DFT based study of transition metal nano-clusters for electrochemical NH3 production

Howalt, Jakob Geelmuyden; Bligaard, Thomas ; Rossmeisl, Jan; Vegge, Tejs

Published in:
Physical Chemistry Chemical Physics

Link to article, DOI:
10.1039/C3CP44641G

Publication date:
2013

Document Version
Publisher's PDF, also known as Version of record

Link back to DTU Orbit

Citation (APA):
This is an Accepted Manuscript, which has been through the RSC Publishing peer review process and has been accepted for publication.

Accepted Manuscripts are published online shortly after acceptance, which is prior to technical editing, formatting and proof reading. This free service from RSC Publishing allows authors to make their results available to the community, in citable form, before publication of the edited article. This Accepted Manuscript will be replaced by the edited and formatted Advance Article as soon as this is available.

To cite this manuscript please use its permanent Digital Object Identifier (DOI®), which is identical for all formats of publication.

More information about Accepted Manuscripts can be found in the Information for Authors.

Please note that technical editing may introduce minor changes to the text and/or graphics contained in the manuscript submitted by the author(s) which may alter content, and that the standard Terms & Conditions and the ethical guidelines that apply to the journal are still applicable. In no event shall the RSC be held responsible for any errors or omissions in these Accepted Manuscript manuscripts or any consequences arising from the use of any information contained in them.
DFT based study of transition metal nano-clusters for electrochemical NH$_3$ production

J. G. Howalt,$^{1,2}$ T. Bligaard,$^{2,3,4}$ J. Rossmeisl,$^2$ and T. Vegge$^*$$^{1,3}$

$^1$Department of Energy Conversion and Storage, Technical University of Denmark, DK-4000 Roskilde, Denmark
$^2$Center for Atomic-scale Materials Design, Department of Physics, Technical University of Denmark, DK-2800 Kgs. Lyngby, Denmark
$^3$SUNCAT Center for Interface Science and Catalysis, SLAC National Accelerator Laboratory, 2575 Sand Hill Road, Menlo Park, CA 94025, USA
$^4$Department of Chemical Engineering, Stanford University, Stanford, CA 94305, USA

(Dated: March 19, 2013)

Abstract

Theoretical studies of the possibility of producing ammonia electrochemically at ambient temperature and pressure without direct N$_2$ dissociation are presented. Density functional theory calculations were used in combination with the computational standard hydrogen electrode to calculate the free energy profile for the reduction of N$_2$ admolecules and N adatoms on transition metal nanoclusters in contact with an acidic electrolyte. The work has established linear scaling relations for the dissociative reaction intermediates NH, NH$_2$, and NH$_3$. In addition, linear scaling relations for the associative reaction intermediates N$_2$H, N$_2$H$_2$, and N$_2$H$_3$ have been determined. Furthermore, correlations between the adsorption energies of N, N$_2$, and H have been established. These scaling relations and the free energy corrections are used to establish volcanoes describing the onset potential for electrochemical ammonia production and hence describe the potential determining steps for the electrochemical ammonia production. The competing hydrogen evolution reaction has also been analyzed for comparison.
I. INTRODUCTION

In the past decade, it has become more apparent than ever that mankind needs to move towards more sustainable energy consumption with significantly smaller carbon footprint per capita.

There are a number of possible ways that could potentially be used to reduce the global carbon footprint and a number of technologies have already been implemented to generate electrical power more or less sustainably, such as for example wind turbines, solar cells, biomass fired power plants, etc. With time, and with increasing prices on fossil resources, some of these may become economically competitive with fossil resources. A difficult problem to address is that of substituting transportation fuels. To make sustainable transportation fuels economically, one needs not only a competitively inexpensive way to harvest a sustainable source of energy, but also to store the energy in a convenient form with a high enough volumetric and gravimetric energy density, and in a form that can easily be transferred to a vehicle. Since catalysis can facilitate the efficient synthesis of chemicals with high energy contents, catalysis plays a key role in many of the potential scenarios for reducing our dependence on fossil resources.

One chemical compound of great versatility is ammonia. Ammonia is primarily used for making fertilizer, ultimately sustaining roughly one-third of the World’s population.[1, 2] In terms of reducing the carbon footprint, ammonia is interesting for a number of reasons. First, there is the potential of improving the sustainability of the already huge industrial catalytic production of ammonia, which is on the order of over 100 million metric tons annually, and responsible for 1-2% of the global energy consumption. Secondly, ammonia is becoming increasingly interesting as a potential transportation fuel.[3] As an energy carrier, ammonia has the benefit that it can be used in the very energy efficient fuel cells such as the solid oxide fuel cell (SOFC) or a direct ammonia fuel cell (DAFC). Furthermore, it has the interesting feature of not emitting CO₂ while having a high energy density that is comparable with traditional fossil fuels, both volumetrically and gravimetrically.[3, 4] A highly energy-efficient method for the synthesis of ammonia (NH₃) from molecular nitrogen (N₂) in air is therefore desirable. Currently, ammonia synthesis is achieved by the Haber-Bosch process that initially dissociates the N₂ bond and then protonates each nitrogen atom[5]. This is the dissociative mechanism. In contrast, the natural enzymatic process in Nitrogenase
takes place by initially weakening the N-N bond through successive protonations until the
dissociation barrier is low enough that the N-N bond breaks; this process is referred to as
the associative mechanism.[6] The Haber-Bosch process is energy-intensive and centralized
due to the high required temperature and pressure and it is associated with a high capital
cost to construct the production plants. What we aim for is the electricity-based production
of ammonia utilizing electrochemistry, thus allowing small production scales and the use of
renewable energy sources like windmills or solar cells.

In the past several years, numerous experimental[7–21] and theoretical[22–34] studies
have examined ammonia synthesis and they offer excellent insight into the challenges faced
when developing new catalytic materials for this reaction. It has been shown in previous
studies that ammonia synthesis is very structure sensitive on metal surfaces and primarily
occurs on the surface steps of Fe and Ru[22, 35, 36] and one could expect the associative
mechanism to be even more structure sensitive. The competing hydrogen evolution reaction
(HER) is structure insensitive[37] and we have therefore looked at highly under-coordinated
nanoclusters as a way to investigate this discrepancy.

