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Gordon, Mark; Hill, David J.

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Global Transient Stability and Voltage Regulation for Multimachine Power Systems

Mark Gordon, Member, IEEE, David J. Hill, Fellow, IEEE

Abstract—This paper addresses simultaneously the major fundamental and difficult issues of nonlinearity, uncertainty, dimensionality and globality to derive performance enhancing power system stability control. The main focus is on simultaneous enhancement of transient stability and voltage regulation of power systems. This problem arises from the practical concern that both frequency and voltage control are important indices of power system control and operation but they are ascribed to different stages of system operation, i.e. the transient and post transient period respectively. The Direct Feedback Linearization (DFL) technique together with the robust control theory has been further developed and applied to design nonlinear excitation compensators which selectively eliminate system nonlinearities and deal with plant uncertainties and interconnections between generators. Then the so called global control law is implemented to coordinate transient stabilizer and voltage regulator for each machine. Digital simulation studies show that global control scheme achieves unified transient stability and voltage regulation in the presence of parametric uncertainties and significant sudden changes in the network topology.

I. INTRODUCTION

SYSTEM stability is the most important issue for power systems; if stability is lost, network collapse may occur with devastating economical losses and power grid damages, see [1], [2]. Traditionally, transient (angle) instability has been the dominant stability problem. With the continuing growth of power system interconnections and the increased operation in highly stressed conditions, different forms of system instability have emerged. For example frequency stability, inter-area modes of oscillations and voltage stability have become great concerns [3]. A clear understanding of different types of instability and how they are interrelated is most important for the satisfactory control design and operation of power systems.

The work presented in this paper is motivated by the occurrence of system instability and blackouts which may be preventable by use of advanced control techniques. Lack of properly automated and coordinated power system controllers to take immediate performance enhancing actions against system events has been recognized as one of the contributing factors for recent power system blackouts [1], [2], [4].

Power systems are modeled as complex, nonlinear and highly structured systems. It is well known that the generator excitation control system can provide one of the most cost effective ways to stabilize power systems. Conventional power system controls primarily deal with small disturbances about an operating point. This type of control can suffer performance degeneracy and in fact linear controllers may even destabilize the system if the operating point of the power system is changed away from the equilibrium point at which the approximate linearization is realized [5]. Control methods for handling system-wide large disturbance problems need to be developed, particularly ones which concern power system nonlinearity and unforeseen circumstances leading to a large sudden operating point deviations. To address this issue, this paper applies DFL as a flexible and structure preserving nonlinear control technique, see [6]–[8]. This technique simply uses the Implicit Function Theorem to selectively eliminate system nonlinearities and the well known nonlinear control approach based on the geometric coordinate transformation is not needed. Considering the effect of plant parametric uncertainties and power system interconnections, the robust control technique is further developed in this paper and applied to ensure the stability of the DFL compensated system. Only the bounds of uncertain parameters need to be specified and the exact time varying network parameters need not to be known.

Much effort has gone over the years into the mathematical modeling and market restructuring of large power systems and, to a lesser extent, systematic stability control design. Development of stability control from both control theory and practical point of view continues to be an interesting subject. The major areas of concern are transient stability, oscillations and voltage stability/regulation. Particular features which motivate the work in this paper are:

- power system nonlinearity, uncertainty and dimensionality in the design of stability controllers;
- the interplay between angle and voltage behavior;
- problems of control coordination;

The main concern is the operation of the generator in var control mode while the power system stabilizer (PSS) is in operation. In [6], [9] we have discussed detrimental stabilizing effects through classical root locus analysis of the linearized power system model. A concern for coordination is a practical problem, which has become a theoretical problem in control theory. How to achieve satisfactory stability performance is an important issue and this motivates the topic of global control [10]. Transient stability and voltage regulation are both important properties of power system stability control, but they relate to different stages of system operation, i.e. the transient period and the post fault period. Different behavior of nonlinear power systems in different operating regions requires different control objectives and therefore different controllers need to be activated or switched to under varying operating conditions. One method to implement such control utilizes
membership functions pioneered in the well known Takagi-Sugeno design which effectively provides smooth switching, see [11]. Global control is the weighted average of the local controllers, where the weights are provided by the operating region membership functions [12]. In this paper we design and investigate the impact of different sensitivity indicators needed to quantify the switching sequence between transient stability controller and voltage regulator in the transient period based on the global control framework.

