Experimental Results and Integrated Modeling of Bacterial Growth on an Insoluble Hydrophobic Substrate (Phenanthrene)

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ABSTRACT: Metabolism of a low-solubility substrate is limited by dissolution and availability and can hardly be determined. We developed a numerical model for simultaneously calculating dissolution kinetics of such substrates and their metabolism and microbial growth (Monod kinetics with decay) and tested it with three aerobic phenanthrene (PHE) degraders: Novosphingobium pentaromativorans US6-1, Sphingomonas sp. EPAS05S, and Sphingobium yanoikuyae B1. PHE was present as microcrystals, providing non-limiting conditions for growth. Total PHE and protein concentration were tracked over 6−12 days. The model was fitted to the test results for the rates of dissolution, metabolism, and growth. The strains showed similar efficiency, with $V_{\text{max}}$ values of $12−18$ g dw $^{-1}$ d$^{-1}$, yields of $0.21$ g g$^{-1}$, maximum growth rates of $2.5−3.8$ d$^{-1}$, and decay rates of $0.04−0.05$ d$^{-1}$. Sensitivity analysis with the model shows that (i) retention in crystals or NAPLs or by sequestration competes with biodegradation, (ii) bacterial growth conditions (dissolution flux and resulting chemical activity of substrate) are more relevant for the final state of the system than the initial biomass, and (iii) the desorption flux regulates the turnover in the presence of solid-state, sequestered (aged), or NAPL substrate sources.

INTRODUCTION

Polycyclic aromatic hydrocarbons (PAH) are hydrophobic compounds with a strong tendency toward absorption on surfaces in aqueous systems that undergo no or only slow decomposition in the environment.1 PAH are metabolized by a large number of enzymes in bacteria, fungi, and algae and by cytochrome P-450 monooxygenases in eukaryotic cells.2 Cometabolic transformation of these compounds is found in all organisms, whereas complete metabolism leading to biomass and carbon dioxide is described only for bacteria.3 Microbial degradation of PAH is well-documented in numerous reviews.1,3−13 In comparison to the general published results on PAH biodegradation, data on the growth kinetics of PAH-degrading organisms are rare.14−18 The biodegradation of the low-soluble PAH is often limited by the diffusive flux to the microbes, and this is the reason for the pseudolinear growth of degraders often found in experiments.19,20 Therefore, reliable data for kinetic parameters such as growth rates ($\mu$) and half-saturation constants ($K_s$) are not easily available for PAH-degrading strains and cannot be derived solely from growth curves.21 The Best equation, which balances diffusive flux to the bacterium with metabolic flux in a steady state, has been applied in order to describe the kinetics of metabolism and mass transfer from solids to bacteria.15,18,19

Recently, a model for fast and slow adsorption (“aging”) was fused with a biodegradation model that calculates degradation and growth kinetics of microbes.22 The model includes dissolution from a nonaqueous phase (source term), adsorption with two different rates, and Michaelis−Menten kinetics for metabolism (sink term) with coupled Monod kinetics plus a decay term for bacterial growth and carbon turnover for the simulation of biotic formation of nonextractable residues.23 This leads to a set of ordinary non-linear differential equations that are solved numerically.

In two recent studies, degradation of phenanthrene (PHE) in soil suspension with strain Sphingomonas sp. 10-1 was investigated, whereby the flux kinetics was inversely modeled with a reduced version of the above model.24,25 The experimental setup with high bacterial numbers and low PHE concentrations led to non-growth conditions where only decay rate constants $b$ could be calibrated. Therefore, very little kinetic data for various PAH degrader bacteria has been

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available until now for the prediction of PAH turnover with this unified model of sorption and metabolism.

The goals of the present work were (i) to study the kinetics of aerobic PHE degradation by three known and well-described bacteria (one with genome sequenced) and their resulting growth at varying substrate concentrations, (ii) to provide the real growth and yield parameters for these bacteria by a combination of experiments and model calibration, and (iii) to determine and interpret differences in the kinetic parameters for dissolution and metabolism.

## MATERIALS AND METHODS

### Strains and Culture Conditions

The three strains _Novosphingobium pentaromativorans_ US6-1, _Sphingomonas_ sp. EPS05, and _Sphingobium yanoukayae_ B1 were enriched from various PAH contaminated sites and are well-described (Table 1). They were chosen on the basis of their rapid PHE degradation plus growth kinetics in liquid cultures.