Furthermore, it has been shown that a similar reaction, CO oxidation, can be performed
on transition metal nanoparticles consisting of more noble metals at lower temperature[36,
40] than traditionally-used catalysts for this reaction. On the basis of the development
in density functional theory (DFT), it has become feasible to reliably model chemical
reactions.[41] We have used DFT calculations to investigate electrocatalytic production of
ammonia. In this work we have studied ammonia synthesis on the highly under-coordinated
M12 nanoclusters, see figure 1, and hence the extreme domain of possible under-coordination
that can be achieved, which earlier has been shown to dramatically change the reactivity of
inert metals[34, 38, 39], and compare the nanocluster to the traditionally studied fcc(211)
surfaces. While previous studies have looked at stepped metal surfaces, the B5 sites in
particular,[22, 31] we are performing all calculations on a consistent calculational basis,
so we can directly compare results on the M12 nanocluster with the reference system of a
fcc(211) stepped surface. We have investigated the reaction intermediates for the dissociative
and associative mechanism on fcc(211) surfaces and M12 nanoclusters for a large number
of transition metals and developed scaling relations similar to stepped and close-packed metal
surfaces. Based on vibrational calculations, entropy and zero point energy corrections calcu-
lated using statistical mechanics we construct Gibbs free energy diagrams for both reaction
pathways. These diagrams can then be used to determine the lowest potential which will make each part reaction exothermic, this is then defined as the onset potential for the overall reaction and can be used to construct volcano plots visualizing the onset potential for the electrochemical ammonia production across the investigated metals.

II. COMPUTATIONAL METHOD

A. The M12 cluster

The model system we analyze is the M12 nanocluster, which contains 12 metal atoms and has previously served as a model for an under-coordinated and very small nanoparticle.[40] The atoms in the M12 are positioned in two layers, with each layer containing six atoms. Each layer follows the fcc close-packed surface structure creating a triangle, see fig. 1a. The layers are placed above each other in the same fashion as they would in a normal close-packed slab, see fig. 1b. For the M12 nanocluster two lattice constants was used for each of the investigated metals. The first lattice constant was determined from calculations of the bulk lattice constants in the fcc structure for each metal (denoted bulk M12). The second lattice constant was determined by letting the M12 nanocluster relax the lattice constant until the lowest energy configuration was found (denoted relaxed M12). For both type of M12 nanoclusters the structure was kept fixed during all adsorption calculations of reaction species.

![Fig. 1](image_url)

**FIG. 1.** a: The M12 nanocluster seen from above. The close-packed structure is shown and the layers are arranged as two fcc close-packed layers would be in a normal fcc structure. b: The M12 nanocluster seen from the side. c: The front six atoms are the ones where the intermediates are allowed bonding to.

In this study, the analysis was limited to the adsorption sites indicated by the atoms marked with red in fig. 1c for the reaction intermediates, presented in eq. 3c-3h and 4b-4g.
These sites are chosen because they are highly under-coordinated and have other features than those of the back side of the clusters which resembles a step closer, but lacks the stabilizing terraces and have been analyzed in great detail in ref. [34].

B. DFT calculations

The calculations were carried out with DFT[42, 43] using the RPBE exchange correlation functional[44] in the projector augmented wave method[45, 46] as implemented in the GPAW code.[47–49] A grid of (3,3) for the finite difference stencils have been used together with a grid spacing of 0.18 Å, at least 20 free bands above the Fermi level and a Monkhorst-Pack[50] k-point sampling of $2 \times 2 \times 2$. A 7 Å vacuum layer around the nanocluster has been applied. In solving the electronic density self-consistently, the convergence criteria have been chosen such that the changes in energy were $< 10^{-5}$ eV and the density was 0.0001 electrons pr. valence electron and for most systems chosen orders of magnitude lower. Spin polarized calculations were also performed for metals that usually have a magnetic moment, such as Fe, Ni and Co although the magnetic moment could depend on the fixed geometry. In all calculations a Fermi smearing of 0.0001 eV have been used. The atomic simulation environment ASE[51] was used to set up the atomic structure of these systems. All relaxations of the adsorbates (N, H, NH, etc.) sitting on the bulk M12 nanocluster were carried out using the BFGS optimizer within ASE.

For the reference calculations on the fcc(211) stepped surface, a slab with five layers was utilized and in the direction following the edge of the step it was repeated once such that each layer consisted of 3 x 2 atoms. Of the five layers that were employed, the top two were allowed to relax and a vacuum of 7 Å on both sides of the slab was used. The utilized computational criteria only differ from the clusters in that a Monkhorst-Pack k-point sampling of $4 \times 4 \times 1$ was used, and the Fermi smearing was 0.0001 eV.

C. Reaction pathways

In the process of forming ammonia electrochemically, it is convenient to model the anode reaction

$$\text{H}_2 \rightleftharpoons 2\text{H}^+ + 2\text{e}^- \quad (1)$$
as the source of electrons and protons. The electrons are transported to the cathode side through an external circuit, while the protons are introduced into the proton conducting electrolyte and sustain the equilibrium and diffuse to the cathode. At the cathode a nitrogen molecule will react with the protons and electrons in the following overall reaction

$$N_2 + 6H^+ + 6e^- \rightarrow 2NH_3,$$

(2)

to form ammonia at the catalytically active site.

In this study two pathways to form ammonia have been investigated, the Heyrovski-type\cite{52} reaction for both the associative and dissociative mechanisms. For the Heyrovski-type mechanism, the adsorbed species of NH$_x$ or N$_2$H$_x$ ($x=\{0,1,2,3\}$) are directly protonated, in the following way: the proton directly attach to the molecule from the electrolyte and the electron comes from the surface and merges with the proton to create a hydrogen bonded to the molecule. In principle, the Tafel-type reaction could also occur, but this requires the reaction barriers for the hydrogenation steps\cite{34, 53} to be overcome, and will therefore require a higher temperature to drive the process forward. This is due to the fact, that the Tafel reaction\cite{54} requires the proton and the electron to merge to form a hydrogen adatom on the surface first, which then reacts with the adsorbed species of NH$_x$ or N$_2$H$_x$ ($x=\{0,1,2,3\}$). These reaction barriers have not be investigated in the present work.