A three machine example system is used to employ the effectiveness of the proposed scheme. Simulation results show that the proposed nonlinear global control framework can simultaneously enhance the transient stability and voltage regulation of the power system regardless of the network parameters and sudden large operating point changes.

II. POWER SYSTEM MODEL

The one line diagram of the example power system model is given in Fig.1. In this model, the generator is modeled as a voltage behind the direct axis transient reactance where the angle of the voltage coincides with the mechanical angle of the synchronously rotating reference frame. The network, including loads, has been reduced to an internal bus representation. The electromechanical dynamical model of the \textit{i\textsuperscript{th}} machine can be written as follows, [13]:

\begin{align}
\dot{\omega}_i &= \omega_i(t) - \omega_i(t_0) \\
\omega_i &= \frac{D_i}{2H} (\omega_i(t) - \omega_i(t_0)) - \frac{\omega_i(t_0)}{2H} (P_{el} - P_{mi}) \\
\dot{e}'_{qi} &= \frac{1}{T_{doq}} (E_{qi} - \Delta x_{di} \dot{i}_{di} - e'_{qi})
\end{align}

with the following electrical equations:

\begin{align}
P_{el} &= e'_{qi} g_{ii} + \sum_{j=1}^{n} (e'_{qi} e'_{qj} b_{ij} \sin \delta_{ij} + e'_{qi} e'_{qj} b_{ij} \cos \delta_{ij}) \\
&= e'_{qi} i_{qi} \\
i_{di} &= e'_{qi} b_{ii} + \sum_{j=1}^{n} (e'_{qi} g_{ij} \sin \delta_{ij} - e'_{qi} b_{ij} \cos \delta_{ij}) \\
i_{qi} &= e'_{qi} g_{ii} + \sum_{j=1}^{n} (e'_{qi} g_{ij} \cos \delta_{ij} - e'_{qi} b_{ij} \sin \delta_{ij}) \\
V_{t1}(t) &= \sqrt{e'_{qi}^2 - 2e'_{qi} x_{di}^2 i_{di} + x_{di}^2 (i_{di}^2 + i_{qi}^2)}
\end{align}

Elements $g_{ij} + j b_{ij}$ represent the admittance between buses \textit{i} and \textit{j}, $g_{ii} + j b_{ii}$ is the self admittance of bus \textit{i} in p.u.. The notation used is standard. For description of variables, readers are referred to [13], [14]. The system parameters used in the simulation are [15]:

\begin{align*}
x_{d1} &= 1.863; x'_{d1} = 0.257; x_{d2} = 2.36; x'_{d2} = 0.319; \\
x_{t1} &= 0.129; x_{t2} = 0.11; x_{L1-2} = 0.275; \\
x_{L1-3} &= 0.53; x_{L2-3} = 0.63; D_1 = 5; \\
H_1 &= 4; T_{do1} = 6.9; \omega_0 = 100\pi; D_2 = 3; \\
H_2 &= 5.1; T_{do2} = 7.96; P_{load} = 0.4, Q_{load} = 0.4;
\end{align*}

and the physical limit of the generator field voltage is taken as $\max|E_{f(1,2)}| \leq 6$. The fault we consider in the simulation is a symmetrical 3-phase short circuit fault that occurs on one of the transmission circuits between generator 1 and 2. The fault sequence is given as follows:

Stage 1: The system is in a pre fault steady state;
Stage 2: A fault occurs at $t = t_0$;
Stage 3: The fault is removed by opening circuit breakers of the faulted line at $t = t_1$;
Stage 4: The system is in a post fault state;

The fault location is indexed by a positive constant $\lambda$ which is the fraction of the line to the left of the fault. For the purpose of simulation the fault location is taken as $\lambda = 0.25$.

III. NONLINEAR COMPENSATOR DESIGN

From the model given in Section II, it can be seen that the power system model is highly nonlinear. To eliminate nonlinearities we use DFL technique to design a nonlinear compensator through the excitation loop of the generator to achieve transient stability and voltage regulation. The DFL technique has been shown to offer considerable flexibility in deriving nonlinear compensating controls for power systems, for example see [6]-[8] and the references therein. The procedure presented here follows the idea by Wang et al. [15] in deriving nonlinear compensating control for multimachine power systems but we consider different input in the control structure. The nonlinear control design presented derives control structures for transient stability and voltage regulation in the presence of electrical loads where the interconnections and coordination of generators is taken into account.

