cell

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Published in:
Journal of The Electrochemical Society

Link to article, DOI:
10.1149/2.1071709jes

Publication date:
2017

Document Version
Publisher's PDF, also known as Version of record

Link back to DTU Orbit

Citation (APA):
In this work an Equivalent Circuit Model (ECM) is developed and used to model impedance spectra measured on a commercial 26650 LiFePO4/Graphite cylindrical cell. The ECM is based on measurements and modeling of impedance spectra recorded separately on cathode (LiFePO4) and anode (Graphite) samples, harvested from the commercial cell. Modeling of the single-electrode impedance spectra provided information about the electronic and ionic resistance in the porous composite electrodes, as well as the solid state diffusion. Focused Ion Beam (FIB)/Scanning Electron Microscopy (SEM) of anode and cathode samples was used to make 3-D maps of the electrode microstructures and to obtain microstructural data for the ECM. The complementary analysis was crucial for the resolution of the single electrode impedance parameters and the proposal and validation of a new equivalent circuit used to model the full commercial battery impedance.

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and vacuum infiltrated with a silicon resin (Wacker Chemie) for 30 minutes to improve phase contrast between CB particles and pores as described by Ender et al.26 Subsequently the samples were infiltrated with epoxy resin to enable high-quality grinding and polishing of the sample.

FIB tomography and SEM imaging of the two electrode samples were carried out on a Zeiss 1540XB Crossbeam microscope, using a lateral E-T (Everhart-Thornley) detector and an In-lens detector. A 3D dataset was collected from each of the two electrodes. Table II shows the volume sizes of the two 3D datasets. A Gallium FIB slicing probe of 2nA was used to mill the LFP/CB electrode with a slice thickness of 27 nm. The slice thickness was calculated by measuring the progress of the milling front in each image during the stack alignment post processing step. For the Gr electrode the current for the Gallium FIB slicing probe was reduced to 1nA and the thickness of each slice was estimated to be 14 nm. The Gr electrode is softer than the LFP/CB electrode. For this reason the FIB current had to be reduced to enable high-quality imaging for the Gr electrode dataset.

The LFP particles in the positive electrode are much smaller than the Gr particles in the negative one. Thus, in order to perform an accurate image segmentation of LFP particles – to be used for 3D reconstruction and particle size distribution (PSD) analysis – it was necessary to collect higher-resolution images. The serial sectioning accurate image segmentation of LFP particles – to be used for 3D processing step. For the Gr electrode the current for the Gallium FIB slicing probe was reduced to 1nA and the thickness of each slice was estimated to be 14 nm. The Gr electrode is softer than the LFP/CB electrode. For this reason the FIB current had to be reduced to enable high-quality imaging for the Gr electrode dataset.

The tortuosity factor of the pore network $\tau$ was calculated using TauFactor.30 The program calculates $\tau$ by finite element modeling of steady state diffusive flow (electrical current/heat transfer/mass transport interchangeably) in a segmented network using normalized potential boundary conditions of 0 and 1 at opposing volume faces. This flow is then related to the flow through a fully open volume.

Electrochemical impedance spectroscopy.—EIS measurements were performed at room temperature in two-electrode configuration for the 26650CC cylindrical cell and in three-electrode setup for the LFP/CB1 and Gr1 electrodes, using a Biologic VMP3 with Pstat/Gstat boards. Two-electrode EIS measurements of the cylindrical cell were obtained in a frequency range from 10 kHz to 1 mHz (10 points per decade) at different SOC (state-of-charge) from 0% to 100% SOC in the voltage range 2.8–3.6 V. All spectra were measured at OCV after the cell had reached steady state defined by a change $< 5$ mV/h.

Three-electrode measurements for the LFP/CB1 and Gr1 electrodes were performed in a EL-CELL ECC-Combi, using lithium metal as counter and reference electrodes. The spectra were measured in the frequency range from 100 kHz to 1 mHz (10 points per decade), however for the LFP/CB1 electrode the impedance data recorded above 1 kHz presented an artifact (a “false” semicircle), hard to remove because of the difficulty to scratch LFP from the Al current collector without damaging it, and is therefore treated separately in the supplementary material. The measurements were performed at OCV after the electrode had reached 0% and 100% SOC using a nominal charge/discharge rate of 0.1 C, and after reaching steady state defined by a voltage change $< 5$ mV/h. The voltage cutoff at 0% and 100% SOC was defined as 0.5 V and 0.01 V for the anode, and 3.0 V and 3.7 V for the cathode.

### Table II. Volumes of collected datasets.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Volume (voxels) $X \times Y \times Z$</th>
<th>Volume ($\mu$m$^3$) $X \times Y \times Z$</th>
</tr>
</thead>
<tbody>
<tr>
<td>LFP/CB2</td>
<td>80 $\times$ 850 $\times$ 400</td>
<td>2.2 $\times$ 12.5 $\times$ 5.9</td>
</tr>
<tr>
<td>Gr2</td>
<td>328 $\times$ 750 $\times$ 150</td>
<td>4.4 $\times$ 36.6 $\times$ 7.3</td>
</tr>
</tbody>
</table>
Cathode equivalent circuit model.—The impedance results obtained from the LFP/CB1 electrode were modeled using the ECM shown in Fig. 2.

