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Design Study of 10 kW Superconducting Generator for Wind Turbine Applications

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Abstract—We have performed a design study of a 10 kW superconducting slow rotating generator suitable for demonstration in a small scale wind turbine, where the drive train only consists of the turbine blades connected directly to the generator. The flux density in the superconducting rotor is chosen as $B = 1$ Tesla to be similar to the performance of permanent magnets and to represent a layout, which can be scaled up in future off-shore wind turbines. The proposed generator is a 8 pole synchronous machine based on race-track coils of high temperature superconducting tapes and an air cored copper stator enclosed in an iron shield.

Index Terms—Superconductivity, synchronous generator, wind turbines.

I. INTRODUCTION

The challenges of future energy demand and the possible global warming due to fossil fuel consumption have increased the interest of large-scale use of wind turbines for electricity production. Most present turbines are operated on-shore, but the interference with the residents and higher wind speeds at sea is the motivation for building off-shore wind farms. A major fraction of the cost of off-shore farms is due to the foundations and volume can be reduced compared to a conventional generator and thereby simplifying the turbine design. The gearbox of present turbines can also be omitted by utilizing a multi-pole generator which is driven directly by the turbine rotor. We have done a design study of a 10 kW direct driven multi-pole superconducting generator, which can be installed in a small wind turbine and used to evaluate the robustness of the superconducting technology in a wind turbine environment, before the generator is scaled up by 3 orders of magnitude to the large scale turbines.

II. SMALL SCALE WIND TURBINES

Small wind turbines are commercially available and a wind turbine from Gaia-Wind [1] is operated at Risø-DTU [2]. It is a stall regulated turbine with a conventional drive train consisting of a gearbox and a fast rotating asynchronous generator with a power rating of 11 kW. This technology represents the first generation of drive trains, but direct driven synchronous generators based on permanent magnets such as Nd$_2$Fe$_{14}$B have recently been introduced even in small scale turbines [3]. A superconducting direct driven synchronous generator will represent a third generation of drive trains for wind turbines, since superconducting coils are expected to provide magnetic flux densities exceeding the operation flux densities of the permanent magnets. The specifications of a superconducting generator for a small scale wind turbine are outlined according to the properties of the Gaia wind turbine. A wind turbine converts the kinetic energy of the wind into electric energy and the power of the wind $P_{wind}$ is ideally given by [4]

$$ P_{wind} = \frac{1}{2} \rho A v_T^3 \omega C_P $$

where $\rho$ is the density of the air, $v_T$ is the average wind speed, $A_{rotor} = \pi R_{rotor}^2$ is the rotor area swept by the blades with a length of $R_{rotor}$ and $C_P$ is the power coefficient, which is determined by the aerodynamic properties of the rotor and is related to the number of blades, the shape of the blade and the blade angle with respect to the incoming wind. The power coefficient determines the fraction of the available kinetic energy, which is transformed into torque on the turbine shaft. It is often given as a function of the ratio $\lambda$ between the blade tip speed $v_T$ and the wind speed $v_0$

$$ \lambda = \frac{v_T}{v_0} = \frac{R_{rotor} \omega}{v_0} $$

where $\Omega$ is the angular speed related to the rotor frequency by $\Omega = 2 \pi f_{rotor}$.

The available wind power and the power curve of the Gaia turbine is shown on Fig. 1 as function of the average wind speed $v_0$. The $C_P$ curve has been plotted by assuming a constant rotation speed of 56 Revolutions Per Minute (rpm) and $R_{rotor} = 6.5$ m. It is seen that the nominal 11 kW power production is first reached when the wind speed exceeds the nominal wind speed of $v_0 = 9.5$ m/s. The Gaia wind turbine illustrate how the stall
regulation is obtained by the aerodynamic properties of the rotor and the rotation speed is fixed by the frequency of the electricity grid down scaled by the conversion factor of the gearbox. The available space in the nacelle is approximately a diameter of $D_{\text{nacelle}} = 0.8$ m and a length of $L = 1.0$ m. Large turbines today are pitch regulated by controlling the blade angle with respect to the incoming wind direction, whereby different power curves can be chosen. Additionally it becomes more common to decouple the generator frequency from the grid frequency by passing all the power of the turbine through power electronics consisting of two back-to-back coupled AC/DC converters. The generator of such a system can be of the synchronous type with the rotation speed controlled by the power electronics and this is also assumed to be the case for future superconducting wind turbine generators.