A. Nonlinear Transient Stability Controller

To eliminate nonlinearities in (1)-(3), $e'_{qi}$ in the generator electrical dynamics can be eliminated by selecting

\begin{equation}
v_{f1} = T_{do1} \dot{e}'_{qi}
\end{equation}

and similarly for the \textit{j\textsuperscript{th}} machine:

\begin{align}
v_{fj} &= T_{doj} \dot{e}'_{qj} \\
&= K_j \delta_j = K_j [\Delta \delta_j \Delta \omega_j \Delta P_{ej}]^T
\end{align}

Fig. 1. Three machine example power system
Differentiating the active power equation (4) we obtain:

\[ \dot{P}_{ei} = 2e_{qi}g_{qi}\dot{e}_{qi} + \sum_{j=1}^{n} (e_{qj}b_{ij}\sin\delta_{ij} + e_{qj}g_{ij}\cos\delta_{ij})\dot{e}_{qi} \]
\[ + \sum_{j=1}^{n} (e_{qj}b_{ij}\sin\delta_{ij} + e_{qj}g_{ij}\cos\delta_{ij})\dot{e}_{qj} \]
\[ + \sum_{j=1}^{n} (e_{qi}e_{qj}b_{ij}\cos\delta_{ij} - e_{qi}e_{qj}g_{ij}\sin\delta_{ij})\dot{\omega}_{ij} \]

and substituting (8) and (10) into (11) we obtain

\[ \dot{P}_{ei} = \frac{1}{T_{do)i}}f_1(t)v_{fi} + f_2(t)\Delta\omega_i \]
\[ + q_1(t)\Delta\delta_i + q_2(t)\Delta\omega_j + q_3(t)\Delta P_{ej} \]

where \( v_{fi} \) is the new nonlinear input of the excitation loop of the \( i^{th} \) machine, \( f_1(t) \) and \( f_2(t) \) are dependent on operating conditions, and similarly \( q_1(t)\Delta\delta_i, q_2(t)\Delta\omega_j, q_3\Delta P_{ej} \) represent the effects of remote dynamics of the \( j^{th} \) generator on the \( i^{th} \) generator. Therefore, the nonlinear power system model (1)-(3) has been compensated into:

\[ \dot{\delta}_i = \Delta\omega_i \]
\[ \dot{\omega}_i = -\frac{D_i}{2H_i}\Delta\omega_i - \frac{\omega_{0i}}{2H_i}\Delta P_{ei} \]
\[ \dot{P}_{ei} = \frac{1}{T_{do)i}}f_1(t)v_{fi} + f_2(t)\Delta\omega_i \]
\[ + q_1(t)\Delta\delta_i + q_2(t)\Delta\omega_j + q_3(t)\Delta P_{ej} \]

From (8) we obtain the DFL nonlinear compensating excitation control law for machine \( i \) as

\[ E_{fi} = v_{fi} + \Delta x_{di}i_{di} + \frac{P_{ei}}{i_{qi}} \]

Designing a controller for \( E_{fi} \) to stabilize the original model is equivalent to designing a controller \( v_{fi} \) to stabilize the DFL compensated plant. Since (13)-(15) contains time varying parameters and interconnections which are not canceled by the DFL compensating law (8), robust control technique is presented and applied in Section IV to design the robust transient stability controller for the DFL compensated system.

B. Nonlinear Voltage Regulator Design

The drawback of the transient stability control is that the feedback of rotor angle \( \delta_i \) is involved, whereas the generator terminal voltage \( V_{ti} \) is not included in the feedback control law. It is important to make nonlinear excitation control practical by preventing \( V_{ti} \) from excessive variations. It has been recognized [7], [10], [16], [17] that voltage regulation can be expected by the feedback of \( \omega_i, P_{ei} \) and \( V_{ti} \). Therefore if a DFL compensated model can be represented by

\[ x_i = [\Delta\omega_i \Delta P_{ei} \Delta V_{ti}]^T \]

an effective feedback control law

\[ v_{fi} = T_{do)i}^*e_{qi} \]
\[ = K_i x_i = [k_{\omega_i}\Delta\omega_i k_{P_{ei}}\Delta P_{ei} k_{V_{ti}}\Delta V_{ti}]^T \]

can be developed to enhance system stability and achieve voltage regulation. Similarly, for the \( j^{th} \) machine we have

\[ v_{fj} = T_{doj}^*e_{qj} \]
\[ = K_j x_j = [k_{\omega_j}\Delta\omega_j k_{P_{ej}}\Delta P_{ej} k_{V_{tj}}\Delta V_{tj}]^T \]