The Heyrovski-type reactions for the electrochemical ammonia formation is presented below. First, we consider the dissociative Heyrovsky mechanism where the nitrogen molecule is dissociated on the surface and then subsequently protonated (an asterisk, *, denotes a surface site):

$$N_2 + 6H^+ + 6e^- \rightarrow 2NH_3,$$
Secondly, the associative Heyrovski mechanism is considered, where the nitrogen molecule attaches to the surface and is protonated before the nitrogen-nitrogen bond dissociates. In the equations below, information from the calculations has been used, where the addition of the fourth H to the molecule \( \text{N}_2 \) weakens the N-N bond so much that the molecule readily dissociates into \( \text{NH}_x \) species on the surface.

\[
\text{N}_2(\text{g}) + 6(\text{H}^+ + \text{e}^-) + 2^* \rightleftharpoons \text{N}_2^{*\ast} + 6(\text{H}^+ + \text{e}^-) \quad (3a)
\]
\[
\text{N}_2^{*\ast} + 6(\text{H}^+ + \text{e}^-) \rightleftharpoons 2\text{N}^* + 6(\text{H}^+ + \text{e}^-) \quad (3b)
\]
\[
2\text{N}^* + 6(\text{H}^+ + \text{e}^-) \rightleftharpoons \text{NH}^\ast + \text{N}^* + 5(\text{H}^+ + \text{e}^-) \quad (3c)
\]
\[
\text{NH}^\ast + \text{N}^* + 5(\text{H}^+ + \text{e}^-) \rightleftharpoons \text{NH}_2^\ast + \text{N}^* + 4(\text{H}^+ + \text{e}^-) \quad (3d)
\]
\[
\text{NH}_2^\ast + \text{N}^* + 4(\text{H}^+ + \text{e}^-) \rightleftharpoons \text{NH}_3^\ast + \text{N}^* + 3(\text{H}^+ + \text{e}^-) \quad (3e)
\]
\[
\text{NH}_3^\ast + \text{N}^* + 3(\text{H}^+ + \text{e}^-) \rightleftharpoons \text{NH}_3^\ast + \text{NH}^\ast + 2(\text{H}^+ + \text{e}^-) \quad (3f)
\]
\[
\text{NH}_3^\ast + \text{NH}^\ast + 2(\text{H}^+ + \text{e}^-) \rightleftharpoons \text{NH}_3^\ast + \text{NH}_2^\ast + (\text{H}^+ + \text{e}^-) \quad (3g)
\]
\[
\text{NH}_3^\ast + \text{NH}_2^\ast + (\text{H}^+ + \text{e}^-) \rightleftharpoons 2\text{NH}_3^\ast \quad (3h)
\]
\[
2\text{NH}_3^\ast \rightleftharpoons \text{NH}_3^\ast + \text{NH}_3(\text{g}) + ^\ast \quad (3i)
\]
\[
\text{NH}_3(\text{g}) + \text{NH}_3^\ast + ^\ast \rightleftharpoons 2\text{NH}_3(\text{g}) + 2^* \quad (3j)
\]

Alternatively, the reaction eq. 4d has the possibility of split into \( \text{NH} \) and \( \text{NH}_2 \) on the surface and has been observed on some of the metals.
D. Electrochemical modelling

With DFT it is possible to calculate the reaction energy, $\Delta E$, for each of the reaction intermediates described above in the dissociative and associative Heyrovski pathway. This reaction energy is calculated with respect to the gas-phase molecules of hydrogen and nitrogen and a clean M12 nanocluster:

$$\Delta E = E_{M12-N_xH_y} - (E_{M12} + \frac{x}{2}E_{N_2(g)} + \frac{y}{2}E_{H_2(g)}),$$  \hspace{1cm} (5)$$

where $E_{M12-N_xH_y}$ is the total energy of the system containing the M12 nanocluster with the adsorbed $N_xH_y$ species, $E_{M12}$ is the total energy of the system containing only the M12 nanocluster, while $E_{N_2(g)}$ and $E_{H_2(g)}$ are the calculated gas-phase energies of nitrogen and hydrogen molecules, respectively.

The reaction energies give information about the catalytic properties for ammonia formation, which we shall elaborate further upon in the discussion of the scaling relations in one of the later sections. However, for a thorough understanding, free energy corrections for each reaction intermediate needs to be determined and included in the analysis.

We obtain a reasonable approximation to the free energy from the DFT calculations for the adsorbate relative to the gas-phase molecular nitrogen and hydrogen from the expression:

$$\Delta G = \Delta E + \Delta E_{ZPE} - T\Delta S,$$ \hspace{1cm} (6)

where the $\Delta E_{ZPE}$ and $\Delta S$ are the reaction zero point energy and reaction entropy, respectively, and we have ignored thermal internal energy contributions.

Within the harmonic approximation, it is possible to calculate the vibrational frequencies for all reaction intermediates using a finite difference method. \cite{55} The surface species were only allowed to vibrate, while the surface atoms were kept fixed and hence the change in free energy of the metal atoms was neglected. From the vibrational frequencies the zero point energy and the entropy at the reaction conditions can been determined. The zero point energy term is given as

$$E_{ZPE} = \sum_i \frac{1}{2}\hbar \nu_i.$$ \hspace{1cm} (7)

The vibrational entropy contribution were calculated explicitly using standard equations from statistical mechanics and are shown below:

$$S_{vib} = R \sum_i \left( \frac{\Theta \nu_i / T}{\exp(\frac{\Theta \nu_i}{T}) - 1} - \ln \left[ 1 - \exp \left( -\frac{\Theta \nu_i}{T} \right) \right] \right)$$ \hspace{1cm} (8)
In these expressions, the characteristic vibrational temperature, $\Theta_{v_i}$, is equal to $h\nu_i/k_B$. Here $R$ is the gas constant, $h$ is Planck’s constant, $k_B$ is Boltzmann’s constant and $T$ is the absolute temperature and $\nu$ is the vibrational frequency.

