Coupling between angled-facet amplifiers and tapered lens-ended fibers

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Abstract—The coupling between angled-facet amplifiers and tapered lens-ended fibers is investigated theoretically and experimentally. The theoretical investigation is based on a three-dimensional plane wave model which accounts for the phase differences introduced by the angled facets. The coupling is investigated with respect to the beam parameters of the amplifier waveguide and the tapered lens-ended fiber, and also with respect to the fiber position. The excess coupling losses due to the facet angle and due to the variation of the fiber lens radius are investigated theoretically and found to be in good agreement with experimental results. For optimized lens radii the excess loss for a 10° facet angle is found to be less than 0.5 dB compared to a normal facet amplifier.

I. INTRODUCTION

Semiconductor laser amplifiers will be employed in many types of optical systems if a high fiber-to-fiber gain and a low-gain ripple can be obtained. Obviously, good coupling between the fiber and the amplifier together with low-facet reflectivities is important. It should also be pointed out that a high-input coupling efficiency is important to obtain a low-effective noise figure in the amplifier. In this paper we report on the coupling efficiency between angled-facet amplifiers and optical fibers. Previously, work on coupling to normal facet diodes was published [11]-[14].

The angled-facet amplifier is very attractive due to its inherently low modal reflectivity [5]. However, the angled facet modifies the radiated far-field pattern from the amplifier. Its influence on the coupling efficiency is here investigated as a function of the facet angle and the beam parameters of the amplifier, and also with respect to the position and the direction of the fiber relative to the amplifier. The theoretical predictions are compared with experimental results, and good agreement is obtained.

The paper is organized as follows: the far-field patterns of the angled-facet amplifier and the tapered lens-ended fiber are described in Sections II and III, respectively. Results for the coupling efficiency are given in Section IV, while Section V gives the conclusion.

II. FAR-FIELD PATTERN OF ANGLED-Facet AMPLIFIERS

In this section, an approximate analysis of the far-field pattern of angled-facet amplifiers will be presented. It is assumed that the waveguide of the amplifier supports only the fundamental modes.

Here we will only consider the TE00 mode but expressions for the TM00 mode would be easy to derive. The field distribution inside the waveguide is described by a Gaussian function

$$E(x, y, z) = \exp \left( -\frac{x^2}{W_x^2} - \frac{y^2}{W_y^2} \right) \cdot \exp \left( -jk_z z \right)$$

where the xyz coordinate system is as shown in Fig. 1(a), $W_x$ and $W_y$ in (1) are the parameters for the 1/e beamwidths in the x and y directions. $k_z$ is the wave number in the z direction. For convenience, the reference plane is now chosen parallel to the facet of the amplifier and taking the phase difference between the different plane wave components into consideration, (1) is transformed into

$$E(x', y', 0) = \exp \left( -\frac{x'^2}{W_x^2} \right) \cdot \exp \left( -\frac{y'^2 \cos \theta_0}{W_y^2} \right) \cdot \exp \left( -jk_y y' \sin \theta_0 \right)$$

Here $\theta_0$ is the tilt angle as shown in Fig. 1(a).

The field of (2) can be represented as the Fourier transformation of an angular spectrum $F(\alpha', \beta')$ of plane waves incident at different directions ($\alpha', \beta'$)

$$F(\alpha', \beta') = \frac{\pi W_x W_y n_i^2}{\lambda^2 \cos \theta_0} \exp \left( -\frac{\pi^2 n_i^2 \alpha^2 W_x^2}{\lambda^2} \right) \cdot \exp \left( -\frac{\pi^2 n_i^2 W_y^2}{\lambda^2} \left( \gamma \sin \theta_0 + \beta \cos \theta_0 \right)^2 \right)$$

Here $\alpha'$, $\beta'$, and $\gamma'$ are the directional cosines of the coordinate system x'y'z', and $\lambda$ is the wavelength of the light. $n_i$ is the effective refractive index of the waveguide [6] given by

$$n_i^2 = \frac{\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} n^2(x', y') E^2(x', y') \, dx dy}{\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} E^2(x', y') \, dx dy}$$