The strains were precultivated on mineral medium (MM) with vitamins (Brunner, DSMZ no. 462). The MM consists of Na$_2$HPO$_4$ 2.44 g L$^{-1}$, KH$_2$PO$_4$ 1.52 g L$^{-1}$, (NH$_4$)$_2$SO$_4$ 0.5 g L$^{-1}$, MgSO$_4$·7H$_2$O 0.2 g L$^{-1}$, CaCl$_2$·2H$_2$O 0.05 g L$^{-1}$, 10 mL L$^{-1}$ trace element solution SL-4 (containing per L: EDTA 0.5 g, FeSO$_4$·7H$_2$O 0.2 g), and 100 mL L$^{-1}$ trace element solution SL-6 (containing per L: ZnSO$_4$·7H$_2$O 0.1 g, MnCl$_2$·4H$_2$O 0.03 g, H$_2$BO$_3$ 0.3 g, CoCl$_2$·6H$_2$O 0.2 g, CuCl$_2$·2H$_2$O 0.01 g, NiCl$_2$·6H$_2$O 0.02 g, Na$_2$MoO$_4$·2H$_2$O 0.03 g)), and 2.5 mL L$^{-1}$ vitamin solution (containing per L: p-amino benzoate 10 mg, biotin 2 mg, nicotinic acid 20 mg, thiamine-HCl·2H$_2$O 10 mg, Ca-pantothenate 5 mg, pyridoxamine 50 mg, vitamin B$_2$, 20 mg).

PHE (98% purity, Sigma-Aldrich, Saint Louis, USA) was provided as the sole source of carbon and energy by adding 5, 12.5, 25, 50, 100, or 200 μL of PHE dissolved in acetone (4 mg mL$^{-1}$) to the cultivation flasks, shaking the vials in order to cover the bottom surface. The acetone was then allowed to evaporate fully in order to cover the inside with a PHE layer prior to adding the MM, resulting in final medium concentrations of 10, 25, 50, 100, 200, and 400 mg L$^{-1}$. This method, as described by Mutnuri et al., is intended to enable nonlimited growth on PHE.

### Experimental Setup

In order to overcome the inhomogeneities of PAH cultures with suspension concentrations above water solubility, a setup of destructively sampled small vials (10 mL with 2 mL MM) was chosen (mini-culture approach). Vials containing 1800 μL of MM were allowed to equilibrate overnight and were inoculated to an initial optical density of 0.01 at 560 nm by adding 200 μL of a preculture grown under similar conditions to late exponential phase. Each vessel was completely sampled at the respective sampling points and analyzed in total. The experiment was performed in six replicates for each concentration and time point in order to provide triplicates for separate quantification of biomass and PHE. The mini-cultures were incubated at 30 °C, shaken at 135 rpm, and harvested as follows: for _N. pentaromativorans_, after 0, 4, 8, 12, 24, 36, 48, and 144 h of incubation for initial 10, 25, and 50 mg L$^{-1}$ PHE concentrations and after 0, 6, 12, 24, 48, 96, 144, 192, and 288 h for initial 100, 200, and 400 mg L$^{-1}$ PHE concentrations; and for _S. yanoukayae_ and _Sphingomonas_ sp., after 0, 4, 8, 12, 24, 30, 36, 48, and 96 h for initial 10, 25, and 50 mg L$^{-1}$ PHE concentrations and after 0, 6, 12, 24, 48, 72, 96, 192, and 288 h for initial 100, 200, and 400 mg L$^{-1}$ PHE concentrations.

### Protein Analysis

Protein concentration was measured photometrically in 96 well plates applying the Bradford protein assay (Bio-Rad Protein Assay, Bio-Rad Laboratories, Munich, Germany) using a Victor2 Multilabel Counter (1420, Wallac Oy, Turku, Finland). A 160 μL culture sample was thoroughly mixed with 40 μL undiluted Bradford dye solution and quantified in triplicates against a bovine serum albumin (298% purity, Carl Roth, Karlsruhe, Germany) as the calibration standard.