To develop a new DFL compensated voltage controller, we differentiate (7):

\[ \dot{V}_{ti}(t) = \frac{1}{V_{ti}}E_{fi} = \frac{1}{V_{ti}}(e_{qj}x_{di}i_{di} + (x_{di}^2i_{di} - e_{qi}x_{di}^2)b_{ij}) \]
\[ + f_2(t)\Delta\omega_i + f_2(t)\Delta\omega_j + q_3(t)\Delta P_{ej} \]
\[ \times \sum_{j=1}^{n} (e_{qj}g_{ij}\cos\delta_{ij} + e_{qj}b_{ij}\sin\delta_{ij}) \]
\[ + q_1(t)\Delta\delta_i + q_2(t)\Delta\omega_j + q_3(t)\Delta P_{ej} \]
\[ \times \sum_{j=1}^{n} (g_{ij}\sin\delta_{ij} - b_{ij}\cos\delta_{ij}) \]
\[ + q_1(t)\Delta\delta_i + q_2(t)\Delta\omega_j + q_3(t)\Delta P_{ej} \]

and substituting (18) and (21) into (22) we obtain

\[ \dot{V}_{ti}(t) = \frac{1}{T_{do)i}}\dot{f}_1(t)v_{fi} + \frac{\dot{f}_2(t)\Delta\omega_i - \Delta\omega_j}{V_{ti}} \]
\[ + q_1(t)\Delta\delta_i + q_2(t)\Delta P_{ej} + q_3(t)\Delta V_{tj} \]

where \( v_{fi} \) is the nonlinear input (8), \( \dot{f}_1(t) \) and \( \dot{f}_2(t) \) are nonlinear functions dependent on the operating point of a power system, and \( q_1(t)\Delta\omega_j, q_2(t)\Delta P_{ej}, q_3(t)\Delta V_{tj} \) represent the effects of remote dynamics of the \( j^{th} \) generator on the \( i^{th} \) generator. Selecting (17) as the new state vector, the DFL compensated model can be written as follows:

\[ \dot{\omega}_i = -\frac{D_i}{2H_i}\Delta\omega_i - \frac{\omega_{0i}}{2H_i}\Delta P_{ei} \]
\[ \dot{P}_{ei} = \frac{1}{T_{do)i}}f_1(t)v_{fi} + f_2(t)\Delta\omega_i \]
\[ + q_1(t)\Delta\delta_i + q_2(t)\Delta P_{ej} + q_3(t)\Delta V_{tj} \]
\[ \dot{V}_{ti} = \frac{1}{T_{do)i}}\dot{f}_1(t)v_{fi} + \dot{f}_2(t)\Delta\omega_i + q_1(t)\Delta\delta_i + q_2(t)\Delta P_{ej} + q_3(t)\Delta V_{tij} \]

After the uncertainty bounds of time varying parameters are found, it is possible to design the feedback control law (19) to stabilize the DFL compensated system (24)-(26). This will be illustrated in Section IV.

IV. ROBUST CONTROL WITH INTERCONNECTIONS

This section further develops on concepts presented in [14], [16], [18] to consider time varying terms in state, input and subsystem interconnection matrices to design robust feedback control which achieves asymptotic stability of the uncertain
We choose the required stabilizing control law as:

\[ \dot{x} = (A + \sum_{i=1}^{N} A_i r_i(t))x + (B + \sum_{i=1}^{l} B_i s_i(t))u_i \]

\[ + \sum_{k=1}^{K} \sum_{j=1}^{N} \{ p_{kij} G_{kij} + \sum_{i=1}^{\rho_k} G_{kij} \sigma_{ki} (t)g_{kij} (x_i, x_j) \} \]  

\[ (27) \]