### III. Analytical Generator Model

We will use the analytical description of an air-cored synchronous machine [5], [6] to determine the properties of a slow rotating generator suitable for a gearless drive train of the Gaia turbine. The problem is only considered in the two dimensional rotation plane of the cylindrical machine, whereby the magnetic flux density distribution $B(\theta, r)$ can be determined from the axial component of the vector potential. A simple representation of the rotor and stator coils is obtained by introducing a sinusoidal turn distribution

$$\frac{d}{d\theta} n(\theta) = n_0 \sin(p \theta)$$  \hspace{1cm} (3)

where $\theta$ is the angle around the machine circumference as shown in Fig. 2, $p$ is the number of pole pairs and $n_0$ is the maximum winding density per circumference segment $dl = r d\theta$. Thus $n(\theta)$ gives the winding distribution, where the thickness of the winding layer is varying as a sinus function and the sheet current distribution is obtained by multiplying by the current $i$ in each wire. $I(\theta) = ni(\theta)$. However the sinusoidal turn distribution is often realized by a box distribution as illustrated on Fig. 2 and the prefactor of (3) is given by the first harmonic obtained from the Fourier transform of the box function.

The box function is specified as

$$n_b(\theta) = \begin{cases} n_0, & \frac{\pi}{2p} - \theta < \delta \theta_h \\ -n_0, & -\frac{\pi}{2p} - \theta < \delta \theta_h \end{cases}$$ \hspace{1cm} (4)

where $\delta \theta$ is half of the opening angle of the box region. By assuming a constant winding density per area $n_A$ then one can obtain the wire density per circumference segment $dl = r_0 d\theta$ from

$$n_0 = \frac{r_0}{r_0} \int_{\theta}^{\theta + t} n_A dr d\theta = n_A (t + 2r_0)$$ \hspace{1cm} (5)

where $t$ is the winding layer thickness and $r_0$ is the radius of the winding support.

The Fourier coefficients $b_k$ of the series representation $n(\theta) = \sum_{k=1}^{\infty} b_k \sin(k \pi \theta/\theta_{\text{max}})$ with $\theta_{\text{max}} = \pi/p$ then becomes

$$b_k = \frac{1}{\theta_{\text{max}}} \int_{\theta_{\text{max}}}^{\theta_{\text{max}}} n_b(\theta) \sin \left( \frac{k \pi \theta}{\theta_{\text{max}}} \right) d\theta$$ \hspace{1cm} (6)

Thus the first harmonic ($k = 1$) of the box function becomes

$$b_1 = \frac{4}{\theta_{\text{max}}} n_0 \sin(p \delta \theta_h) = \frac{4}{\pi} n_0 k_w$$ \hspace{1cm} (7)

where $k_w$ is called the fundamental harmonic winding factor [5]. The sheet current distribution then becomes

$$\frac{d}{d\theta} i(\theta) = b_1 i \sin(p \theta) = A \sin(p \theta)$$ \hspace{1cm} (8)

where $A$ is the sheet current density in the unit $[A/m]$ 

$$A = b_1 i = \frac{4}{\pi} n_0 k_w i$$ \hspace{1cm} (9)
A. Magnetic Flux Distribution

The flux distribution at \( r \) caused by the turn distribution (3) at \( r_0 \) and enclosed by an iron shield at \( r_{S2} \) has been derived analytically in [5]

\[
B_{r} = \frac{\mu_0 A}{2} \left( \frac{r_0}{r} \right)^{p+1} \left[ 1 + \eta \lambda_s \left( \frac{r}{r_{S2}} \right)^{2p} \right] \left\{ \cos(\phi) \sin(\theta) \right\}
\]

where \( \mu_0 \) is the vacuum permeability and the square bracket is the enhancement factor due to the iron shield. The factor \( \eta \lambda_s \) ranges between 0 and 1 in case of a fully saturated and infinitely permeable iron shield.