### PAH Analysis

For tracking the PAH consumption the mini-cultures were extracted two times with 2 mL of hexane, with fluorine (98% purity, Sigma-Aldrich, Saint Louis, USA) as internal standard. PHE was quantified by means of a gas chromatograph (7890A, Agilent Technologies, Santa Clara, California) equipped with a BPX5 column (30 m × 0.25 mm i.d., 0.25 μm film, SGE Analytical Science, Melbourne, Australia) and coupled to a mass spectrometer (5975C, Agilent Technologies, Santa Clara, California). The GC oven temperature was programmed to initial 40 °C (2 min hold), then heat to 180 °C (2 min hold) at 40 °C min$^{-1}$, to 240 °C (2 min hold) at 5 °C min$^{-1}$, and to a final temperature of 300 °C (5 min hold) at 15 °C min$^{-1}$ with a helium flow of 1.5 mL min$^{-1}$ (based on ref 28). The injector was set to 280 °C. The MS was operated in the electron impact ionization mode at 70 eV. The source temperature was set to 230 °C, the quadrupole temperature to 150 °C. Full scans were acquired in the m/z range 40–500.

### Model

The model consists of a set of ordinary differential equations (spatial dependencies were not occurring) with

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<th>Table 1. Phenanthrene-Degrading Strains Used in the Present Experiments</th>
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chemical and bacterial mass as state variables. Combined modeling was carried out for the dissolution of PHE from microcrystals into water and for microbial biodegradation. Dissolution, i.e., the diffusive flux from PHE phase into water was considered as

$$\frac{dm_{ph}}{dt} = PA_{ph}(S - C_W)$$

(1)

where $m_{ph}$ (g) is the PHE mass, $t$ (d) is time, $P$ (m d$^{-1}$) is the permeability or mass transfer coefficient, $A_{ph}$ (m$^2$) is the surface area of PHE phase, $S$ (g m$^{-3}$) is water solubility of PHE, and $C_W$ (g m$^{-3}$) is the freely dissolved concentration (synonym chemical activity) of PHE in water.

The metabolism of substrate by microbes is given by the Michaelis–Menten equation:

$$\frac{dm_{M}}{dt} = \frac{u_{max}C_W}{K_M + C_W}X = \nu X$$

(2)

where $u_{max}$ is the maximum removal rate (g substrate g$^{-1}$ bacteria d$^{-1}$), $K_M$ is the half-saturation constant (g substrate m$^{-3}$), and $X$ (g) is the microbial mass.$^{29,30}$ Microbial growth is described by the Monod equation (plus decay term):

$$\frac{dX}{dt} = \left(\frac{dm_{M}}{dt} - Xr\right)Y$$

(3)

where $Y$ (g bacteria g$^{-1}$ substrate) is yield, and $r$ (g substrate g$^{-1}$ bacteria d$^{-1}$) is maintenance given as $r = b/Y$, with $b$ (d$^{-1}$) being a first-order rate constant describing the decline of microbial activity with time; the term $dm_{M}/dt$ (g substrate d$^{-1}$) describes metabolic flux, and the term $X$ times $r$ (g substrate d$^{-1}$) describes microbial maintenance needs.$^{15,18,31}$ These

Figure 1. Experiments with *N. pentaromativorans*: phenanthrene concentration in suspension $C_{sus}$ (− − , straight lines, diamonds) and protein concentration $C_X$ (− - - , dashed lines, circles), measured (data points) versus modeled (curves). Experiments with nominal initial phenanthrene concentrations: (a) $C_0 = 10$ mg L$^{-1}$, (b) $C_0 = 25$ mg L$^{-1}$, (c) $C_0 = 50$ mg L$^{-1}$, (d) $C_0 = 100$ mg L$^{-1}$, (e) $C_0 = 200$ mg L$^{-1}$, (f) $C_0 = 400$ mg L$^{-1}$. Error bars indicate minimum and maximum (3 replicates).
calculations are based upon the assumption that only freely
dissolved chemicals are subject to microbial degradation. For
converting from protein mass to microbial mass, a fraction
\( f_{\text{m,prot}} \) of 0.55 g protein g\(^{-1}\) bacteria (dw) was considered.\(^{32}\)

The mass of substrate dissolved in water (index W) is
increased by dissolution of solid PHE (index ph), and
decreased by metabolism (index M):

\[
\frac{dm_W}{dt} = \frac{dm_{ph}}{dt} - \frac{dm_M}{dt}
\]  

(4)

The freely dissolved concentration \( C_W \) (mg L\(^{-1}\)) is \( m_W/V \),
where \( V \) (L or m\(^3\)) is volume. The total PHE concentration in
suspension is \( C_{\text{tot}} = (m_{ph} + m_W)/V \). Experimentally observed
lag phases were taken into consideration by introducing an
inhibition factor \( f_{\text{inh}} \) (described in Supporting Information).