where there are \( K \) sources of interconnection uncertainty, and for the \( i^{th} \) subsystem \( x_i (t) \in \mathbb{R}^{n_i} \) is the state, \( u_i (t) \in \mathbb{R}^{m_i} \) is the control and \( r(t) \in \mathbb{R}^l \), \( s(t) \in \mathbb{R}^l \), \( \sigma_k (t) \in \mathbb{R}^{\rho_k} \) represent uncertainty inputs, \( g_{kij} \in \mathbb{R}^{n_{ij}} \) are vector functions that represent nonlinearities in the \( i^{th} \) subsystem and in the interactions with other subsystems. The parameters \( p_{kij} \) are constants with values either 1 or 0. Note that for a power system model whose \( j^{th} \) machine is an infinite bus, \( p_{kij} = 0 \). It has been assumed that each uncertainty parameter satisfies the same bound in the known compact sets \( \mathcal{R}, \mathcal{S}, \mathcal{O}_k \):

\[ \mathcal{R} = \{ r : |r_i| \leq \bar{r}, i = 1, 2, \ldots, \xi \} \]  

(28)

\[ \mathcal{S} = \{ s : |s_i| \leq \bar{s}, i = 1, 2, \ldots, l \} \]  

(29)

\[ \mathcal{O}_k = \{ \sigma_{ki} : |\sigma_{ki}| \leq \bar{\sigma}_{ki}, i = 1, 2, \ldots, \rho_k \} \]  

(30)

and the matrices \( A_i, B_i \) and \( G_{kij} \) are assumed to be rank one decompositions of the form similar to [18]:

\[ A_i = d_i e_i^T, \quad B_i = f_i g_i^T, \quad G_{kij} = \varphi_{ki} \omega_{ki}^T \]  

(31)

We choose the required stabilizing control law as:

\[ u_i (t) = -\frac{1}{\epsilon} R^{-1} B^T P_i x_i (t) \]  

(32)

and consider the following:

\[ 2x_i^T P_i \Omega x_i = x_i^T (P_i \Omega + \Omega^T P_i) x_i \]  

(33)

Assumption 1: There exist known constant matrices \( W_{1i}, W_{1ij}, W_{2i}, W_{2ij}, \) \( W_{3i}, W_{3ij} \) such that for all \( x_i(t) \in \mathbb{R}^{n_i}, x_j(t) \in \mathbb{R}^{n_j}, i, j = 1, 2, \ldots, N \):

\[ ||g_{kij} (x_i, x_j)|| \leq ||W_{ki} x_i (t)|| + ||W_{kij} x_j (t)|| \]  

(34)

Lemma 1, [16]: The following identity

\[ \Sigma_i^T \Pi_i + \Pi_i^T \Sigma_i \leq \lambda_1^{-1} \Sigma_i^T \Sigma_i + \lambda_i \Pi_i^T \Pi_i \]  

(35)

holds for any real matrices \( \Sigma_i \) and \( \Pi_i \) of appropriate dimensions, and any scalar \( \lambda > 0 \).

Now, consider the state equation (27), the controller (32) and let the Lyapunov function be defined as

\[ V (x) = \sum_{i=1}^{N} x_i^T P_i x_i \]  

(36)

Then, by taking into account (33), we have that along the closed loop state trajectory

\[ \dot{V} (x) = \sum_{i=1}^{N} \{ 2x_i^T P_i A_i x_i + 2x_i^T P_i \sum_{i=1}^{l} A_i r_i(t) x_i \] 

\[ - \frac{2}{\epsilon} x_i^T P_i B_i R^{-1} B_i^T P_i x_i - \frac{2}{\epsilon} x_i^T P_i \sum_{i=1}^{l} B_i s_i(t) R^{-1} B_i^T P_i x_i \] 

\[ + \sum_{k=1}^{K} \sum_{j=1}^{N} \{ G_{kij} g_{kij} (x_i, x_j) \}^T P_i x_i \] 

\[ + x_i^T P_i \sum_{k=1}^{K} \sum_{j=1}^{N} \{ G_{kij} g_{kij} (x_i, x_j) \} \]  

(37)

where

\[ G_{kij} = p_{kij} G_{kij} + \sum_{i=1}^{\rho_k} G_{kij} \sigma_{ki} (t) \]  

(38)

The terms on the right hand side of (37) can be rewritten

\[ 2\bar{r} \sum_{i=1}^{\xi} x_i^T P_i d_i e_i^T x_i \leq \bar{r} \sum_{i=1}^{\xi} (x_i^T P_i d_i)^2 + \bar{r} \sum_{i=1}^{\xi} (e_i^T x_i)^2 \] 

\[ = \bar{r} x_i^T P_i \mathcal{D} P_i x_i + \bar{r} \bar{x}^T \mathcal{D} x_i \]  