$L_0$ is an inductor. The modelled inductance is primarily related to the current leads of the test setup. $R_E$ is a resistor modelling the ionic resistance of the electrolyte. $Q_{el}$ is a constant phase element and $R_{Al}$ is a resistor, where the brackets indicate a parallel connection between $R_{Al}$ and $Q_{el}$, models the high-frequency part of the electrode impedance spectra associated with associated with Lithium ions traveling in the pores. The low-frequency part of the electrode impedance spectra is modeled with a generalized TLM for a porous electrode (Fig. 2b). The model assumes cylindrical pores with length $L$ filled with the electrolyte solution and oriented perpendicular to the current collector. $R_{ion,L}$ is the resistance associated with Lithium ions traveling in the pores.

The pores in the electrode are surrounded by carbon coated LFP particles mixed with carbon black particles. $R_{ct}$ is the resistance associated with electrons traveling in the surface coating and CB particles. The equivalent circuit element $\zeta_{cat}$ models the impedance of the electrode/electrolyte interface and includes the diffusion of lithium ions inside a LFP particle with radius $r$. $\zeta_{cat}$ consists of a charge transfer resistance $R_{ct}$ in parallel with a constant phase element $Q_{Al}$ to model the electronic resistivity along the electron pathway on the surface of the LFP particles, and through the CB network.

As previously mentioned the electronic resistance is often assumed to be much lower than the ionic resistance of the solution ($R_{ct} < R_{ion,L}$) resulting in a simplified TLM where $R_{ct}$ is omitted. The generalized TLM was used in this study as it reveals non-negligible $R_{ct}$ values. This is further detailed in the Results and Discussion sections.

The impedance of the generalized TLM model is:

$$Z_{TLM} = \frac{R_{ct} + R_{ion,L}}{R_{ct} + R_{ion,L}} \left( L + \frac{2\lambda_{TLM}}{\sinh (L/\lambda_{TLM})} \right)$$

$$+ \frac{\lambda_{TLM}}{R_{ct} + R_{ion,L}} \coth (L/\lambda_{TLM})$$

With:

$$\lambda_{TLM} = \frac{\zeta_{cat}}{(R_{ct} + R_{ion,L})}$$

As mentioned above the electrode/electrolyte interface (Fig. 2c) is modeled with the Randles circuit $\zeta_{cat}$ which includes the charge transfer resistance $R_{ct}$, a constant phase element (CPE) $Q$ and the general finite space Warburg element $W_{GF,1D}$. $W_{GF,1D}$ has the impedance:

$$Z_{W_{GF,1D}} = R_{w} \frac{\coth \left( j \omega \tau_{w} \right)}{\left( j \omega \tau_{w} \right)}$$

with the time constant:

$$\tau_{w} = \frac{r^2}{D}$$

$R_{w}$ is polarization resistance, $r$ is the particle radius, $n_w$ is an exponent (0 $< n_w < 0.5$) reflecting the degree of non-uniform diffusion, and $D$ is the diffusion coefficient of lithium ion within LiFePO$_4$.

The effective double layer capacitance $C_{dl}$ is calculated using the expression:

$$C_{dl} = \frac{Q}{\zeta_{cat}} \left( \frac{R_{ct}^{-1} + R_{ion,L}^{-1}}{(n-1)/n} \right)$$

where $Q$ is the CPE, $n$ the exponent of the CPE, $R_{ct}$ is the ohmic resistance and $R_{ion}$ the generic resistance associated with the CPE.

The units of $R_{ct}$ and $C_{dl}$ in the TLM model are respectively $\Omega \text{ cm}^2$ and $\text{F cm}^{-3}$. $R_{ct}$ and $C_{dl}$ values obtained from the modeling can be related to the geometrical electrode area (with the units $\Omega \text{ cm}^2$ and $\text{F cm}^{-3}$).
Fcm$^{-2}$) by division and multiplication respectively with the cylindrical pore length $L$ (expressed in cm). Here $L$ is set equal to the electrode thickness. The TLM neglects the ion diffusion driven by concentration gradient in the electrolyte phase, but only consider the ion migration, and the structural inhomogeneity.\textsuperscript{12}

Anode equivalent circuit model.—The impedance spectra measured on the Gr1 electrode were modeled using an ECM almost similar to the circuit used to model the LFP/CB1 electrode impedance (Fig. 3a). The $R_{el}(Q_{el})$ elements model the high frequency part of the impedance spectra. $R_{el}$ models the ionic resistance of the electrolyte, while the $Q_{el}$ element representing the combined copper current collector/electrode polarization.\textsuperscript{23} Similar to the model for the cathode, the mid- and low-frequency part of the anode spectra are modeled with a TLM for a porous electrode, however here the simplified version is used.\textsuperscript{36,32,33} (Fig. 3b), as the condition $R_{el} << R_{ion}$ is valid for the graphite electrode.\textsuperscript{44–46}

For a simplified TLM in with negligible $R_{el}$, Equation 1 reduces to:

$$Z_{TLM} = \lambda_{TLM} \frac{R_{ion,L} \coth(L/\lambda_{TLM})}{1}$$

where

$$\lambda_{TLM} = \frac{\zeta_{an}}{R_{ion,L}}$$

is different from $\zeta_{an}$. It is constituted by a resistor $R$ in series with a Randles circuit and in parallel with a constant phase element $Q$ (Fig. 3c).\textsuperscript{6} The element $\zeta_{an}$ is equivalent to the ECM proposed by Meyers et al. (Case 2)\textsuperscript{6} which describes the impedance response of a porous electrode, covered by a film (in this case the SEI layer illustrated in Fig. 3c). $R_{SEI}$ models the SEI layer resistance, while the film capacitance $C_{SEI}$ associated with it is calculated from $Q_{SEI}$ according to.\textsuperscript{10} The Randles circuit includes the charge transfer resistance $R_{ct}$, a constant phase element $Q_{ct}$, and the general finite space Warburg element with a two-dimensional diffusion path, $W_{WSF,2D}$ with the impedance:

$$Z_{WSF,2D} = \frac{R_{w} \left[\right.}{\left.\frac{\left(j \omega \tau_{w} \right)^{\nu} w}{\left(j \omega \tau_{w} \right)^{\nu} w}}$$

where $I_0$ and $I_1$ are modified zero- and first-order Bessel functions of the first kind.

