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Evolution of magnetic states in frustrated diamond lattice antiferromagnetic Co(Al$_{1-x}$Co$_x$)$_2$O$_4$ spinels

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Using neutron powder diffraction and Monte Carlo simulations we show that a spin-liquid regime emerges at all compositions in the diamond-lattice antiferromagnets Co(Al$_{1-x}$Co$_x$)$_2$O$_4$. This spin-liquid regime induced by frustration due to the second-neighbor exchange coupling $J_2$ is gradually superseded by antiferromagnetic collinear long-range order ($k=0$) at low temperatures. Upon substitution of Al$^{3+}$ by Co$^{3+}$ in the octahedral B site the temperature range occupied by the spin-liquid regime narrows and $T_N$ increases. To explain the experimental observations we considered magnetic anisotropy $D$ or third-neighbor exchange coupling $J_3$ as degeneracy-breaking perturbations. We conclude that Co(Al$_{1-x}$Co$_x$)$_2$O$_4$ is below the theoretical critical point $J_3/J_1=1/8$, and that magnetic anisotropy assists in selecting a collinear long-range ordered ground state, which becomes more stable with increasing $x$ due to a higher efficiency of O-Co$^{3+}$-O as an interaction path compared to O-Al$^{3+}$-O.

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I. INTRODUCTION

Magnetic systems with frustration induced by competing exchange interactions quite often manifest unconventional ground states, the most intriguing of which are spin liquids.1 Recently one such exotic state, a “spiral spin liquid,” was uncovered theoretically in a classical treatment of diamond-lattice Heisenberg antiferromagnets (AFM) by Bergman et al.,$^2$ who showed that competition between nearest and next-nearest-neighbor exchange couplings $J_1$ and $J_2$ creates—for $J_2/J_1 > 1/8$—a highly degenerate ground state consisting of a set of coplanar spirals, whose propagation vectors form a continuous surface in momentum space. The frustration results in a rich phase diagram as a function of the ratio $J_2/J_1$. The degeneracy of these ground states can be lifted by thermal or quantum fluctuations leading to an “order-by-disorder” phase transition from a spiral spin-liquid regime to an ordered state.

Among the diamond-lattice AFMs, compounds with the spinel structure recently attracted much attention.$^{4–6}$ In particular, Co-Al oxides were considered as promising candidates for study of order-by-disorder physics.$^{2,3}$ In these compounds of general stoichiometry AB$_2$O$_4$ the tetrahedral A sites are occupied by high-spin ($S=3/2$) magnetic Co$^{3+}$ ions which form a diamond lattice consisting of two interpenetrating face-centered cubic sublattices coupled antiferromagnetically. The octahedral B sites can be filled either by nonmagnetic Al$^{3+}$ ions and/or by low-spin ($S=0$) nonmagnetic Co$^{3+}$ ions.

Existing experiments on Co-Al oxide spinels do not provide a clear picture. An early neutron-diffraction study$^7$ on Co$_2$O$_4$ showed that the magnetic moments of the Co$^{3+}$ ions located at the tetrahedral sites form a simple collinear AFM below the Neel temperature $T_N=40$ K. This picture has been questioned by a recent muon spin rotation and relaxation ($\mu$SR) study$^8$ which found two frequency components near $T_N$ suggesting incommensurate magnetic order. Experimental observations on CoAl$_2$O$_4$ are also contradictory. A powder neutron-diffraction study of Roth$^9$ suggested long-range AFM order below 4 K, while Krimmel et al.$^{10}$ detected a spin-liquid (or glassylike) ground state. Electron spin resonance, magnetization and specific-heat measurements identified the ground state of CoAl$_2$O$_4$ as spin glasslike with a high-frustration parameter $|J_{CH}/T_N|$ of 22 (Ref. 11) and 10 (Ref. 12), respectively. These experimental results are consistent with the calculations of Bergman et al.$^{2}$ which placed CoAl$_2$O$_4$ in the region of $J_2/J_1=1/8$ where the surface spiral begins to develop. To clarify the situation, it is essential to understand whether the ground state of Co$_2$O$_4$ is a simple collinear antiferromagnet and if CoAl$_2$O$_4$ is a spiral spin liquid fluctuating among degenerate spirals. It is also important to understand why substitution within the nonmagnetic B site changes the magnetic properties so drastically. Tristan et al.$^{13}$ attempted to answer these questions based on bulk macroscopic measurements of Co(Al$_{1-x}$Co$_x$)$_2$O$_4$ system. They proposed that the spin-liquid state is realized in CoAl$_2$O$_4$($x=0$), while with increasing Co substitution $x$ the second-neighbor coupling $J_2$ decreases and collinear AFM long-range order develops.