(39)

and also

\[ \frac{2}{\epsilon} \sum_{i=1}^{l} x_i^T P_i f_i g_i^T R^{-1} B_i^T P_i x_i \] 

\[ \leq \frac{1}{\epsilon} \sum_{i=1}^{l} (x_i^T P_i f_i)^2 + \frac{1}{\epsilon} \sum_{i=1}^{l} (g_i^T R^{-1} B_i^T P_i x_i)^2 \] 

\[ = \bar{s} x_i^T P_i \mathcal{S} P_i x_i + \bar{s} \bar{x}^T \mathcal{S} x_i \]  

(40)

where

\[ \mathcal{D} = \sum_{i=1}^{\xi} d_i d_i^T, \quad \mathcal{S} = \sum_{i=1}^{l} f_i f_i^T \]  

(41)

then defining

\[ \bar{x} = [x_1^T, g_{11}^T \ldots g_{11N}^T, g_{21}^T \ldots g_{21N}^T, g_{31}^T \ldots g_{31N}^T]^T \]  

(43)

we have

\[ \dot{V} (x) = \sum_{i=1}^{N} \{ \bar{x}_i^T A_i \bar{x}_i \} - \sum_{k=1}^{K} \sum_{j=1}^{N} \{ p_{kij} [x_i^T W_{kij}^T W_{kij} x_i \] 

\[ + x_j^T W_{kij}^T W_{kij} x_j - g_{kij}^T g_{kij} ) \} \]  

(44)

such that

\[ A_{11} = A^T P_1 + P_1 A + \bar{r} \mathcal{D} P_1 + \bar{r} \mathcal{S} - \frac{2}{\epsilon} P_1 B R^{-1} B^T P_1 \] 

\[ + \frac{\bar{s}}{\epsilon} P_1 \mathcal{S} P_1 + \frac{\bar{s}}{\epsilon} P_1 B R^{-1} B^T P_1 \] 

\[ + \sum_{k=1}^{K} \sum_{j=1}^{N} \{ p_{kij} [W_{kij}^T W_{kij} + W_{kij}^T W_{kij} ] \} \]  