All differential equations were solved numerically, both by an
Euler one-step solution scheme realized as a Microsoft Excel
spreadsheet and by the ODE45 solver (Runge–Kutta scheme
with variable step size) within MATLAB R2013b. The correct
implementation of the model was quality-controlled by
comparing both numerical solutions and by verification against
analytical (steady-state) solutions offered by the Best equation.

**Determination of Kinetic Parameters.** In the experiments,
only microbial mass \( X \) and substrate mass \( m \) can be observed directly. The substrate metabolized by the microbes is
related to bacterial growth via the yield \( Y \) (g bacteria g\(^{-1}\)
substrate); it is used by microbes both for actual growth (with
rate \( \mu \) in d\(^{-1}\)) and for maintenance needs \( r \) (g substrate g\(^{-1}\)
bacteria d\(^{-1}\)) of microbes decaying with rate \( b \) (d\(^{-1}\)).\(^{33}\) The
experimentally observable growth rate constant is bacterial mass
versus time per bacteria, \( dX/dt \), and can be obtained from
eq 3 as

\[
\frac{dX}{X \, dt} = \frac{\nu_{\text{max}} C_W}{K_M + C_W} Y - rY = \nu Y - rY = \mu - b
\]  

(5)
By rearranging, the “true” yield $Y$ (g bacteria g$^{-1}$ substrate) follows

$$Y = \frac{\mu - b}{v} $$

(6)

The experimentally derived yield $Y_{exp}$ is the ratio of observed growth $dX/dt$ to change of substrate mass $dm_{M}/dt$:

$$Y_{exp} = \frac{dX}{dm_{M}} $$

(7)

This “experimental yield” is different from the true yield and varies with concentration due to the (concentration-independent) maintenance. Due to the complexity of the coupled model approach, the rapid change of numerical values, and the multitude of model parameters, least-squares fitting of predictions to the measured data was performed with manual expert adjustment of model parameters in an iterative procedure. Statistical data on the curve fits (root-mean-square errors, mean absolute errors, and coefficients of determination) are provided in Supplementary Table S12 for all simulations. In order to improve accuracy prior to determining $Y$, the death rate constant $b$ was found first from experiments with low substrate concentrations. The parameters $v_{max}$, $K_{M}$, $Y$, and $b$ were then determined iteratively for each bacterial strain until a combination was found that is optimal for all sets of experiments (initial nominal concentrations 10, 25, 50, 100, 200, and 400 mg L$^{-1}$). For an assessment of the dissolution kinetics, $f_{x0}$ and $k_{mg}$ (affecting the surface area of the PHE phase and thus the dissolution rate parameter values; see Supporting Information) were varied in order to explain the experimental observations. At low initial concentrations, a delay of metabolism (lag phase) was observed, and mass balance equations were adjusted with $f_{inhibit}$ (leading to an adjustment of inhibition as a function of time).

### RESULTS

The strains of bacteria applied in the experiments are characterized in detail as phenanthrene-degrading bacteria (Table 1). However, this characterization includes mostly physiologic and genetic descriptions and does not provide the basic growth and turnover kinetic data. The measured and simulated PHE suspension concentrations (left axis) and bacterial mass (right axis) of the experiments with S. yanoikuyae are shown in Figure 1. At all initial concentrations (10, 25, 50, 100, 200, and 400 mg L$^{-1}$), PHE is degraded virtually completely within the experimental period ($t = 6$ d for $C_{0} \leq 50$ mg L$^{-1}$ and $t = 12$ d for $C_{0} \geq 100$ mg L$^{-1}$) and faster at lower initial concentration. Rapid bacterial growth was observed from the increase of protein at the first day and up to 2 days with higher initial concentration, followed by decay after depletion of the substrate. Figure 2 shows the change of the parameters over time, i.e., measured and simulated PHE consumption (degradation flux) $dm_{M}/dt$ (g d$^{-1}$) plus (calculated) maintenance needs $rX$ (g d$^{-1}$) on the left axis and the bacterial growth rate constant $dX/dt/X$ (d$^{-1}$) on the right axis for the same experiments. Substrate consumption and growth are very closely related, peaking at the same time. With higher initial concentration, both peak later, and the substrate consumption is higher. In all samples, growth declines and growth rates become negative (below the line indicating no-growth conditions) as soon as the substrate is depleted. The fitted curves are within the measured range or very close (see Supplementary Table S12 for details on the statistics).