In addition to the entropy and zero point energy corrections we include the effects of the applied potential driving the electrochemical reaction. To include the effect of potential, we use the computational standard hydrogen electrode,[56] which has been successfully applied to describe a number of electrochemical reactions, including the trends in oxygen[57, 58] and nitrogen[35] and CO$_2$ reduction.[59] The procedure of the computational standard hydrogen electrode is briefly outlined below.[56]

The standard hydrogen electrode (SHE) is been chosen as reference potential. The chemical potential (the free energy per H) of (H$^+$ + e$^-$) is related to that of $\frac{1}{2}$H$_2$(g), see eq. 1.

For pH = 0, a potential of $U = 0$ V relative to the SHE and a partial pressure of 1 bar of H$_2$ in the gas phase at 298 K, the reaction free energy of eq. 1 is equal to the net reaction of eq. 2 at an electrode.

Use the free energy for the reaction intermediates as defined in eq. 6.

The next step is to incorporate the effects of an applied potential in all reactions involving an electron transfer and for the protons the pH. The free energy shift for a reaction involving $n$ electrons is $-neU$ and hence the free energy reads

$$\Delta G = \Delta E + \Delta E_{ZPE} - T\Delta S - neU,$$

This holds true for a pH value of 0.

For pH values different from 0, the correction to the free energy of H$^+$-ions have to be corrected for the concentration dependence of the entropy, the shift reads $G(pH) = -kT \cdot \ln[H^+] = kT \cdot pH \cdot \ln[10]$.

All calculations presented in the present study are for a pH value of 0.

III. RESULTS AND DISCUSSION

In this section, we present the adsorption sites for the reaction intermediates, show the corresponding adsorption energies defined by eq. 5 plotted as linear scaling relations (a linear relation between different reaction intermediate) for this geometric structure, and introduce the corrections to the free energy. With these tools, the construction of volcano
plots showing the onset potential for each of the reaction mechanisms when electrochemical N₂ fixation is possible.

A. Adsorption sites

We will use adsorption on the ruthenium M12 nanocluster as an illustration because the adsorption sites for this metal resembles the characteristics for all the metals studied here. Among the studied metals, from the very reactive metals such as Sc, Ti, and Nb to the very noble metals such as Au, Ag, and Cu, there are small variations in the adsorption sites. However, the M12 nanocluster have many similar types of adsorption sites, which can be divided in the usual adsorption-site subgroups such as hollow, bridge, on-top. Each of the adsorption site in each subgroup will be slightly geometrically different and hence for each of the metal the specific electronic properties will diversify which of the specific sites are most stable. But the type of sites are close to identical throughout the investigated metals across all reaction intermediates. In figure 2, the adsorption sites on ruthenium M12 nanocluster can be seen.

In fig. 2(1) the adsorption site for N₂ is shown. The nitrogen molecule prefer to bind in a di-sigma type bond to the surface where the nitrogen atoms are bonded to two different metal atoms in the surface. Here the most stable sites were edges. For some sites on most of the metals, bonding of the N₂ molecule vertically to the surface was possible, where one atom was attached to the surface while the other atom where away from the surface and acting as an antenna. The difference in adsorption energy between these two types of bonds are on the order of 0.1 to 0.3 eV. It should be noted that for the very reactive metals, the N₂ molecule had very few stable adsorption configurations since the splitting of the N-N bond and creation of two N* on the surface is exothermic. Furthermore, the barrier for this splitting is in the literature shown to be very low compared to the noble metals.[60]

The nitrogen adatom adsorbs in a hollow site. For hydrogen, the H₂ molecule was very rarely stable on the surface and would split into two hydrogen adatoms on the surface. The hydrogen bonding site is shown here to be a bridge site, but the difference in energy between the different types of adsorption sites were very small. For NH, NH₂ and NH₃ they bind to hollow, bridge and ontop sites respectively, see fig. 2(4-6).

The N₂Hₓ species on the M12 nanoclusters prefer to bond to a bridge site, where each N
The most stable adsorption sites for the reaction intermediates in both the dissociative and associative mechanism on the ruthenium M12 nanocluster. The dark atoms are nitrogen, the small atoms are hydrogen and the light atoms are ruthenium. The adsorption sites for the adsorbates presented for the M12 nanocluster are only representative for the type of adsorption site (hollow, bridge, ontop) and not the actual bonding site for the other metals, which means a N atom could bind more strongly to another hollow site on a different metal studied in this work.

Looking carefully at the figures of the N$_2$H$_x$, on fig. 2(7-9), it is possible to see an increase in the internal bonding length as the number of hydrogen is increased and that one of the nitrogen atoms is further away from the metal atom than the other nitrogen atom. This represent the internal weakening of the N-N bond and is a key factor in the associative mechanism and the weakening of the bond between the metal and nitrogen atom. The molecule is therefore mostly bonded through one of the nitrogen atoms.

**B. Scaling relations**

In earlier studies it has been shown that for hydrogen containing adsorption species (such as NH$_x$, OH$_x$, CH$_x$, and SH$_x$) linear scaling relations exists that describes the adsorption energies for all species adsorbed onto either a closed packed or a stepped surface.[61] This
means that the adsorption energies of \( AH_x \) (\( A \) being one of the backbone parts mentioned earlier, C, N, O, or S) on a given number of metals scale with the corresponding adsorption energy of \( A \) adsorbed onto the surface:

\[
\Delta E_{AH_x} = \alpha(x) \Delta E_A + \kappa(x).
\] (10)

Here \( \alpha(x) \) is the slope of the scaling relation, while \( \kappa(x) \) is a constant. In previous studies, \( \kappa(x) \) was the factor influenced by the geometric structure (whether it is a closed-packed, a stepped or another kind of surface) while the slope \( \alpha(x) \) was found to be close to a constant for different surface types.