B. Machine Power

The output power of a synchronous machine consisting of a rotor and 3 stator turn distributions given by (3) at a radius \( r_R \) and \( r_S \) can now be calculated as

\[
P = \frac{\pi^2}{2} k_w B_{S0} A_S D^2 I_{gen} \eta_s
\]

where \( B_{S0} \) is the peak radial flux density at the stator winding at \( r_S \) [6]. \( A_S \) is the sheet current of the 3-phase stator windings and \( A_S = (3/2)A \) when the wire current \( i \) is an alternating current with root mean square amplitude \( i_{rms} \). The stator diameter \( D = 2r_S \) has been introduced, the effective length of the generator is \( L_{gen} \) and the rotation speed \( \eta_s \) in [revolutions s\(^{-1}\)]. Thus the output power of a 10 kW machine consisting of a superconducting rotor and Cu stator inclosed in an iron shield can now be calculated from a box representation of the windings. We are aiming for a rotor field at the stator radius of the order \( B_{S0} \sim 1 \text{T} \) to match the magnetic flux density obtained by permanent magnets. The generator must fit into the nacelle giving a diameter \( D = 0.56 \text{ m} \) and length of \( L_{gen} = 0.4 \text{ m} \). Finally a rotation speed of \( \eta_s = 56 \text{ rpm}/60 \text{s} \text{ min}^{-1} = 0.93 \text{ s}^{-1} \) results in a stator sheet current density \( A_S = 1.2 \times 10^6 \text{ Am}^{-2} \). The physical realization of such a machine is proposed below.

IV. GENERATOR LAYOUT

The coil geometry of a superconducting generator is restricted by the mechanical properties of the used superconducting wire and in the case of the ceramic high temperature superconductors (HTS) one can not bend the flat wires, which are often called tapes, on a diameter less than the critical bending diameter \( D_{cb} \). Typical bending diameters of HTS tapes are \( D_{cb,Bi2223} = 50-70 \text{ mm} \) for the Bi\(_2\)Sr\(_2\)Ca\(_2\)Cu\(_2\)O\(_{10-x}\) (B2223) tapes and \( D_{cb,BCO} = 25-35 \text{ mm} \) for YBa\(_2\)Cu\(_3\)O\(_{6+x}\) (YBCO) coated conductors. The tape thickness \( t_{tape} \) is \( 0.30-0.32 \text{ mm} \) typical including 100 \( \mu \text{m} \) plastic insulation wrapped around the wire. The width of the tape is typically \( w_{tape} = 4.3-4.5 \text{ mm} \) again including insulation. Thus the winding density of HTS tapes is typically, \( n_A = 7.3 \times 10^2 \text{ m}^{-2} \). Coils of HTS tape is often winded in the form of a double pan-cake coil with an inner diameter larger than the critical bending diameter \( D_{cb} \) and a thickness equal to \( 2w_{tape} \).

V. RESULTS AND DISCUSSION

The superconducting rotor coils are based on the race-track geometry, where the strait section is assumed to be the effective length of the machine, \( L_{gen} = 0.4 \text{ m} \), and the inner opening of the coil is determined by the bending diameter of the HTS tapes \( L_{air} = 0.08 \text{ m} > D_{cb} \) as illustrated on Fig. 3. The frequency \( f \) of the generator voltage and current is related to the synchronous rotation speed \( \omega \) and the number of pole pairs \( p \) in the generator \( f = p \Omega / 2 \pi = 3.7 \text{ Hz} \). Fig. 3 shows the 8 pole rotor coil geometry with each pole produced by a race-track coil consisting of two double pan-cakes. The thickness and width of the coil is \( t_c = 2.0 \text{ cm} \) and \( w_c = 5.0 \text{ cm} \) respectively. The positions of the rotor and stator windings are given in Table I, but the box representation of the rotor is assumed to span \( TRbox = 0.223-0.243 \text{ m} \) and the opening angle is \( \beta \theta = (\pi/2p)(2/3) \).

TABLE I

<table>
<thead>
<tr>
<th>Generator Dimensions</th>
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</thead>
<tbody>
<tr>
<td>Rotor</td>
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<tr>
<td>( r_{m1} = 0.200 \text{ m} )</td>
</tr>
<tr>
<td>( r_{R1} = 0.215 \text{ m} )</td>
</tr>
<tr>
<td>( r_{R2} = 0.250 \text{ m} )</td>
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</table>

The load line of the rotor coils is determined from the field and temperature dependent critical current \( I_C(H,T) \) of different tapes [7]–[9] by calculating the resulting flux density in the rotor coil from (10) when the \( I_C(H,T) \) at a certain field \( \mu_0 H_0 \) is inserted in the expression for the sheet current \( A \) given by (9). If the flux density produced by the coil exceeds the flux density used to determine the \( I_C \) then superconductivity is suppressed. Fig. 4 shows the maximum flux density along the \( \theta \) direction in the rotor coil as function of the field used to determine \( I_C \) and the critical region is at the left of the dashed line. The \( \theta \) component corresponds to the magnetic flux density perpendicular to the tape surface and will result in the lowest \( I_C \) due to the anisotropy of the critical current [10]. A safety margin of 50-80% of \( I_C \) must be applied to lower the probability of quenches of the rotor coils.