The measured and simulated PHE suspension concentrations (left axis) and protein concentrations (right axis) of the experiments with Sphingomonas sp. EPA505 are shown in Supplementary Figure S11. The pattern is similar to the results in Figure 1, but the scatter of experimental data points is considerably higher. This is accompanied by less successful model fits (e.g., Supplementary Figure S11e). Supplementary Figure S12 again shows the change of substrate and bacteria with time. At low initial concentrations, in particular for 25 mg L$^{-1}$ (Supplementary Figure S12b), the substrate loss $dm/dt$ is higher and the growth is faster than for strain N. pentaromativorans. No advantage of Sphingomonas sp. is seen in experiments with high initial substrate concentrations (Supplementary Figure S1f vs Figure 2f).

Finally, the results for strain S. yanoikuyae are shown in Supplementary Figures S13 and 4. This strain does not degrade PHE completely at the low initial concentrations (Supplementary Figure S13a and b). Due to adsorption of the microbes to the crystals, the results for the protein concentration have a high scatter but seem to indicate no or little increase at these low concentrations, except for the first time period ($t = 0$ to 0.17 d). The protein concentrations measured at $t = 0$ are distinctly lower than for the following time periods. The fit of bacterial mass (Supplementary Figure S13) is thus not very good. Starting with these low measured initial protein concentrations, the model does not reproduce the higher protein concentrations some hours later. Supplementary Figure S14 shows the change of substrate and bacterial mass with time for strain S. yanoikuyae. Loss of mass quickly falls to zero, and growth becomes negative for the low initial concentrations (10 and 25 mg L$^{-1}$, Supplementary Figure S14a and b). At higher initial concentrations, metabolism and growth do not differ significantly from those of the two other strains.

All strains showed the typical growth curves with lag phases and exponential growth behavior instead of the limited growth mostly observed in previous experiments. The calibration of the model can yield these kinetic data and can also indicate differences in hydrophobic substrate mobilization. All strains showed yields and half-saturation constants within a similar range during growth on PHE (Table 2), which indicates similar metabolic pathways, but this is also due in part to the insensitivity of some data ($K_{M}$). Best curve fits for this scenario were obtained with $K_{M} = 0.1$ mg L$^{-1}$, $Y = 0.21$ g bact dw g$^{-1}$, $b = 0.04$ to 0.05 d$^{-1}$, $v_{max} = 12$ g g$^{-1}$ bact d$^{-1}$, both for strains N. pentaromativorans and Sphingomonas sp. EPA505, whereas for strain S. yanoikuyae a higher $v_{max}$ of 18 g g$^{-1}$ bact d$^{-1}$ resulted from the curve fits (Table 2).

### DISCUSSION

Growth experiments with bacteria plus water-insoluble and/or solid-state substrates are mostly biased by transport limitations and thus by limited bioavailability.20 For water-soluble substrates without mass-transfer limitations, such data are typically acquired using continuous chemostat cultures. However, this approach is not applicable to hydrophobic solid-state substrates with low water solubility due to the limitations of mass transfer at higher growth rates generally leading to limited non-exponential growth.19 Therefore, in the present work we provide a modeling approach to determine the real growth and yield parameters from turnover data measured.
Table 2. Model Parameters, Symbols, and Units

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Fitted Parameters—Monod

(8)

2. Model Parameters, Symbols, and Units

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Sphingomonas sp. EPA505

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Sphingobium yanoikuyae

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In batch experiments with PHE as model PAH substrate and several degrading strains.

For comparison of the strains, Figure 3 shows the substrate metabolism flux and the growth rate constants of the three degrader strains versus initial substrate concentrations. Figure 3a–c represents the maximum fit and experimental value seen during the whole simulation period. The measured maximum loss and growth were typically very early in the experiment, therefore the results for \( t = 0.5 \) d (Figure 3d–f) do not differ significantly. Measured metabolism and growth at \( t = 1 \) d (Figure 3g–i) is lower than at \( t = 0.5 \) d for all strains. At \( t = 1 \) d, substrate depletion at lower initial concentration has progressed, and negative growth rates are seen for the two initially fast-growing strains (Sphingomonas sp. EPA505 and S. yanoikuyae), accompanied by zero loss of PHE mass (Figure 3h and i). The no-growth concentration can be found from setting \( dx/dt \) in eq 5 to zero

\[
C_{W,\text{no growth}} = \frac{bK_{\text{M}}}{\mu_{\text{max}} - b}
\]

and is close to \( 2 \) \( \mu g \) L\(^{-1}\) (corresponding to 10 nM). Such low values are quickly reached, due to vivid metabolism. Plots of \( C_W \) versus time are shown in Supplementary Figures SI5–7.