Here a 2D Warburg finite space element with cylindrical geometry is used.\textsuperscript{15,47} This geometry describes a diffusion along the radial axis, usually associated with layered-structure electrodes, such as graphite, which allow two-dimensional lithium insertion.\textsuperscript{48}

Simulations of the impedance of the full cell/electrode/individual circuit elements, and complex nonlinear least squares fitting of the equivalent circuit models to the data was performed using software programmed in Python\textsuperscript{51} which relies on the scientific Python stack,\textsuperscript{50–52} and for the 1D/2D elements the library mpmath was used to provide higher precision complex floating-point arithmetic.\textsuperscript{53}

Tortuosity estimation from TLMs.—The ionic resistivity in the infiltrated pore with length $L$, $R_{ion,L}$ [2cm] calculated from the TLMs is correlated to the effective electrode pore tortuosity $\tau_{el}$ through the equation:

$$\tau_{el} = \sigma_{ion} R_{ion,L} \epsilon_{el}$$

where $\sigma_{ion}$ is the bulk ionic conductivity with the unit [Scm$^{-1}$], and $\epsilon_{el}$ is the electrode porosity.\textsuperscript{15} In our modeling work we used $\sigma_{ion} = 1.18 \cdot 10^{-2}$ Scm$^{-1}$, which is an average of the values reported for 1 M LiPF$_6$ in 1:1 EC/DMC (the electrolyte used for the single electrode tests) by Lombardo et al.\textsuperscript{45} and Porion et al.\textsuperscript{46}

Results

FIB/SEM tomography.—Figures 4 and 5 show respectively cross-section lateral E-T images after FIB milling of the LFP/CB2 and the Gr2 electrode. In the top region of the images it is possible to observe a very bright region, which is the sample surface after polishing. Looking inside the milled samples, current collector/electrode and electrode/electrolyte interfaces can be distinguished for both samples. Guidelines are shown in Fig. 4a to indicate how the interfaces extend into the sample. From Fig. 4a the cathode thickness is estimated to 65 m. Fig. 4b show a higher resolution image of the electrode/electrolyte interface. Inside the electrode, three different phases are distinguished: light gray LiFePO$_4$ particles, dark gray pores (infiltrated with silicon resin) and black CB particles. On the right side of the SEM image (Fig. 4a), where the electrolyte is supposed to be, there is a dark gray bulk of silicon resin with some LFP and CB particles, which probably detached during sample preparation.

Inside the Gr2 electrode (Fig. 5), only two phases can be distinguished: dark graphite particles and gray pores infiltrated with silicon

Figure 3. a) Equivalent circuit used to model the anode sample impedance spectra, b) Simplified Transmission Line Model without $R_{el}$ resembling the element TLM$_{an}$ in a), c) Meyers (Case 2)\textsuperscript{6} equivalent circuit used to model electrode/electrolyte interface with Li$^{+}$ diffusion (Warburg Finite Space element, $W_{WSF,2D}$) within a graphite particle. Meyers circuit resembles the element $\zeta_{an}$ in b).
resin. On the left side the copper/electrode interface is present, while on the right side the electrode/electrolyte interface is found. From the figure the electrode thickness is estimated to 35 µm. The darker gray bulk on the right is the epoxy resin, used for sample preparation, which yields a different brightness in the SEM images than silicon resin. The red rectangle indicates the region segmented for 3D reconstruction and PSD analysis.

Figure 6 shows a 3D reconstruction of the LFP/CB2 electrode/electrolyte interface and of the Gr2 electrode. In the cathode 3D reconstruction (Fig. 6a) the gray phase is the LiFePO₄, the black phase is the CB additive network, while the electrolyte infiltrated pores are transparent blue. All phases (separated in Figs. 7a, 7b, 7c) seem quite homogeneously distributed. In the anode 3D reconstruction (Fig. 6b) the orange region represents the copper current collector, the black particles are graphite agglomerates and the transparent blue region is the pores network infiltrated with the electrolyte. The two phases in the Gr2 electrode are shown in Figs. 7d, 7e.

Figs. 8a, 8b show respectively the PSD distributions for the three phases in the LFP/CB2 electrode and for the two phases in the Gr2 electrode. The average particle size for the active materials, Li₁₋ₓFePO₄ and LiₓC₆, is respectively 76 nm and 1096 nm. These values are implemented in the TLMs used to model the impedance spectra measured on the cylindrical cell and the electrode samples. Volume fraction values for all the phases are shown in Table III.

Fig. 9 shows the normalized 3D potential maps used in the pore tortuosity factor calculations. The calculated cathode pore tortuosity factor is 5.9, while the anode pore tortuosity factor is 24.8. From Fig. 9b it is evident that the volume analyzed for the anode is too small to be representative due to the big graphite particles and the single narrow pathway that connects the two sides of the volume. Thus the accuracy of the calculated anode tortuosity factor is very low. The tortuosity factor for a larger representative part of the electrode is expected to be significantly smaller.