The slope is to a large extent dependent on the adsorbates number of hydrogen versus the maximum number of possible hydrogen in \( AH_x \) (it is 3 for \( NH_3 \)).[61] The dependency on the hydrogen is such that:

\[
\alpha(x) = \frac{x_{\text{max}} - x}{x_{\text{max}}}. \tag{11}
\]

where \( x_{\text{max}} \) is the maximum number of hydrogen that can bond to the central atom, i.e. 3 for N, while the valency is defined as \( (x_{\text{max}} - x) \). It should be noted that these relations exist (but vary) for different vicinal surfaces/adsorption sites. The relations are therefore useful for understanding the basic underlying trends, but one should keep in mind the complexity arising from variations in adsorption sites.

![Graph](image)

**FIG. 3.** The scaling relations for \( NH_x \) species on the relaxed M12 nanoclusters consisting of transition metals. The adsorption geometries are chosen as the most stable calculated ones.

In fig. 3 the adsorption energy for \( NH, NH_2 \) and \( NH_3 \) is plotted as a function of the adsorption energy of N adatoms on the relaxed M12 nanocluster. There exist a linear
relation for all NH$_x$ species on this very under-coordinated structure. The slopes follow to a large extent the predicted ones from eq. 11. For NH, NH$_2$, and NH$_3$ the slopes are 0.72, 0.46, and 0.05. For both the bulk M12 and the relaxed M12 nanoclusters and the stepped surface fcc(211) the trend for the slope is the same, see fig. S1-4 in the supporting material, and the scaling relation holds true for both lattice constants. The only difference is an electronic effect that shifts the binding energy of a metal with the bulk lattice constant along the line to the adsorption energy of the metal with the relaxed lattice constant. The adsorption energies for the reaction species show that the bulk lattice constant M12 nanocluster structure is more reactive than the relaxed M12 nanocluster. This is to be expected due to the effects of stress and strain that has been shown previously by Nørskov et al.[62] The values of the slopes are in good agreement with what we would have expected from results obtained in earlier studies of the scaling relations for these species on close-packed and stepped surfaces. We can not directly compare these calculated scaling relations with the previous described relations of NH$_x$ species, since the underlying computational ab initio codes are different. Therefore, reference calculations of similar relations for a lower number of stepped fcc(211) surfaces have been carried out and the slopes $\alpha(x)$ and the constants $\kappa(x)$ are presented in table I. The variations in the constants between the two systems are very small and close to the uncertainty of DFT calculations. It is therefore not possible to define a noticeably geometrical effect when going from the stepped fcc(211) surface to this highly under-coordinated surface. However, the electronic effect (which is the movement down the line) is somewhat more noticeable, in the order of 0.1-0.6 eV for the bulk M12 nanoclusters. For the relaxed M12 nanoclusters the electronic effect is small. Comparing these effects with the previous obtained shifts between close-packed and stepped surfaces the geometrical effect is minor. [61, 63]

The fixation of the metals in the M12 structure will, however, influence the calculated adsorption energies and hence effect the determined scaling relations. Structures with or without adsorbates would all have had lower energy, if the structure were allowed to relax fully but this study is focused on determining trends in such under-coordinated structures. Calculations with completely free metal atoms will be difficult to systematically the examined metals.

In fig. 4, the scaling relations for the adsorption energy of a N$_2$ molecule and a H adatom are plotted against the adsorption energy of N adatoms. The slope for the adsorption energies
TABLE I. The energy scaling relations for all reaction intermediates for ammonia synthesis on the M12 nanocluster for both relax and bulk lattice constants structures and compared with the fcc(211) stepped surface. The energy relations are with respect to an adsorbed N. It has to be noted that the number of metals in this study is not as large as on the M12 nanocluster calculations. The figures of the scaling relations for stepped surfaces can be found in the supplementary material.

<table>
<thead>
<tr>
<th>Adsorbate</th>
<th>fcc(211)</th>
<th>M12</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\alpha(y,x)$</td>
<td>$\kappa$ (eV)</td>
</tr>
<tr>
<td>(\text{N}_2)</td>
<td>0.31</td>
<td>-0.47</td>
</tr>
<tr>
<td>(\text{H})</td>
<td>0.23</td>
<td>-0.49</td>
</tr>
<tr>
<td>(\text{NH})</td>
<td>0.65</td>
<td>-0.47</td>
</tr>
<tr>
<td>(\text{NH}_2)</td>
<td>0.39</td>
<td>-1.32</td>
</tr>
<tr>
<td>(\text{NH}_3)</td>
<td>0.16</td>
<td>-1.51</td>
</tr>
<tr>
<td>(\text{N}_2\text{H})</td>
<td>0.57</td>
<td>0.21</td>
</tr>
<tr>
<td>(\text{N}_2\text{H}_2)</td>
<td>0.54</td>
<td>0.01</td>
</tr>
<tr>
<td>(\text{N}_2\text{H}_3)</td>
<td>0.46</td>
<td>-0.25</td>
</tr>
</tbody>
</table>

FIG. 4. The scaling relations for \(\text{N}_2\) and \(\text{H}\) species on the M12 nanoclusters consisting of transition metals. The adsorption positions are chosen as the most stable ones.

of 0.2 for H adatoms lies close to what previously has been documented in literature.[35] The scaling relation for a H adatom is systematic and there is only a minor electronic effect between the bulk M12 and the relaxed M12 nanocluster, see fig. S5 in the supporting material. The shift between the M12 nanocluster calculations and the fcc(211) stepped
calculations for H are again minor and there is no signs of a noticeable geometric effect, see fig. S6 in the supporting material.