(45)
Taking into account results of [14], and the fact that
\[
K = 3 \sum_{k=1}^{N} \sum_{i=1}^{N} \left\{ p_{ij} [x^T W_{ki} W_{ij} x_i + x_i^T W_{kj} W_{ij} x_j - g_{kij}^T g_{kij}] \right\} \geq 0
\]
\[ (46) \]
it can be shown that \( \dot{V}(x) < 0; x \neq 0 \) and the Lyapunov function \( V(x) \) would be negative definite if
\[
A_{11} + P_i \left( \sum_{k=1}^{N} \sum_{j=1}^{N} g_{kij} G_{kij}^T \right) P_i < 0
\]
\[ (47) \]
It follows immediately that there exists positive definite matrix \( Q_i \) and \( \epsilon > 0 \) such that
\[
A_{11} + P_i \left( \sum_{k=1}^{N} \sum_{j=1}^{N} g_{kij} G_{kij}^T \right) P_i + \epsilon Q_i = 0
\]
\[ (48) \]
and using (35) it can be shown that
\[
\sum_{j=1}^{N} G_{kij} G_{kij}^T = \sum_{j=1}^{N} \left\{ (1 + \frac{\sigma_k^2}{\sum_{i=1}^{N} \lambda_i}) G_{kij} G_{kij}^T \right\} + \sum_{i=1}^{N} \lambda_i \varphi_k \bar{w}_k \varphi_k^T + \sum_{i=1}^{N} \sigma_k^2 \sum_{i=1}^{N} \varphi_k \bar{w}_k \varphi_k^T
\]
\[ (49) \]
Combining (45), (48) and (49) we can state that for the system with uncertainties in state, input and subsystem interconnection matrices described by (27), robust control law (32) achieves global asymptotic stability around the origin for resulting closed loop system, for all admissible uncertainties, if there exists positive definite solution \( P_i \) of the following algebraic Riccati equation:
\[
A_i^T P_i + P_i A_i - P_i \left[ \frac{2}{\epsilon} B_i R^{-1} B_i^T - \frac{s}{\epsilon} B_i R^{-1} \varphi R^{-1} B_i^T - \frac{s}{\epsilon} \mathcal{F} - \tilde{r} \mathcal{F} \right] P_i - \sum_{k=1}^{K} \sum_{j=1}^{N} \left( 1 + \frac{2}{\sum_{i=1}^{N} \lambda_i} \right) G_{kij} G_{kij}^T + \sum_{i=1}^{N} \lambda_i \varphi_k \bar{w}_k \varphi_k^T + \sum_{i=1}^{N} \sigma_k^2 \sum_{i=1}^{N} \varphi_k \bar{w}_k \varphi_k^T \right] P_i
\]
\[ (50) \]
where
\[
g_{112} = \Delta \delta; \quad g_{212} = \Delta \omega; \quad g_{312} = \Delta P_{ej}
\]
Considering the system parameters given in Section II, we have
\[
A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & -0.625 & -39.26 \\ 0 & 1.36 & 0 \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 0.12 \end{bmatrix}
\]
\[ (51) \]
\[
G_{112} = \begin{bmatrix} 0 \\ 0.017 \end{bmatrix}, \quad G_{212} = \begin{bmatrix} 0 \\ -0.6 \end{bmatrix}, \quad G_{312} = \begin{bmatrix} 0 \\ -0.06 \end{bmatrix}
\]
\[ (52) \]
and define the associated matrices that describe the uncertainty structure:
\[
d_1 = [0, 0, 1]^T; \quad e_1 = [0, 1, 0]^T; \quad f_1 = 0.1; \quad g_1 = [0, 0, 10]
\]
\[
\varphi_{11} = 1 = \varphi_{21} = \varphi_{31}; \quad \varphi_{11} = [0, 0, 1] = \varphi_{21} = \varphi_{31}
\]
\[
W_{11} = W_{112} = [1, 0, 0]; \quad W_{21} = W_{212} = [0, 1, 0]
\]
\[
W_{31} = W_{312} = [0, 0, 1]; \quad R = 5; \quad Q_1 = \text{diag}([2800, 100, 30000])
\]
\[ (53) \]
Solving the algebraic Riccati equation (50), robust control law for achieving transient stability of power systems is obtained
\[
v_{ft} = 35.78 \Delta \delta + 17.68 \Delta \omega - 125.28 \Delta P_{ei}
\]
\[ (54) \]
and the nonlinear excitation compensating loop is given by
\[
E_{fi} = v_{ft} + \Delta x_{di} i_{di} + \frac{P_{ei}}{i_{qi}}
\]
\[ (55) \]
where \( \tilde{r} = 0.9; \tilde{s} = 0.011; \epsilon = 0.001; \tilde{\sigma}_{11} = 0.03; \tilde{\sigma}_{21} = 0.3; \tilde{\sigma}_{31} = 0.03; \Lambda_1 = 0.01; \Lambda_2 = 0.1; \Lambda_3 = 0.0001 \)
\[ (56) \]
\[ (57) \]
\[ (58) \]
\[ (59) \]
\[ (60) \]
\[ (61) \]
\[ (62) \]
B. Robust Voltage Regulator

The DFL compensated model (24)-(26) can be written in the state equation form (27) where
\[
A = \begin{bmatrix} -\frac{D}{2\pi} & -\frac{\omega}{2\pi} & 0 \\ f_2(t) & 0 & 0 \end{bmatrix}, \quad B = \begin{bmatrix} \frac{1}{T_{d1}} f_1(t) \\ \frac{1}{T_{d2}} f_1(t) \end{bmatrix}
\]
\[ (63) \]
\[
G_{112} = \begin{bmatrix} 0 \\ \bar{q}_1(t) \end{bmatrix}, \quad G_{212} = \begin{bmatrix} 0 \\ \bar{q}_2(t) \end{bmatrix}, \quad G_{312} = \begin{bmatrix} 0 \\ \bar{q}_3(t) \end{bmatrix}
\]
\[ (64) \]
\[ (65) \]
\[ (66) \]
\[ (67) \]
where
\[
g_{112} = \Delta \delta; \quad g_{212} = \Delta \omega; \quad g_{312} = \Delta P_{ej}
\]
Considering the data given in Section II we have
\[
A = \begin{bmatrix} -0.625 & -39.26 & 0 \\ 1.36 & 0 & 0 \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 0.12 \end{bmatrix}
\]
\[ (68) \]
control law. The weighting functions can be derived from general control structure weights controllers for each domain, or as operating conditions change. More recently, attention has been paid to the application of the approach for power system transient stability assessment. The following sensitivity indicator is proposed:

\[ z_1 = \sqrt{\omega_1^2 + \Delta V_i^2} \]  

This simple choice of measurements has been shown to work quite well on a single machine infinite bus system model. The challenge now is to determine whether more sophisticated measurements would yield performance enhancing stability control.