**Galvanostatic cycling with potentiostatic limitation (GCPL).**—The 26650CC cell was cycled between 2.8 – 3.6 V as suggested from the commercial supplier, at a nominal C-rate of 0.1 C. The charge/discharge curve for 26650CC is shown in Fig. 10a (black line).

Figs. 10b and 10c show respectively the charge/discharge curves for the LFP/CB1 and Gr1 electrodes. The LFP/CB1 electrode is cycled between 3.0 – 3.7 V with a constant current of 330 µA, corresponding to a C-rate of 0.1. The charge/discharge curve shows a typical flat plateau of a Li₁₋ₓFePO₄ electrode at around 3.45 V (with 0 ≤ x ≤ 1). Note that the normalized charge/discharge capacity of LFP/CB1 is 10% higher than the normalized capacity of 26650CC. This matches with the typical 10% lithium loss for SEI layer formation on the graphite surfaces in the anode during the first charge/discharge cycle of the 26650CC. The Gr1 electrode was cycled between 0.01 V and 0.5 V, also at 330 µA (Fig. 10c) showing typical Li⁺ ion intercalation steps (with 0 ≤ x ≤ 1). Note that the normalized charge/discharge curve of 26650CC resembles well the voltage difference between the LFP/CB1 and Gr1 normalized charge/discharge curves, as shown by the green curve in Fig. 10a. This voltage difference does not match exactly the 0% and 100% SOC voltage cutoff for the 26650CC charge/discharge curves. This may again be explained by either the 10% capacity difference of the LFP/CB1 electrode.

To simplify the nomenclature, “LiFePO₄” refers to the Li₁₋ₓFePO₄ electrode at 0% SOC, and “FePO₄” denotes the Li₁₋ₓFePO₄ electrode at 100% SOC.

**EIS modelling of Li₁₋ₓFePO₄ electrode (three-electrode configuration).**—Fig. 11 shows the area-normalized EIS spectra measured for the LFP/CB1 electrode in the discharged (Figs. 11a, 11b, 11c, 11d) and charged state (Figs. 11e, 11f, 11g, 11h). Figs. 11a, 11c show respectively a Nyquist and a Bode plot of the EIS spectrum.

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**Figure 4.** a) FIB/SEM cross-section image of the LFP/CB2 electrode, collected with lateral E-T detector. On the top, guidelines are shown to distinguish Al/Electrode and Electrode/Electrolyte interfaces, b) High resolution FIB/SEM cross-section image of Electrode/Electrolyte interface, used for 3D reconstruction and PSD.

**Figure 5.** FIB/SEM cross-section image of the Gr2 electrode, obtained with a lateral E-T detector. The copper current collector is seen in the left part of the figure and the Electrode/Electrolyte interface, in the right part. The red rectangle indicates the region segmented for 3D reconstruction and PSD analysis.
Figure 6. 3D reconstructions of a) LFP/CB2 electrode/electrolyte (transparent blue) interface and b) Gr2 electrode/Cu current collector (orange) interface. The scale bar units are [μm].

Figure 7. 3D reconstruction of a) LFP, b) CB and c) pore networks in the LFP/CB2 electrode. 3D reconstruction of d) Graphite and e) pore networks in the Gr2 electrode.

Figure 8. Particle size distributions for a) LFP/CB2 and b) Gr2 electrodes.
Table III. Volume fraction and average size for the different phases.

<table>
<thead>
<tr>
<th>Phase</th>
<th>LFP/CB2</th>
<th>Gr2</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Volume Fraction [%]</td>
<td>Avg. size [nm]</td>
</tr>
<tr>
<td>Active Material</td>
<td>58</td>
<td>76</td>
</tr>
<tr>
<td>CB Additive</td>
<td>17</td>
<td>49</td>
</tr>
<tr>
<td>Pores</td>
<td>25</td>
<td>39</td>
</tr>
</tbody>
</table>

Figure 9. 3D surface renderings of the normalized potential maps used in the tortuosity factor calculations by TauFactor. a) LFP/CB2 electrode b) Gr2 electrode.

measured at OCV after discharging to 3.0 V and relaxation. Figs. 11e, 11g show a Nyquist and Bode plot of the EIS spectrum measured at OCV after changing the LFP electrode to 3.7 V and subsequent relaxation. Figs. 11b, 11f and the insets in Figs. 11c, 11g show a zoomed view of the high frequency regions of the spectra. The measured data is modeled (black lines) using the ECM described in Cathode Equivalent Circuit Model section highlighting two parts of model: The \((R_{al}Q_{al})\) part (red line) and the TLM\(_{an}\) part (blue line). The most interesting part of the modelling results are presented in Table IV and discussed in Discussion section. All the modeling results are presented in the supplementary information in Table S1. The relative residuals between measured and modeled spectra are shown in Figs. 11d, 11h.

Equivalent circuit modelling of \(Li_{x}C_{6}\) electrode (three-electrode configuration).—Fig. 12 shows the area-normalized EIS spectra measured for Gr1 in the delithiated (Figs. 12a, 12b, 12c, 12d) and lithiated form (Figs. 12e, 12f, 12g). Figs. 12a, 12c show Nyquist and Bode plot of the Gr1 spectrum measured at OCV after charging the electrode to 0.5 V followed by relaxation. Figs. 12e, 12f show Nyquist and Bode plots of the Gr1 spectrum measured after discharging the electrode to 0.01 V and after relaxation. Fig. 12b and the inset in Fig. 12c show a zoomed view of the high frequency region of the spectrum. The measured data is modeled (black lines) using the ECM described in Anode Equivalent Circuit Model section highlighting two parts of model: The \((R_{1}Q_{1})\) part (green line) and the TLM\(_{an}\) part (blue line). The most interesting part of the modelling results are presented in Table V and discussed in Discussion section. All the modeling results are reported in Table S2 in the supplementary information. The relative residuals between measured and modeled spectra are shown in Figs. 12d, 12g.