However, for the N\textsubscript{2} scaling relation there is a significant variation in the slope. The bulk M12 nanocluster has a slope of 0.46, while the relaxed M12 nanocluster gives a slope of 0.26, see fig. S7 in the supporting material. The values for the relaxed M12 corresponds very well to the reference calculations on the fcc(211) stepped surface, see fig. S6 in the supporting material, which gives a slope of 0.31; the slope for N\textsubscript{2} scaling of 0.3 from literature for both stepped and close-packed surfaces.[61]

The variation in the adsorption energy of N\textsubscript{2} between the bulk M12 and relaxed M12 nanocluster calculations originates from a combination of an electronic effect from the relaxation of the lattice constant, causing a shift along the scaling relation line, and a geometric effect caused by different adsorption geometries for the reactive metals compared to the noble metals. For the reactive metals, the adsorption sites are disigma bonded while for the more noble metals N\textsubscript{2} is adsorbed as an antenna on the surface, which could explain the big change observed specifically for the reactive metals. This difference in adsorption geometry can influence the strength of the adsorption when changing the overall reactivity of the nanocluster going from one M12 lattice constant to another. For the other reaction intermediates studied in this work and N\textsubscript{2} on the noble metals, one nitrogen atom is mainly bound to the surface, while for N\textsubscript{2} on the reactive metals, both nitrogen atoms are adsorbed to the surface. The adsorption sites for the adsorbed N\textsubscript{2} molecule is different on the stepped fcc(211) surface where the N\textsubscript{2} molecule is bonded to the edge and terrace at the same time.[32, 34, 35] The consequences of this dramatic change is that the associative mechanism on the bulk M12 nanoclusters seem to be more active. The same tendencies are seen for the other important reaction intermediates NH\textsubscript{3} and N\textsubscript{2}H. These three reaction intermediates are key reaction species for the associative mechanism and therefore a shift in scaling relations is very interesting.

In fig. 5, the linear scaling relations for the N\textsubscript{2}H\textsubscript{x} adsorbates are shown. In the plot only the adsorption energies calculated for the N\textsubscript{2}H, N\textsubscript{2}H\textsubscript{2}, and N\textsubscript{2}H\textsubscript{3} species are included, since adsorbates containing more hydrogen spontaneously split into two molecules, ranging over NH, NH\textsubscript{2}, NH\textsubscript{3} to NH\textsubscript{3}(g). The slopes for the species are 0.77, 0.66 and 0.50 for N\textsubscript{2}H, N\textsubscript{2}H\textsubscript{2} and N\textsubscript{2}H\textsubscript{3} respectively. The slopes for N\textsubscript{2}H and N\textsubscript{2}H\textsubscript{2} species are different than those of the reference system of the stepped fcc(211) surface, see fig. S8 in the supporting material.
FIG. 5. The scaling relations for $N_2H_x$ species on the M12 nanoclusters consisting of transition metals. The adsorption positions are chosen as the most stable ones.

These relations again present a change in the mechanics for the associative mechanism for the under-coordinated reaction sites. To compare with the substantial effect effects between the bulk M12 and relaxed M12 nanocluster observed for $N_2$, there is no change between the two systems, see fig. S9-11 in the supporting material, indicating that the electronic effect on $N_2$ is higher because the $N_2$ is bonded in two sites, whereas $N_2H_x$ species are bonded mostly to one site.

The simple underlying argument for scaling relations for $AH_x$ species (where A is N in this case) does not hold for more complicated molecules, such as the $A_2H_x$ molecules considered in this work. The internal bonding of orbitals in the A-A backbone will make a derivation similar to the one carried out for $AH_x$ species much more complicated and may depend more strongly on the local adsorption environment; i.e. whether both backbone atoms binds to the surface or only one, and how will the hydrogen atoms bind to one or both backbone atoms and how this may effect the bonding.

C. Entropy and Zero Point Energy corrections

The established linear scaling relations greatly simplify the adsorptions energies for all reaction intermediates on all involved metals. As a reference the gas-phase entropy of nitrogen and hydrogen molecules have been used. The conditions for which the corrections have been calculated are ambient conditions, room temperature and 1 bar. The corrections
for the zero point energy $E_{ZPE}$ and for the entropy $S$ have been calculated using statistical mechanics for the surface intermediates, see eq. 7 and eq. 8 respectively, and for the gas phase species table values have been used.[64, 65]

<table>
<thead>
<tr>
<th>Molecule</th>
<th>ZPE (eV)</th>
<th>TS (eV/K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_2(g)$</td>
<td>0.211</td>
<td>0.592</td>
</tr>
<tr>
<td>$H_2(g)$</td>
<td>0.344</td>
<td>0.404</td>
</tr>
<tr>
<td>$NH_3(g)$</td>
<td>0.985</td>
<td>0.596</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Molecule</th>
<th>ZPE (eV)</th>
<th>TS (eV/K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N^*$</td>
<td>0.076</td>
<td>0.020</td>
</tr>
<tr>
<td>$H^*$</td>
<td>0.171</td>
<td>0.014</td>
</tr>
<tr>
<td>$N_2^*$</td>
<td>0.182</td>
<td>0.033</td>
</tr>
<tr>
<td>$NH^*$</td>
<td>0.365</td>
<td>0.032</td>
</tr>
<tr>
<td>$NH_2^*$</td>
<td>0.713</td>
<td>0.041</td>
</tr>
<tr>
<td>$NH_3^*$</td>
<td>1.036</td>
<td>0.058</td>
</tr>
<tr>
<td>$N_2H^*$</td>
<td>0.480</td>
<td>0.057</td>
</tr>
<tr>
<td>$N_2H_2^*$</td>
<td>0.796</td>
<td>0.067</td>
</tr>
<tr>
<td>$N_2H_3^*$</td>
<td>1.135</td>
<td>0.063</td>
</tr>
</tbody>
</table>

**TABLE II.** The thermodynamic corrections for the reaction intermediates on the M12 nanocluster calculated at 298 K. These corrections are based on statistical thermodynamics calculated using a harmonic vibration of adsorbates on the surface.

The calculated thermodynamic corrections are presented in table II. These thermodynamic corrections have been calculated for all adsorption species on the Ru M12 nanocluster and have been used as a first order approximation for the entropy and zero point energy terms for the other metals and later tested on Mo. It is reasonable to expect that the difference in the correction terms across the metals is small because the type of adsorption site for each reaction intermediate are similar.
IV. VOLCANO PLOTS

Using the tools described above, it is possible to create plots visualizing the onset potential for electrochemical nitrogen fixation. This method was introduced in ref. [58] for the electrolysis of water on oxide surfaces.