From Fig. 4 it is seen that the coated conductors will have a \( B_{mrel} = 0.5-0.8 \text{ Tesla} \) corresponding to an \( I_C = 50-120 \text{ A} \).
at $T = 75$ K and $T = 64$ K respectively. The large anisotropy of the Bi-2223 pinning properties makes operation at $T = 77$ K impossible due to the complete suppression of superconductivity when a magnetic flux component perpendicular to the tape is present. Thus a maximum flux density at the conductor of $B_{\text{max}} = 1$–3 T is possible with $I_C = 100$–550 A at $T = 50$ K and $T = 20$ K respectively. An operational engineering critical current of $I = 1.1 \cdot 10^4$ A cm$^{-2}$ is assumed to fulfill the safety margin and this will correspond to a wire current of $I = 150$ A. The corresponding sheet current (9) becomes $A_R = 2.5 \cdot 10^6$ A m$^{-1}$ and the maximum flux densities at the rotor coil and stator is predicted from (10) to become $|B|_{\text{rotor,max}} = 1.79$ T and $|B|_{\text{stator,max}} = 0.96$ T. Finite element calculation of the layout shown on Fig. 3 have confirmed the predicted flux densities and shows that the analytical box winding description is a good approximation of realistic superconducting coils.

### A. Stator Properties

The current of one stator phase winding $I_S$ can be determined by choosing a base voltage of $U_S = 400$ V/√3 = 231 V

$$P_{\text{phase}} = U_S I_S \Rightarrow I_S = \frac{P_{\text{phase}}}{U_S} = \frac{10 \text{ kW}/3}{231 \text{ V}} = 14.4 \text{ A} \quad (12)$$

By assuming a stator winding made of square copper wire with area $A_{Cu} = 5.3 \text{ mm}^2$ then one can determine the wire area density needed to obtain a sufficient stator sheet current $A_S$. First $A_S$ is calculated from the rotor flux density found in the previous section and the output power given by (11)

$$A_S = \frac{\sqrt{2}}{\pi^2} k_{\text{cu}} B_{\text{SO}} D^2 L_{\text{gen}} n_S = 1.5 \cdot 10^4 \text{ Am}^{-1} \quad (13)$$

The stator wire density is then determined from (5), (7) and (9) applied to the stator geometry

$$n_{A_S} = \frac{\pi}{2 \left(t + 2r_{S1}\right)} k_{\text{Cu}} S I_S = 1.0 \cdot 10^5 \text{ windings m}^{-2} \quad (14)$$

which correspond to approximately 20% of the stator area for epoxy. The resistance of the stator is estimated to be $R_S = 4.06 \Omega$ which will give a stator loss of $P_{\text{Cu}} = R_S I_S^2 = 842$ W and a stator efficiency of 0.92.

### B. Wire Length and Generator Weight

The estimated length of the wires needed for the generator is shown in Table II. The weight has been estimated by assuming that the density of the HTS superconductor tapes is either equivalent to a 70/30 ratio of silver and Bi2223 or to pure nickel representing the coated conductors. Additionally the weight of the rotor support is estimated from the density of glass fiber. It is seen that the choice of a high rotor flux density comes at the price of a larger amount of superconductor in the rotor than copper in the stator. Thus from an economical point of view it would be desirable to replace some superconductor by Cu in the stator, but the present design is focused on demonstrating a superconducting coil layout, which can be scaled up to larger power ratings in future off-shore turbines. It is interesting to note that the total weight of Table II is $W_{\text{total}} = 449$ kg, which must be compared to 300 kg of gearbox and generator in the Gaia turbine. An increase of the drive train weight is often seen when changing to direct drive, but it is expected that the superconducting machines will become lighter than the conventional at high power ratings [11].

## VI. Conclusion

We have shown a possible design of a direct driven 10 kW superconducting 8 pole synchronous generator based on 7.5 km of high temperature superconductor tape and that this generator might be demonstrated in a small scale wind turbine. An optimization of the generator is needed as a next step as well as the design of a cryogenic cooling system. The operation temperature will be determined by the trade off between higher engineering critical current density $J_C$ at low temperatures and the power loss of the cooling system. However tapes with higher $J_C$ would be needed if the operation temperature should be increased up to $T = 50$ K.
REFERENCES