The provided data show that the apparent growth and degradation rates are only slightly different from the modeled ones and differ only slightly between the strains. Observed and modeled degradation flux (\( dm/dt \)) increases at higher initial concentration of PHE, \( C_0 \) most pronouncedly for strain N. pentaromativorans and S. yanoikuyae, whereas for strain Sphingomonas sp. EPA505 there is only little change for \( C_0 \) above 200 mg L\(^{-1}\). Microbial growth rates (\( dx/(dtX) \)) show a peak at \( C_0 \) of 50 or 100 mg L\(^{-1}\) and are highest for strain S. yanoikuyae, followed by Sphingomonas sp. EPA505 and N. pentaromativorans (the maximum growth rates occur earlier than \( t = 0.5 \) d). There is an obvious underestimation of growth (and, to some extent, also of metabolism) of the strains Sphingomonas sp. EPA505 and S. yanoikuyae at substrate concentrations <100 mg L\(^{-1}\) (Supplementary Figure SI1b,c). This leads to the speculation that at the lowest substrate concentrations, these bacteria have mechanisms to make the substrate more available. Also, in Supplementary Figures SI1b,c and SI3a–d, measured protein concentrations are higher than the calculated ones. However, there is also considerable scatter in the data.

In the experiments with Sphingomonas sp. EPA505 and S. yanoikuyae the substrate metabolism rate \( dm/dt \) is far from linearly increasing with initial concentration. The comparison to the growth \( dx/(dtX) \) leads to the conclusion that this decline cannot be explained by the half-saturation constant \( K_{\text{M}} \) but is due to the dissolution kinetics (see Supporting Information) and may also be due to toxic effects. All strains already reach their maximum growth at low initial substrate concentrations (though, as Figures 2 and Supplementary Figures SI2 and 4 show, only for a short time period), with little increase or even decrease for higher substrate concentrations.

Uptake from Solid State. Growth of bacteria with water-insoluble and/or solid-state substrates can be biased by transport limitations and thus by limited bioavailability (see Supporting Information for discussion of dissolution kinetics). In real contaminated sites, sorption processes to solid matter and dissolution from NAPLs additionally limit the mass transfer and cause residual non-degradable concentrations. It is generally assumed that the transport and bacterial uptake of compounds occurs only via the water phase, and the model thus calculates this way (eq 1). There are some indications that transport may also occur directly from the organic phase or crystal to the cell membrane, e.g., Mycobacteria. However, the presented model describes the transfer and the following turnover processes sufficiently without considering direct transfer. The dissolution kinetics derived from the fit of parameters indicates differences between the strains, but these are small at least for dissolution during the first days when maximum metabolism occurs (variation of \( f_{A_0} \) less than a factor 2; see Supporting Information). An interesting feature of the equations is, however, that direct uptake from crystals would not change the kinetics: the driver for uptake and metabolism is the chemical activity in solution, and the maximum activity that can be achieved is equivalent to the water solubility. This is at the same time the activity of the pure solid phase in contact to water. According to the equations, it is not the concentration of substrate in the dissolved state that limits degradation but the flux of substrate to the microbes. Thus, in order to increase their substrate supply, bacteria have no need to metabolize directly solid-phase substrate, for example, by pinocytotic endocytosis. The right strategy for microbes to increase the flux...
to their enzymes is to increase the dissolution kinetics. This can be achieved by various means, e.g., increase of surface or mobilization by exudates or biosurfactants or perhaps by mycolic acids. This theoretical conclusion is confirmed for alkanes by experiments of Yoshida et al. (cited in ref 20) that compare the growth rates of Candida tropicalis on liquid and vapor n-hexadecane in two different fermenters. In both cases, the chemical activity is at maximum (but either in gas phase or in liquid phase), and the specific growth rate of the microorganisms does not differ. The conclusion of the authors was that microbial hydrocarbon uptake by direct contact with the liquid hydrocarbon is negligible.