Equivalent circuit modelling of 26650CC (two-electrode configuration).—Impedance spectra obtained on the 26650CC were recorded at different SOC in charging and discharging mode. Fig. 13 shows the area-normalized EIS spectra measured for 26650CC at different SOC (dots), with the simulated curves corresponding to the best model fit (solid lines) for each spectrum. A full description of the equivalent circuit used to model the spectra and the fitting results are provided in Equivalent Circuit Description and EIS spectra fitting sections.

Discussion

Cathode impedance modelling: three-electrode configuration.—The Nyquist plots of LiFePO\(_4\) and FePO\(_4\) (Figs. 11b, 11f) consist of a small semicircle in the high frequency region between
Figure 11. a) Nyquist plot, b) Zoomed view, and c) Bode plot of the Li\(_{1-x}\)FePO\(_4\) electrode at 0% SOC (\(x = 0\)). e) Nyquist, f) Zoomed view, and g) Bode plot of the Li\(_{1-x}\)FePO\(_4\) electrode at 100% SOC (\(x = 1\)). d) and h) show relative residuals between model fit and measured data. Inset in c) and g) shows rescaled Bode plots to highlight the high-frequency part of the spectra.

1 kHz – 100 Hz and a low frequency branch characterized by an almost vertical tail in the charged state, and a less vertical tail in the discharged state.

\(R_{Al}\) models the contact resistance between the Aluminum foil and the Li\(_{1-x}\)FePO\(_4\)/CB network. From Table IV it is seen that the \(R_{Al}\) values change very little for the two different SOCs, in agreement with literature.\(^{14}\)

The high frequency side of the semicircle intersects with the x-axis at 12.0 \(\Omega\) cm\(^2\) and 8.0 \(\Omega\) cm\(^2\) for LiFePO\(_4\) and FePO\(_4\) respectively. However, because of the inductance and in particular due to the non-negligible electronic resistance (\(R_{el}\)), the electrolyte resistance (\(R_{E}\)) values are somewhat smaller: 11.2 \(\Omega\) cm\(^2\) and 7.4 \(\Omega\) cm\(^2\), respectively as presented in Table S1. When \(R_{el}\) is non-negligible relative to \(R_{ion,L}\) the generalized TLM\(_{cat}\) features a small ohmic contribution which shifts the starting point of the red semi-circle to the left in the Nyquist plot, Figs. 11b, 11f. If this ohmic contribution was placed on the left side of the red semi-circle it would be easier to see how the semi-circle contributes to the total spectrum, however the semi-circle is deliberately plotted with the TLM\(_{cat}\) shifted to the right side to highlight the small ohmic contribution from the TLM\(_{cat}\), as this contribution also affects the value of \(R_{E}\). The value of \(R_{E}\) is not expected to change with SOC and the change is possibly related to measurement uncertainties; the impedance measured above 1 kHz, as described before, presented an artifact and was therefore removed before the impedance was modeled. A “false” semicircle was observed and related to some effect of the non-complete scratching of active materials from the Al current collector. It was not observed on the graphite electrode where the active material was much softer and easier to scratch off.

<table>
<thead>
<tr>
<th>Element</th>
<th>(R_{Al}) ((\Omega) cm(^2))</th>
<th>(C_{Al}) (mF cm(^{-2}))</th>
<th>(R_{el}) ((\Omega) cm(^2))</th>
<th>(C_{el}) (F cm(^{-2}))</th>
<th>(D) (cm(^2) s(^{-1}))</th>
<th>(R_{ion,L}) ((\Omega) cm)</th>
<th>(R_{el}) ((\Omega) cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>LiFePO(_4)</td>
<td>2.7</td>
<td>0.16</td>
<td>34.9</td>
<td>0.51</td>
<td>4.4 (\times) 10(^{-13})</td>
<td>1596</td>
<td>109</td>
</tr>
<tr>
<td>FePO(_4)</td>
<td>2.3</td>
<td>0.24</td>
<td>8.2</td>
<td>0.48</td>
<td>1.8 (\times) 10(^{-12})</td>
<td>395</td>
<td>54</td>
</tr>
</tbody>
</table>

Table IV. Results from EIS fitting of Li\(_{1-x}\)FePO\(_4\) electrode.
The values used in the TLMcat for the electrode thickness $L$ and the particle radius $r$ are 65 $\mu$m and 38 nm, respectively. These values were obtained from the presented FIB/SEM analysis and PSD calculation.

Diffusion of $\text{Li}^+$ ions through the liquid electrolyte in the electrode pores results in a 45° slope in the beginning of the TLMcat curve. The length of the part of the TLMcat curve resembling a line with a 45° slope is determined by $R_{\text{ion,L}}$ and the thickness of the electrode. Once a $\text{Li}^+$ ion has traveled through a pore and reached a coated LFP particle, it will adsorb (insert) and diffuse (together with an electron, forming a polaron) into the bulk of the LFP particle. This is modelled by $\zeta_{\text{cat}}$ and results in a semicircle followed by a 45° curve terminating in a capacitive-like response as seen in Figs. 11a, 11b, 11e, and 11f. The semicircle is the result of charge transfer resistance, $R_{ct}$, of $\text{Li}^+$ at the particle/electrolyte interface and double layer capacitance $C_{dl}$, in parallel, calculated from the CPE used to model it. The 45° line followed by a capacitive-like curve corresponds to the finite space Warburg element $W_{\text{GFS,1D}}$ which represents diffusion of $\text{Li}^+$ ions in the electrode network, until all the active material is lithiated/delithiated.