**Sensitivity Indicator 2**: The energy function method has been widely used in transient stability analysis to estimate the domain of attraction of a stable equilibrium point. Here, a structure preserving energy function method based on the development in [22]–[24] is used for power system transient stability assessment. The following sensitivity indicator is proposed:

\[ z_2 = \sqrt{\omega_1^2 + \Delta V_i^2} \]  

where \( V_i \) is the structure preserving energy function for the multimachine power system model.

**VI. AN APPLICATION EXAMPLE**

To evaluate global control schemes presented in Section V, a three machine example system presented in Section II is utilized in the simulation study. Following the design procedure in Section IV, complete robust excitation controllers are obtained:

**Robust Transient Stabiliser**

\[ v_{ft} = 35.78 \Delta \delta_i + 17.68 \Delta \omega_i - 125.28 \Delta P_{ei} \]  

**Robust Voltage Regulator**

\[ v_{fvr} = 15.5 \Delta \omega_i - 20.93 \Delta P_{ei} - 85.46 \Delta V_i \]
and following the discussion in Section V, we propose the following global excitation control:

$$E_{fi} = \mu_\delta_i(z)e_{fis} + \mu_{\nu_i}(z)e_{fvr} + \Delta x_{di}i_{di} + \frac{P_ei}{i_{qi}}$$

(74)

where each global control law is distinctively implemented by sensitivity indicators given in (70) and (71).

The power system responses with excitation system controllers subjected to a severe short circuit fault are shown in Fig. 3. From the simulation results it can be seen that transient stability controller stabilizes the disturbed multimachine system but the post fault voltage differs from the prefault value. Excessive voltage deviation in the post fault period is not acceptable in practice. To maintain good post fault performance, voltage controller has been shown to achieve required voltage regulation.

The performance of global control scheme are illustrated in Fig.4 and Fig.5. From the simulations, it can be seen that transient stability and voltage regulation can be simultaneously enhanced with the proposed global control law.

A. Discussion on Global Control

Simulation studies have shown that simple choice of frequency and voltage measurements can be sufficient enough to interpolate different stages of system operation. While the sensitivity indicator based on the energy function method provides more detailed description of system stabilizing conditions, it can however offer considerable measuring and computational burden in the evaluation of system stability. In general, several important aspects need to be considered in the design of global control for power systems during the transient period such as: the network structure, nonlinearity and uncertainty, contingency screening, nature of faults or operating point changes, stabilizing priorities, number of controllers and stabilizing characteristics of each, available (decentralized or wide area) measurements to indicate system transients or changes in operating conditions, formulation of membership functions and partitioning of transient and post transient regions etc.

It still remains to develop global control methods to address highly complex structure of power systems, considering the dynamic coupling and coordination of all associated control actions. In practice, a general method is needed for designing controllers of global kind which are valid across the whole
Fig. 5. Comparison of Transient Stabiliser, Voltage Regulator and Global Control

time (sec)

power system operating region, for all states, and robust as parameters and conditions vary.

VII. CONCLUSIONS

This paper addresses simultaneously the major fundamental and difficult issues of nonlinearity, uncertainty and globality to derive performance enhancing power system stability control. Firstly, the DFL is presented as a simple nonlinear control tool to design nonlinear generator excitation controllers to achieve performance enhancing power system stability control. The global control law is then proposed to achieve simultaneous coordination of multiobjective control requirements of power systems. The global control is of smooth switching kind constructed by membership functions. Different sensitivity indicators are proposed and compared to assess stability requirements of a power system based on operating point variations. The design methodology is illustrated by application to the three machine power system model. The simulation results show that system stability and voltage regulation can be simultaneously preserved with the global control framework over a wide range of operating regions as a result of sudden changes in network topology.

REFERENCES