Comparison to Other Findings. Using solid anthracene as substrate for Mycobacterium sp. LB501T, Wick et al. fitted a yield of 15,500 mg protein mol⁻¹ h⁻¹ for suspended bacteria and of 19,200 mg protein mol⁻¹ h⁻¹ for total biomass. With molar mass M of anthracene and 0.55 g protein g⁻¹ bacteria (dw) this corresponds to a yield Y of 0.158 and 0.196 g biomass g⁻¹ substrate d⁻¹. A decay rate b of 0.017 d⁻¹ was derived from the zero-growth phase of batches and by using total biomass, while calculations for only the crystal-bound biomass and non-linear model fit gave 0.048 d⁻¹, corresponding to a maintenance need r of 0.245–0.303 g g⁻¹ d⁻¹. The other parameters were $K_M = 2.4 \times 10^{-4}$ mol m⁻³ (0.0428 mg L⁻¹) and $v_{max} = 7.8 \times 10^{-6}$ mol mg⁻¹ protein h⁻¹ (18.4 g substrate g⁻¹ biomass d⁻¹), from which $\mu_{max}$ values of 2.9–3.59 d⁻¹ result. In contrast, the experimentally determined $\mu_{max}$ from growth in the exponential state was only 0.864 d⁻¹. As in our study, growth and metabolism of the test organisms were limited by the substrate flux to the organisms. Comparison of these values for anthracene with those from our study for PHE (Table 2, $K_M = 0.1$ mg L⁻¹, $v_{max} = 12$ to 18 g g⁻¹ d⁻¹, $Y = 0.21$ g g⁻¹, b = 0.04 –0.05 d⁻¹) makes obvious that the data from the non-linear fits of the different experiments agree with each other quite closely. This is remarkable because it means that all four strains, including Mycobacterium sp. LB501T, have very similar kinetic properties. In particular, S. yanoikuyae with $v_{max}$ values of 18 g g⁻¹ bacter d⁻¹ shows growth and metabolism kinetics almost identical that of to Mycobacterium sp. LB501T. S. yanoikuyae was isolated from a marine contaminated site. The values for $K_M$ differ more, but $K_M$ is rather insensitive, and moderate variations of this parameter do not change the simulation results. However, the $K_M$ values derived here are also surprisingly similar to the half-saturation constants of Aitken

Figure 3. Degradation flux $\frac{dM}{dt}$ (−−−) and microbial growth rate $\frac{dX}{dt}/X$ (−−−−−−) as a function of the initial concentration $C_0$ for the three investigated strains. Measured (data points) vs modeled (curves). (a−c) Maximum values, (d−f) values at time $t = 0.5$, (g−i) values at $t = 1$ day. Strains: (a,d,g) = N. pentaromativorans; (b,e,h) = Sphingomonas sp. EPA505; (c,f,i) = S. yanoikuyae. Error bars indicate minimum and maximum (3 replicates).
et al., who found for 11 isolates from PAH contaminated sites $K_M$ values between 0.014 and 0.38 mg L$^{-1}$, with median at 0.155 mg L$^{-1}$.38

Ortega-Calvo and Gschwend analyzed biodegradation experiments where oxygen supply and desorption of PAH from black carbon materials were limiting pyrene degradation by *Mycobacterium gilvum*.37 Low levels of oxygen were sufficient for removal. The measured pyrene concentrations reached a quasi-steady-state balancing desorption and removal. The kinetics followed Michaelis–Menten and was determined by fit of a calibrated mass-balance model. $K_M$ values obtained were a factor of 100 lower than for PHE (6 nM, corresponding to $1.2 \times 10^{-3}$ mg L$^{-1}$).

In general, the $K_M$ values of around 0.1 mg L$^{-1}$ determined in the present study by inverse modeling of the PHE degradation are in the range of other PAH14,18 but are 2–3 orders of magnitude higher than for other monoaromatic substrates.38 The yields of 0.21 g biomass g substrate$^{-1}$ observed are in the range of values observed for other aromatic hydrocarbons.38

**Other Model Approaches.** The Best equation15,39,15,18,19 balances diffusive flux to the bacterium with metabolic flux; both can limit substrate degradation. A shortcoming of the concept is that it requires steady-state, i.e., equal dissolution and metabolism kinetics constant over time. The dynamic model described above can mimic these conditions by starting with initial conditions at steady-state and then yields identical results. This was used to mathematically verify the model and its implementation.

An elegant and comparatively simple equation for the kinetics of microbial degradation of poorly soluble organics was developed and applied by Yassine et al.20 The model assumes that biodegradation takes place in the aqueous phase and that, like here, growth kinetics follow Monod kinetics with decay term. The approach was applied to rather insoluble petroleum diesel alkanes (C10–C24) and fatty acid methyl esters. Thus, it was also assumed that the dissolution is fast compared to biodegradation, and aqueous concentrations were set to constant (at solubility). This allowed an analytical solution of the equation system.