The fitted values from the TLMcat show that $R_{ct}$ is not negligible compared to $R_{\text{ion,L}}$. Both resistances in the pore and the electrode are observed to decrease when the electrode is charged and mainly consists of FePO$_4$.$\text{Li}_{1-x}$FePO$_4$ particles are known to be subjected to expansion/contraction with cycling. When the electrode is completely delithiated, FePO$_4$ particles have a small volume and consequently the pore volume have increased, resulting in a lower $R_{\text{ion,L}}$. $R_{ct}$ depends on the CB network tortuosity which changes due to particle movements during lithiation/delithiation process. $R_{ct}$ is observed to be significantly lower at 100% SOC, in agreement with literature.

### Table V. Results from EIS fitting of $\text{Li}_x\text{C}_6$ electrode.

<table>
<thead>
<tr>
<th>simplified transmission line</th>
<th>Meyers element</th>
<th>Pore</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_1 Q_1$ element</td>
<td>$R_{\text{SEI}}$ ($\Omega$ cm$^2$)</td>
<td>C$_{\text{SEI}}$ (mF cm$^{-2}$)</td>
</tr>
<tr>
<td>R$_1$ ($\Omega$ cm$^2$)</td>
<td>C$_1$ (mF cm$^{-2}$)</td>
<td>32.3</td>
</tr>
<tr>
<td>Li$_6$</td>
<td>8.3</td>
<td>0.39</td>
</tr>
</tbody>
</table>

Figure 12. a) Nyquist, b) Zoomed view, and c) Bode plot of the Li$_x$C$_6$ electrode at 0% SOC ($x = 0$). (e) Nyquist, and f) Bode plot of the Li$_x$C$_6$ electrode at 100% SOC ($x = 1$). d) and g) show relative residuals between model fit and measured data. Inset in c) and f) shows rescaled Bode plots to highlight the high-frequency part of the spectra.
The Nyquist plot of the impedance spectra for Gr1 (Figs. 12a, 12b, and 12c) consists of a small semicircle in the high frequency region, between 100 kHz – 10 kHz, a second bigger semicircle in the mid-frequency range (100 Hz – 10 Hz) and – similar to the LFP/CB1 electrode – a low frequency branch (at frequencies lower than 1 Hz) characterized by an almost vertical tail, in the charged state, and a diffusive tail in the discharged state. Parameter values obtained from the modelling are given in Table V.

The high frequency side of the impedance curve does not intersect with the x-axis, so the electrolyte resistance \( R_{E} \) is obtained from the modeling and was 12.9 \( \Omega \) cm\(^2\) and 12.5 \( \Omega \) cm\(^2\) for C and LiC\(_6\) respectively, see Table S2. The first semicircle \( (R_{SEI}Q_{SEI}) \) observed at high frequencies (higher than 10 kHz) can be assigned to the interface between the copper current collector and/or the porous graphite anode or the graphite particle/particle contact resistance, with \( R_{C} \) and \( Q_{C} \) representing contact resistance and the double layer capacitance at these interfaces, respectfully. The value obtained for \( R_{C} \) is expected to be significantly lower at 100% SOC than at 0% SOC. The double layer capacitance at this interface \( C_{D} \) is around three orders of magnitude smaller than \( C_{M} \) at the cathode (Table IV). This is probably due to the smaller specific surface area in the anode: the average graphite particle diameter is around 1.1 \( \mu \)m, while CB grains in the positive electrode – a low frequency branch (at frequencies lower than 1 Hz) is associated with the Randles element of a SEI and \( Q_{SEI} \) placed in parallel which are part of \( \zeta_{an} \) inside the Simplified Transmission Line Model (TLM\(_{an}\)) for a porous electrode. The low frequency branch \((< 1 \text{ Hz})\) is associated with the Randles element of \( \zeta_{an} \), inside TLM\(_{an}\). The values used for \( L \) and \( r \) are respectively 35 \( \mu \)m and 548 nm, obtained from the FIB/SEM analysis and PSD calculation. The fitting values for \( R_{SEI} \) and \( R_{C} \) are highest for C in the delithiated form, Similarly \( D \) is highest for C in the delithiated form which could indicate that Li\(^+\) ions travel faster through the graphene planes when they are delithiated. The lithium diffusivity in the anode is observed to be around 2 orders of magnitude larger than the lithium diffusivity in the cathode.

\( R_{E} \) is extremely low and could be neglected, enabling the use of a Simplified Transmission Line Model \((R_{SEI}Q_{SEI})\) for the graphite electrode. This is because the entire anode is made of C which is highly conductive. On the contrary the cathode is a mixed LiFePO\(_4/\)CB electrode with a significant electronic resistance.
13 and 15, respectively, and putting them in series results in a model with 23 variables. The analysis of the single electrode impedance spectra plays a crucial role for the successful modeling of the full battery since it enables us to determine the parameters that are used as guesses in the final ECM. This allows an accurate modeling of the measured 26650CC spectra. It should be noted that the single electrode models only provided input for the 0% and 100% SOC spectra. Values obtained at intermediate SOCs are obtained from the full model.