In this work we address these important issues and refine the evolution of the magnetic states in Co(Al$_{1-x}$Co$_x$)$_2$O$_4$ spinels by means of neutron powder diffraction supported by Monte Carlo simulations.$^{14}$ Our analysis reveals that for $x = 0$ the system is close to the critical point $J_2/J_1=1/8$ in the phase diagram while frustration is weaker for $x > 0$. We argue that magnetic anisotropy assists in the selection of a collinear long-range ordered ground state. The difference in $T_N$ and in the extent of the spin-liquid regime apparently
concluded that the Co$^{3+}$ ions are homogeneously and randomly distributed over the B sites. This follows because the Curie-Weiss temperature reflecting short-range magnetic order start to develop below the Curie-Weiss temperature $|\theta_{\text{CW}}|=110$ K$^{10}$ they narrow and shift to higher sin $\theta/\lambda$ with cooling (Fig. 1). Approaching $T_N$ the diffuse scattering localizes near the $\langle 111 \rangle$ and $\langle 200 \rangle$ positions. Below $T_N$ the liquidlike features remain but gradually lose spectral weight as magnetic Bragg peaks due to long-range order develop. The spectral weight of the diffuse scattering component continuously increases from Co$_3$O$_4$ to CoAl$_2$O$_4$ (Fig. 2) as the frustration parameter $|T_{\text{CW}}|/T_N$ grows. We can quantify it by the area of a Lorentzian fitted to the first diffuse bump. As shown in the inset of Fig. 2 this area is largest roughly at $T/T_N \approx 1$ for all compositions, but for $x=0$ and 0.35 diffuse scattering develops far above and remains significantly below this value. For $x=1$ the $T/T_N$ interval revealing diffuse scattering is narrower but still much too large to be interpreted as classical critical scattering of a three-dimensional long-range ordered magnet.

Regarding the long-range order, all samples show magnetic Bragg peaks at low temperatures. The ordering temperature $T_N$ and the static ordered magnetic moment decrease from Co$_3$O$_4$ to CoAl$_2$O$_4$ (see Table I and inset of Fig. 1). It should be noted that the $x=0$ diffraction pattern does not correspond to a conventional long-range ordered state: diffuse scattering clearly dominates and the $\langle 200 \rangle$ peak is so broad and weak that the ordered moment cannot be determined with high accuracy. Nevertheless, the magnetic Bragg pattern is the same for all compositions and is consistent with the collinear two-sublattice model proposed by Roth.$^7$

### III. MODELING

To model the observed magnetic diffuse scattering we used the quasistatic approximation,$^{15}$ which assumes that the spectral weight of the diffuse scattering component continuously increases from Co$_3$O$_4$ to CoAl$_2$O$_4$ (Fig. 2) as the frustration parameter $|T_{\text{CW}}|/T_N$ grows. We can quantify it by the area of a Lorentzian fitted to the first diffuse bump. As shown in the inset of Fig. 2 this area is largest roughly at $T/T_N \approx 1$ for all compositions, but for $x=0$ and 0.35 diffuse scattering develops far above and remains significantly below this value. For $x=1$ the $T/T_N$ interval revealing diffuse scattering is narrower but still much too large to be interpreted as classical critical scattering of a three-dimensional long-range ordered magnet.

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We found that for the range 0 < J_2/J_1 < 1/8 the collinear AFM configuration more stable. For this we considered separable terms so that the AFM minimum would be deeper and the energy decrease corresponding to the ground state for J_2/J_1 = 1/8 is extremely flat around the q=0 point of the first Brillouin zone, and therefore, very many states are in the range of thermal excitation at any accessible temperature.

The MCGS starts closely related to the collinear AFM state, but progressively departs from it with increasing J_2/J_1. This is clearly seen in the decay of spin correlations, which is justified since the bandwidth of magnetic excitations is below 6 meV whereas all scattering with energies below 14.7 meV is summed in our diffraction experiment. We performed a Monte Carlo search for the ground state of a cluster of 1047 atoms. The energy of the classical Heisenberg Hamiltonian for spins S interacting with first- and second-neighbor antiferromagnetic couplings J_1, J_2 > 0

\[ H = J_1 \sum_{i<j} S_i \cdot S_j + J_2 \sum_{i<j} S_i \cdot S_j \]

was minimized (i,j) means that the sum runs over first-neighbor pairs, \( \langle i,j \rangle \) on second-neighbors pairs). If we add either a third-neighbor interaction or an anisotropy contribution, the Hamiltonian will be completed with an additional term \( \Delta H \), given, respectively, as

\[ \Delta H = J_3 \sum_{(i,j,j')} S_i \cdot S_j \cdot S_j' \text{ (third neighbor);} \]

\[ \Delta H = D \sum_i (S_i \cdot u)^2 \text{ (anisotropy),} \]