In this analysis, the reaction free energy can be used directly as a simple measure of electrocatalytic activity. The reaction free energy for each elementary step can be expressed as functions of the applied bias \( U \) and the adsorption energy \( \Delta E_N \) or the reaction free energy \( \Delta G_N \) of the nitrogen adatom (\( N^* \)). This is possible because the linear scaling relations combined with the approximation that the free energy corrections at the Ru M12 nanocluster describe all important trends for the electrocatalytic activity. All protonation steps for both the dissociative and associative mechanisms include a removal of a proton and an electron from the surrounding electrolyte and an addition of a hydrogen to the adsorbed molecule. A dependency on the applied potential will therefore be a direct result of this framework. In the following, the method to determine the onset potential as a function of the free energy of an adsorbed nitrogen adatom will be illustrated.

The free energy of a basic protonation reaction where both reaction intermediates (initial and final state) are bonded to the surface, e.g. eq. 3d, can be described solely by the reactants taking active part in the electron transfer. The result is a simplification of the reaction described in eq. 3d to the following reaction:

\[
\text{NH}^* + 2(\text{H}^+ + \text{e}^-) \rightleftharpoons \text{NH}_2^* + (\text{H}^+ + \text{e}^-),
\]

\[
\Delta G_{\text{dis,2}} = \Delta G_{\text{NH}_2^*} - \Delta G_{\text{NH}^*},
\]

which describes the change in free energy of the reaction as defined in eq. 9. Inserting the general expression for the scaling relations formulated in eq. 10 into the equation above, the change in free energy for this part reaction is given as a function of the nitrogen binding
energy, $\Delta E_N$, and the applied potential, $U$.

\[
\Delta G_{\text{dis,2}} = \Delta G_{\text{NH}_2} - \Delta G_{\text{NH}} \\
= \alpha_{\text{NH}_2} \Delta E_N + \kappa_{\text{NH}_2} + E_{\text{ZPE, NH}_2} - T\Delta S_{\text{NH}_2} - eU \\
- (\alpha_{\text{NH}} \Delta E_N + \kappa_{\text{NH}} + E_{\text{ZPE, NH}} - T\Delta S_{\text{NH}} - 2eU) \\
= (\alpha_{\text{NH}_2} - \alpha_{\text{NH}}) \Delta E_N + eU \\
+ (\kappa_{\text{NH}_2} + E_{\text{ZPE, NH}_2} - T\Delta S_{\text{NH}_2}) \\
- (\kappa_{\text{NH}} + E_{\text{ZPE, NH}} - T\Delta S_{\text{NH}}) \\
\] (13)

Inserting the derived numbers from the scaling relations presented in table I and the calculated free energy corrections from table II into eq. 13 and subsequently converting $\Delta E_N$ to $\Delta G_N$ yields:

\[
\Delta G_{\text{dis,2}} = -0.26 \Delta E_N - 0.34eV + eU \\
= -0.26(\Delta G_N - 0.23eV) - 0.34eV + eU \\
= -0.26 \Delta G_N - 0.28eV + eU, \\
\] (14)

where the 0.23 eV is the calculated change in energy going from adsorption energy to reaction free energy for an adsorbed nitrogen adatom. The next step that must be taken is to apply a potential such that each forward reaction has negative free energy change and the onset potential is defined when $\Delta G_{\text{dis,2}} = 0$. This ensures that the reaction occurs spontaneously, as long as the protonation barrier is low. Applying this constraint to eq. 14, the minimum onset potential needed to drive this specific reaction is given by:

\[
U = 0.26/e \Delta E_N + 0.28 V \\
\] (15)

where $e$ is the elementary charge.

This procedure can be done for all pure protonation steps and plotting the obtained expressions in one plot will form a volcano describing the necessary onset potential which makes each part reaction exothermic. Fig. 6 shows both the associative and dissociative process. The associative process is purely electrochemical, whereas the dissociative process involves the non-electrochemical (thermal) step, i.e. the splitting of the N-N bond, which has to be dealt with separately as outlined below.

The volcano for the associative mechanism can be understood utilizing the method behind eq. 13, 14 and 15, and it forms the two solid lines in fig. 6 forming a volcano. These part
reactions are the ones that limit the associative electrochemical ammonia synthesis. The two solid lines form a volcano, where the lowest onset potential for driving the associative ammonia synthesis electrochemically is close to $U = -0.45 \, V$. None of the investigated metals are, however, at the optimal reaction free energy of a nitrogen adatom at $-0.5 \, eV$. The closest metals are divided in two groups, one consisting of the more reactive metals Mo, V and Nb and the other group consisting of Fe being by far the closest metal and Ru, Pt and Co further away. Here Ru and Fe are already well known good heterogeneous catalyst materials for the Haber-Bosch process and are unfortunately even better HER catalysts. Finding that the optimum for the associative mechanism lies between Mo and Fe fits very well with the active site in the enzyme Nitrogenase which is the Iron Molybdenum cofactor.[28] Employing this methodology, effects such as coverage dependence, and the dissociation of $N_2$ or desorption of $NH_3$ in particular are not included and will have an effect on the predicted efficiency. However, this analysis suggest that alloy particles with free energies of $-0.5 \, eV$ for adsorbed N adatoms should be good catalysts for the associative mechanism.

![Diagram](image.png)

**FIG. 6.** Volcano plot for the associative and dissociative mechanism with the free energy $\Delta G_{N^*}$ as a descriptor. The competing reaction of creating hydrogen on the surface is also shown as the dotted lines. The two solid lines indicate the limiting potential for the associative mechanism. For the dissociative mechanism the gray area is added as a potential area for where it could be more favorable to go through the dissociative mechanism. The efficiency in this area is dependent on the dissociation of the $N_2$ molecule on the surface. At the top of the gray area the dissociative mechanism will be comparable to HER.
The above mentioned framework does not describe the main challenges of the dissociative mechanism because it lacks the description of the dissociation of \( N_2 \) on the surface. Furthermore, this description will not form one of the two legs to create the volcano (in this case the so-called right leg), see fig. 6 where solid black line is the electrochemical limiting reaction for the dissociative mechanism. The reason for this behavior is the scaling relations and that the slopes depends on the number of hydrogen vacancy in the adsorbed molecule. The lines describing the necessary onset potential for the dissociative mechanisms will therefore have slopes with the same sign and almost the same size. The consequence of this behavior will be that the limitations to the electrochemical reaction will only be described for the reactive metals and lack for the noble metals. This description suggest that the electrochemical nitrogen fixation efficiency will be perfect over the noble metals. However, this picture is not correct, since the main hindrance for the noble metals is the \( N_2 \) dissociation. The dissociation of \( N_2 \) is not affected by the potential and is normally seen as a heterogenous reaction step and will have activation barriers that is much higher for noble metals than for reactive metals described by the Brandsted-Evans-Polanyi lines.\cite{60}

For the good dissociation catalysts (the reactive metals) the hydrogen evolution reaction are preferred compared to ammonia production. This is the reason why a shift of the volcano utilizing the structure (in)sensitivity to relatively enhance the ammonia production with respect to HER is interesting.