The $R_{\text{AlQAl}}$ elements model the high-frequency region. $R_E$ models the ionic resistance of the electrolyte, while $R_{\text{AlQAl}}$ represents the aluminum/cathode polarization observed in the LFP/CB electrode in the frequency range 1 kHz – 100 Hz. The $R_{\text{AlQAl}}$ element, previously used to model the particle/particle contact in the Gr electrode, is not included in the total circuit since this process occurs at relative high frequency (> 10 kHz), leading to a reduction in the number of model variables. Above ~ 1 kHz the 26650CC is dominated by inductance and possibly beginning skin-effects or other processes yielding also an increased real resistance. This contributes to the reduction.

TLM_{an} and TLM_{cat} model the mid- and low-frequency regions of the spectra. More specifically the mid-frequency region (100 Hz – 10 Hz) represents the SEI layer which covers each graphite particle in the anode and is described by the $R_{\text{SEI}}$ and $Q_{\text{SEI}}$ elements placed in parallel inside $\varsigma_{\text{an}}$ (Fig. 3c). The low-frequency branch (< 1 Hz) is ascribed to the Li insertion or intercalation process at the interface (Li$_{1-x}$FePO$_4$ or Li$_x$C$_6$) and is modelled by the Randles circuits in $\varsigma_{\text{an}}$ and $\varsigma_{\text{cat}}$ (Figs. 2c and 3c). The results of $R_{\text{SEI}}$ and $C_{\text{SEI}}$ obtained from TLM_{an} are normalized for both geometrical surface area and internal surface area and reported in Table VI and in the supplementary information.

Table VI and the supplementary information also report normalized values for $R_d$ (from TLM_{an}) and $R_{\text{ct}}$, $C_{\text{dl}}$ (calculated from CPE according to Eq. 5), $D$ and $R_{\text{ion,L}}$ from both TLMs.

EIS spectra fitting.—The normalized EIS spectra for 26650CC measured at OCV after relaxation at 0, 50 and 100% SOC, after removal of the wire inductance, are shown in Fig. 15. Figs. 15a, 15b, 15c show Nyquist plots of the different EIS spectra, including best-fits to the data using the model described in Equivalent Circuit Description section, and the zoomed views of the high frequency regions in the insets. Figs. 15d, 15e, 15f show zoomed view of the correspondent Bode plots, including best-fits of the model to the data. Relevant values obtained by EIS modelling at the different SOCs are reported in Table VI and values for selected resistors are plotted in Figure 16. All parameter values are reported in Tables S3 and S4 in the supplementary information. The relative residuals and the higher zoomed views of the Nyquist plots are shown in Fig. S2 in the supplementary information.

The red semicircle seen in Fig 15 shows the impedance for the $(R_{\text{AlQAl}})$ element assigned to the interface between the Aluminum current collector and the porous cathode. As reported in Table VI, $R_{\text{Al}}$ is slightly dependent of SOC. However, the values obtained for $R_{\text{Al}}$ and $C_{\text{Al}}$ are comparable to the values obtained for the same variables from the single-electrode Li$_{1-x}$FePO$_4$/CB EIS modelling (Table IV).
The yellow dotted line shows the TLM_{in} impedance. From the fitted values, $R_{SEI}$ decreases upon charging (Fig. 16a) in agreement with the Gr1 modeling results. In both cases $R_{SEI}$ reduces by around 60% when going from the discharged state to the charged state but for the single-electrode EIS spectra the magnitude of this decrease is in agreement with the values obtained from the single-electrode EIS spectra the magnitude of $R_{SEI}$ is observed to slightly raise with SOC.

As seen from the fitted values (Table VI and Fig. 16b) $R_{ct}$ and $D$ decreases with increasing SOC (or with lithiation of graphite), which is in agreement with the values obtained from the single-electrode impedance modelling. $R_{con,l}$ is observed to slightly raise with SOC and dramatically increase in the fully lithiated graphite, because of particles expansion an pores volume reduction.

The blue dotted line represents the TLM_{in} impedance. The fitted values in Table VI, and Figs. 16c, 16d show how $R_{ct}$, $R_{con,l}$ and $R_{rd}$ decreases with increasing SOC (or with delithiation of LFP), in agreement with the values obtained from the single-electrode impedance modelling. $D$ is observed to be higher in the fully delithiated state.

From a careful analysis of Fig. 15 is possible to notice that the graphite impedance is characterized in the low frequency region by a capacitive vertical tail, while LFP shows a diffusive tail at 0% SOC (Fig. 15a), and vice versa at 100% (Fig. 15c). This perfectly resembles the behavior observed for the single electrode impedance spectra in Figs. 11 and 12. The values for Li diffusion $D$ obtained from modeling the 26650CC spectrum are found to be around $10^{-12}, 10^{-13} \text{cm}^2\text{s}^{-1}$ for LFP electrode and about 2–3 orders of magnitude larger in graphite (Fig. 16b), in agreement with previous findings. However larger particles size in graphite is not negligible and time constant $\tau_{e}$ is calculated using Eq. 4 for both electrodes. $\tau_{e}$ is found equal to 24, 61 and 6 $\text{s}$ for LFP at 0, 50 and 100% SOC respectively, and equal to 7, 59 and 120 $\text{s}$ for graphite at 0, 50 and 100% SOC respectively. From $\tau_{e}$ comparison is evident how the Li insertion process is diffusion-controlled by LFP when the battery is discharged, by Graphite when charged and there is a shared contribution at intermediate SOC.