where \( \langle\langle i,j \rangle \rangle \) refers to third-neighbors pairs and \( u \) is the magnetic anisotropy term, that we took as (111). D is the magnitude of the anisotropy term. The moments were kept equal and constant in magnitude; their direction was changed at random, one at the time, and to obtain the ground state only energy-decreasing moves were accepted in the final stage. The stopping criterion for the Monte Carlo was that the last 1000 accepted configurations had an energy spread less than 10^{-6}J_1. Runs have been repeated for the whole range 0 ≤ J_2/J_1 ≤ 1. We calculated the static spin-pair correlation functions and diffraction patterns for the Monte Carlo ground state (MCGS) and the reference AFM clusters for each J_2/J_1. The correlation function is given by

\[ CF(d) = \frac{2}{3} \sum_{ij} S_i \cdot S_j \delta(|r_i - r_j| - d), \]

where \( d \) is the distance between spins at positions \( r_i \) and \( r_j \). We found that for the range 0 < J_2/J_1 < 1/8 the collinear AFM is the ground state, in agreement with Ref. 2. Remarkably, the MCGS was always configurationally different from a collinear AFM state even if the energy difference was negligible (order of 1 mK or less). Analytical calculations (Fig. 3 inset), similar to Ref. 2, support this result. In fact, the energy minimum corresponding to the ground state for J_2/J_1 < 1/8 is extremely flat around the q=0 point of the first Brillouin zone, and therefore, very many states are in the range of thermal excitation at any accessible temperature.
model we described anisotropy as a single-ion parameter \( D \). The MC procedure was now changed, allowing for system equilibrations at different temperatures. All moves that would decrease the energy or that would increase it with probability \( e^{-\Delta E/T} \) were accepted.\(^8\) When the average and fluctuations of the energy of a large number of the last accepted states were sufficiently stable the temperature was changed. Fixing \( J_1 = 1 \) as a convenient energy scale, \( J_2, J_3, D \), or \( T \) were varied, each in several steps.

Equally good fits were obtained with \( J_1 \) and magnetic anisotropy \( D \) as perturbations, signifying that the available diffraction data are not sufficient to determine which of these terms stabilizes the ordered ground state. However, we give preference to the magnetic anisotropy following the theoretical study of Ref. 17. The best fits presented in Fig. 4 (bottom) suggest the ratio \( J_2/J_1 = 0.125 \) for CoAl\(_2\)O\(_4\) and \( J_2/J_1 = 0.05 \) for Co\(_3\)O\(_4\). The change in the exchange energy with substitution apparently originates from the peculiarities of the electronic structure. Band-structure analysis\(^9\) shows that near the Fermi level in Co\(_2\)O\(_4\) there are Co\(^{3+}\) d and oxygen p states, while in CoAl\(_2\)O\(_4\) the Al p states are absent from the Fermi level and the weight of O p is diminished. This implies that the interaction path O-Co\(^{3+}\)-O is more effective and the corresponding exchange integrals are larger in Co\(_2\)O\(_4\).

Our findings give a natural explanation of the \( \mu \)SR results\(^8\) on Co\(_3\)O\(_4\) as due to spin-liquid physics rather than incommensurate magnetic order. Also, based on the position of CoAl\(_2\)O\(_4\) in the \( J_2/J_1 \) phase diagram, we suggest that even in an ideal sample, with no inversion or other perturbation, the ground state would be a collinear AFM, though one might need very low temperatures to reach it. As the ground state is the collinear AFM the general term “spin liquid” and not “chiral spin liquid” is appropriate for the high-temperature regime above \( T_N \) in the title system.

A single-crystal inelastic neutron-scattering experiment would allow to extract the absolute values of \( J_1, J_2 \) and to validate our conclusions. We remark that the elaborated approach to fit measured diffuse magnetic neutron scattering to Monte Carlo simulations can be easily adapted to other frustrated systems and would be useful in justification of an anticipated Hamiltonian.

IV. SUMMARY

In summary we studied the evolution of magnetic states in Co(Al\(_{1-x}\)Co\(_x\))\(_2\)O\(_4\) polycrystalline samples with temperature and substitution in the B site. We observed short-range and long-range orders for all compositions. Employing Monte Carlo simulations we found that for \( x = 0 \) the system is in the vicinity of the critical point \( J_2/J_1 = 1/8 \), where the spiral spin liquid develops,\(^2\) but stays in the weakly frustrated limit for \( x > 0 \). We also found that replacement in the nonmagnetic B site changes the strength of exchange interactions which, in turn, leads to significant differences in the ordering temperatures and in the extent of the spin-liquid regime.

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16 \( \Delta E \equiv E_{\text{last trial}} - E_{\text{last accepted}} \)