Another method is therefore needed to describe the limitations for the dissociative mechanism on the right leg. Three limitations that should be satisfied for the dissociation of \( N_2 \) to be possible on the surfaces are:

1: It should be preferred to have a nitrogen molecule bonded to the surface. The free energy of \( N_2^* \) should hence be negative. This break-point are located at \( \Delta G_N = 0.03 \) eV.

2: The reaction free energy of \( N_2(g) \) to \( 2N^* \) should be negative and hence exorthermic. This corresponds to \( \Delta G_N = 0 \) eV and should describe the shift from having nitrogen on the surface to having problems bonding the nitrogen at all.

3: The gain in reaction free energy for the dissociation reaction of \( N_2^* \) to \( 2N^* \) on the surface should be negative and hence have a more stable end configuration. Using the linear scaling relations and free energy corrections a break-point for where the gain is zero. This occur at the reaction free energy of nitrogen adatoms at -0.08 eV.

The most conservative limit have been implemented as a horizontal line on fig. 6. To-
gether with the line defining the limiting onset potentials, this limit adds a triangle to the existing associative volcano and this triangle is marked with gray.

These three possible ways of looking at the limiting step for the dissociative mechanism gives an estimate of the upper and lower bounds on when the dissociative mechanism will be limited by the dissociation. Including one of the other proposed limitations only shift the top of the volcano by 0.11 eV on the x-axis and only have a minor change in the onset bias. The added triangle only marks a potential increase in electrocatalytic activity and is to some degree uncertain. Here it is worth to note that in the gray marked area the vertical line is the best case scenario, while the two lines are the worst case.

Comparing the onset potential for ammonia and hydrogen production it is only at the very top of the volcano that there is a possibility of ammonia production requiring a lower onset potential than hydrogen production. As it seems from this volcano it would still be marginally preferred to create hydrogen. However, there will be effects not included in this analysis that will have an effect in the efficiency of the catalyst and on the competition between ammonia and hydrogen production such as coverage, adsorbate-adsorbate effects, the surrounding electrolyte affecting the equilibriums. Furthermore, the fixed geometry used in this study could also influence the results. But it is important to see this study as trend study to understand to some degree how under-coordinated reactive sites can act as ammonia catalysts.

The volcano plot in fig. 6 shows the potential determining steps of both the dissociative and associative mechanism when using the free energy corrections calculated for the adsorbed reaction intermediates within the harmonic approximation. Leaving out the free energy corrections would yield a minor shift for the top of the volcano where the free energy for adsorbed an adsorbed nitrogen adatom moves from -0.5 eV to -0.6 eV while the onset potential moves up with 0.4 eV, see fig. 12 in the supplementary material. The potential determining step remains the same for the new volcano and the overall trend is the same, however NH$_3$ would be favored compared to HER. The fact that the top of the volcano is positioned close to the same free energy of adsorbed nitrogen adatom indicates that the overall trends for these very under-coordinated reaction sites are to a large degree independent on the calculated free energy corrections.
V. CONCLUSION

A theoretical analysis of the highly under-coordinated reaction sites of forming ammonia electrochemically on pure transition metal electrodes indicates that the associative mechanism could yield ammonia at an onset potential around -0.6 to -0.45 V with respect to SHE. Here, the hydrogen reaction will be a competing reaction and have a slightly lower onset potential and hence should be preferred. The most promising candidate for electrochemical ammonia production through the associative mechanism is Mo but closely followed by Fe. Alloys materials with reactivities between that of Mo, Fe and Ru could also be candidates, especially if they can hinder the HER and still be good catalysts for NH$_3$ production. Additionally, alloys with a reactivity such that the free energy of N adsorbed to the surface is in the vicinity of -0.5 eV. However, even at these very under-coordinated structures there is still a gap between HER and electrochemical ammonia production in terms of onset potential for the potential determining steps. Though this problem could potentially be solved by further utilizing the structure (in)sensitivity, this remains the main challenge for the electrochemical ammonia production.

For the dissociative mechanism a proposed onset potential of -0.5 to -0.1 could be obtained with a preferred ammonia production with respect to HER for the potential determining steps. However, for the dissociative mechanism N$_2$ dissociation barrier of splitting the N$_2$ molecule has not been included since this would require a purely thermally activated Langmuir-type mechanism for one elementary step combined with the electrochemical onset potential. Instead an estimate of the equilibrium of having N adatoms compared to N$_2$ molecules on the surface has been established and this will hence act as a cut-off for the noble metals and describe to some extent the limitations for these metals for the dissociation of a nitrogen molecule on the surface. The cutoff could vary depending on the detailed treatment from a free energy of N adatoms of -0.08 eV to 0.03 eV, which gives the overall uncertainty of approximately 0.1 V in onset potential for the potential determining steps.

ACKNOWLEDGMENTS

The authors would like to acknowledge the Danish Center for Scientific Computing for supercomputer access. The Center for Atomic-scale Material Design (CAMD) and the Catal-
ysis for Sustainable Energy (CASE) initiative is funded by the Danish Ministry of Science, Technology and Innovation. This work was funded in part by the U.S. Department of Energy under contract number DE-AC02-76SF00515.


[49] The GPAW code is available as a part of the CAMPOS software: http://www.camd.dtu.dk/Software.


[51] The ASE code is available as a part of the CAMPOS software: http://www.camd.dtu.dk/Software.


The onset potential for electrochemical ammonia production on transition metal nanoclusters, plotted as a function of the nitrogen binding energy.