**Conclusions**

In this work a commercial 26650 cylindrical LiFePO4/Graphite battery was disassembled and the two electrodes were characterized individually by charge/discharge curves and electrochemical impedance spectroscopy (EIS) in a three-electrode setup, and by FIB/SEM tomography. Two different equivalent circuits were used to model the cathode and anode impedance. The circuits included a transmission line model (TLM) for a porous electrode, which, among other parameters, involves pore length $L$ and particle radius $r$. The values for $L$ and $r$ were obtained from the FIB/SEM tomography. A thorough analysis was conducted of the parameter values obtained from fitting the individual electrode impedances. The analysis enabled us to propose a new equivalent circuit, which includes two TLMs in series, to model the full commercial battery impedance. The parameter values obtained from fitting the circuit impedance to the full battery impedance were discussed and validated against the parameter values obtained from fitting the individual electrode impedance spectra.

From fitting the ECM to the commercial battery impedance, values were obtained for the ionic resistance $R_{ion,L}$ of Li$^+$ ions diffusing into the electrodes pores, electron resistance $R_{el}$ in the porous electrodes and lithium diffusivity in the active materials in the electrodes. By comparing the obtained values with the ones obtained from single electrode modeling, it was demonstrated that several of these param-

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Table VI. Results from EIS fitting of 26650CC. a. charging mode, b. discharging mode.

<table>
<thead>
<tr>
<th>RA,QA element</th>
<th>Transmission line graphite</th>
<th>Meyers element</th>
<th>Pores</th>
<th>Transmission line LiFePO4</th>
<th>RAl, CAl</th>
<th>RSEI, CSEI</th>
<th>Rct, Cdl</th>
<th>D</th>
<th>$R_{con,l}$, $R_{el}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_{SEI}$ ($\Omega$/cm²)</td>
<td>$C_{SEI}$ (mF/cm²)</td>
<td>$R_{ct}$ (\Omega)</td>
<td>$C_{dl}$ (F/cm²)</td>
<td>$D$ (cm²/s)</td>
<td>$R_{con,l}$ ($\Omega$/cm²)</td>
<td>$R_{el}$ ($\Omega$/cm²)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0%</td>
<td>1.83</td>
<td>0.14</td>
<td>8.08</td>
<td>0.46</td>
<td>33.1</td>
<td>0.39</td>
<td>4.4 $\times$ 10⁻¹⁰</td>
<td>247</td>
<td>22.3</td>
</tr>
<tr>
<td>12.5%</td>
<td>1.74</td>
<td>0.22</td>
<td>5.24</td>
<td>0.40</td>
<td>28.9</td>
<td>0.72</td>
<td>5.9 $\times$ 10⁻¹¹</td>
<td>357</td>
<td>12.0</td>
</tr>
<tr>
<td>25%</td>
<td>1.74</td>
<td>0.19</td>
<td>5.01</td>
<td>0.37</td>
<td>26.0</td>
<td>0.81</td>
<td>5.3 $\times$ 10⁻¹¹</td>
<td>397</td>
<td>12.3</td>
</tr>
<tr>
<td>37.5%</td>
<td>1.72</td>
<td>0.20</td>
<td>4.78</td>
<td>0.37</td>
<td>23.4</td>
<td>0.77</td>
<td>4.7 $\times$ 10⁻¹¹</td>
<td>357</td>
<td>11.0</td>
</tr>
<tr>
<td>50%</td>
<td>1.74</td>
<td>0.20</td>
<td>4.77</td>
<td>0.36</td>
<td>23.6</td>
<td>0.78</td>
<td>4.8 $\times$ 10⁻¹¹</td>
<td>321</td>
<td>11.9</td>
</tr>
<tr>
<td>62.5%</td>
<td>1.72</td>
<td>0.18</td>
<td>4.76</td>
<td>0.36</td>
<td>25.4</td>
<td>0.77</td>
<td>5.3 $\times$ 10⁻¹¹</td>
<td>357</td>
<td>10.8</td>
</tr>
<tr>
<td>75%</td>
<td>1.75</td>
<td>0.24</td>
<td>4.31</td>
<td>0.40</td>
<td>23.4</td>
<td>0.65</td>
<td>5.3 $\times$ 10⁻¹¹</td>
<td>357</td>
<td>10.8</td>
</tr>
<tr>
<td>87.5%</td>
<td>1.75</td>
<td>0.24</td>
<td>4.25</td>
<td>0.42</td>
<td>24.0</td>
<td>0.68</td>
<td>5.8 $\times$ 10⁻¹¹</td>
<td>397</td>
<td>10.5</td>
</tr>
<tr>
<td>100%</td>
<td>1.69</td>
<td>0.25</td>
<td>4.10</td>
<td>0.78</td>
<td>23.9</td>
<td>0.24</td>
<td>2.7 $\times$ 10⁻¹¹</td>
<td>901</td>
<td>5.9</td>
</tr>
</tbody>
</table>

a) 100% 1.69 0.25 3.10 0.78 23.9 0.24 2.7 $\times$ 10⁻¹¹ 901
b) 100% 1.69 0.25 3.10 0.78 23.9 0.24 2.7 $\times$ 10⁻¹¹ 901

Figure 16. Fitted values as function of SOC.


25. Y. Zhao et al., “Advances in new cathode material LiFePO4 for lithium-ion batteries,” Synth. Met., 162(13–14), 1315 (2012).