Turnover kinetics was influenced by the poor water solubility of the substrate and probably below maximum. We found an actual turnover of only 0.24 to 0.48 g g$^{-1}$ d$^{-1}$, which is low, presumably because substrate solubility was much lower than the half-saturation concentration. Maximum stoichiometric yield coefficients $Y$ were about 1.6 g g$^{-1}$. The decay rate constants $b$ calculated from controls were at 0.023 and 0.026 d$^{-1}$, which is about half of the values found in our study and by Wick et al.18 Yassine et al.20 pointed out that conventional Monod-type kinetic models for poorly soluble organic compounds are of little practical value; actual utilization rates may be orders of magnitude lower because these substrates do not dissolve in sufficient quantities. A couple of other earlier model approaches were reviewed in Yassine et al.20 and we refer to this.

**Limitations.** The approach presented in this study has limitations. First of all, the experimental design was intended to create nonlimited growth conditions for the bacterial strains by providing sufficient substrate. Due to the hydrophobicity of PHE, microcrystals were used that dissolve over time. This obviously succeeded in providing sufficient substrate for unlimited growth of all strains, but only for the first period of the experiments. After about 1 day, bacterial numbers had increased so much, and smaller crystals had dissolved, so that substrate availability nevertheless became limiting. Another disadvantage of the approach was that the use of crystals does not lead to controlled, constant concentrations in dissolved state, and (small) variations in the dissolution kinetics of crystals may also have appeared. Additional parameters for the dissolution kinetics had to be introduced, which led to additional uncertainty and provided some problems in the calibration.

For the model approach, only two experimental parameters could directly be observed: total substrate concentration in suspension and protein density. These two variables were also the state variables of the model. Of the several input parameters into the model (Table 2), some were unknown and had to be fitted by model calibration. The kinetic parameters of the bacteria, i.e., $v_{max}$, $Y$, and $b$, were also the target parameters of the study, and no independent control or direct measurement is feasible. The parameter $K_M$ affects metabolism and growth rates only at low concentrations and was rather insensitive for the simulations. Two additional parameters were necessary for improved simulation of the observations, which we consider to describe the dissolution kinetics ($f_{sol}$, $k_{deg}$). In principle, the observed reduction of metabolism during the progress of the experiment could as well have been an effect of the accumulation of metabolites, leading to inhibition of the strains and thus less substrate turnover and reduced bacterial growth. However, with our analytical approach we did not find any evidence for primary oxidation products of PHE, which may be toxic.

The model was applied to well-mixed vessels without spatial differences. Subsequently, a set of ordinary differential equations was solved. In real environmental systems, such as soils and sediments, conditions are not homogeneous and not well-mixed, and such spatial dependencies may play a crucial role.40 Advection processes (water flow) may also impact the compound transport to the organisms. Moreover, in real systems, parameters affecting the growth such as water content and temperature are variable and different from the conditions in laboratory. This may lead to suboptimal growth conditions, and the growth rates determined in laboratory experiments are perhaps not realistic for such environmental conditions.

**Implications of the Model.** In the present work we provide new and improved experimental kinetic data for three Gram-negative PHE-degrading strains well-known from the literature, isolated from various contaminated sites. The new dynamic model for desorption and metabolism describes mass transfer of the substrate, taking into consideration chemical activity, sorption and dissolution processes, metabolism, and growth as well as cell maintenance and decay processes simultaneously in non-steady state.

Moreover, provided that the equations describe the kinetic data correctly and the initial conditions of the system are known, model simulations may predict the residual concentrations. The approach is also valid for compounds that are generally biodegradable with formation of biomass; even the special case of cometabolic degradation can be integrated. The model offers distinct prospective power for the assessment of residual non-degradable concentrations to be expected after various treatment options of contaminated soils and remediation measures. We plan to describe this in a future article in detail.

A surprising outcome of the simulation is that variations of the initial amount and of kinetic data of the degrader bacteria do not strongly affect the overall turnover. As long as the
dissolved concentration is sufficiently high the degrader strains will grow, until a balance between dissolution of substrate and bacterial metabolism is reached. This balance was reached within a day or less in all set-ups. Thus, for longer time periods, the amount of PAH ultimately degraded depends more on the ad/desorption rates than on the Monod and Michaelis–Menten parameters.

**ASSOCIATED CONTENT**

**Supporting Information**

More detailed equations for crystal surface and initial lag phases in the mathematical model; details of the determination of kinetic parameters, statistical data on curve fits, and the discussion of dissolution kinetics. This material is available free of charge via the Internet at http://pubs.acs.org.

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