When a plane wave component incident at ($\alpha', \beta'$) passes the coating layer both its amplitude and its direction of propagation change. The direction changes according to Snell's law (see Fig. 1(b)), whereas the change in the amplitude is given by the Fresnel transmission and reflection coefficients. Thus, the plane wave spectrum $F_s(\alpha', \beta')$ after the coating is given by [7]

$$F_s(\alpha', \beta') = F(\alpha', \beta') \frac{t_{12}(\alpha', \beta') t_{23}(\alpha', \beta') \exp \left( jB(\alpha', \beta') \right)}{1 + r_{12}(\alpha', \beta') r_{23}(\alpha', \beta') \exp \left( j2B(\alpha', \beta') \right)}$$

$$B(\alpha', \beta') = \frac{\pi n_i^2}{\lambda} \left( \gamma \sin \theta_0 + \beta \cos \theta_0 \right)$$

$$\alpha = \frac{\pi n_i^2}{\lambda} \gamma \sin \theta_0$$

$$\beta = \frac{\pi n_i^2}{\lambda} \beta \cos \theta_0$$

$$\theta_0 = \frac{\lambda}{n_i}$$
where \( t_{12}(\alpha', \beta') \) and \( r_{12}(\alpha', \beta') \) are the Fresnel transmission and reflection coefficients between region 1 and region 2, and \( t_{23}(\alpha', \beta') \) and \( r_{23}(\alpha', \beta') \) are those for region 2 and region 3 while \( B \) is given by

\[
B = \frac{2\pi n_2^2}{\lambda} h \sqrt{1 - \alpha'^2 - \beta'^2}. \tag{6}
\]

In (6) \( n_2 \) is the refractive index and \( h \) is the thickness of the coating layer.

According to [8], the far-field pattern \( S(\alpha', \beta') \) is expressed as

\[
S(\alpha', \beta') = C_1(1 - \alpha'^2) |F_\alpha(\alpha', \beta')|^2 \tag{7}
\]

where \( C_1 \) is a constant.

We have calculated the far-field pattern of an angled-facet amplifier in the direction parallel to the junction plane for different angles \( \theta_o \) between the waveguide and the facet normal. As shown in Fig. 2(a) the far-field pattern of the TE\(_{00} \) mode is not Gaussian distributed, but is becoming increasingly asym-

### III. FAR FIELD OF TAPERED LENS-ENDED FIBER

In this section, we will discuss the far-field pattern of a tapered lens-ended fiber as shown in Fig. 4. The mode conversion in the taper and the lens is studied with the beam propagation method (BPM) which allows for a numerical calculation of the field. The BPM solves the scalar-wave equation [11] in small propagation steps along the fiber taper axis. In each step the input field is propagated first through a homogeneous medium with an effective refractive index and second through an infinite thin lens correcting for the index variation during the step. It should be added that an analytical solution for the field in the taper section is difficult to obtain.

The tapered lens-ended fibers are fabricated from standard silicon fibers with taper lengths of about 300 \( \mu \)m and lens radii of about 15 \( \mu \)m. The transverse diameter of the fiber taper is linearly changed (see Fig. 4) along the axial direction of the fiber and the optical field distribution in the \( x'y'z' \) plane is taken as a Gaussian function with a flat phase front. The beamwidth \( W_{f0} \) is estimated by [12]

\[
W_{f0} = a \left( 0.65 + \frac{1.619}{\nu^{2/3}} + \frac{2.879}{\nu^{1/3}} \right) \tag{9}
\]
Fig. 4. Schematic of a tapered lens-ended fiber.

Fig. 5. The 1/e beamwidth of the local mode of the tapered lens-ended fiber versus the position along the fiber axis.

Fig. 6. Phase conversion by the fiber lens, calculated by BPM (---) and the simple method (---).

Fig. 7. Calculated (---) and measured (---) far-field pattern of the tapered lens-ended fiber.

where $a$ is the radius of the fiber core, and $V$ is given by

$$V = (n_f^2 - n_i^2)k^2a^2$$  (10)

$n_i$ and $n_f$ are the refractive indices of the fiber core and the cladding layer. As the optical field propagates from the AA$_1$ plane to the BB$_1$ plane (see Fig. 4), it spreads out and the beamwidth increases along the fiber taper as shown in Fig. 5. Passing through the fiber lens the concave phase front is changed into a convex (see the solid curves in Fig. 6), however, the beamwidth of the field in the CC$_1$ plane is about same as in the BB$_1$ plane.

The far-field pattern is calculated from a Fourier transformation of the field distribution in the CC$_1$ plane [8] as shown in Fig. 7 by the dotted curve. The good agreement with the measured far field given by the solid curve supports the validity of the BPM calculation. The 1/e beamwidth in the CC$_1$ plane is $W_f = 8.8 \mu m$.

The BPM requires a long computation time, so for an investigation of the influence of the fiber lens radius on the coupling efficiency we have investigated the possibility of considering the lens as a phase delay only. The dotted curve in Fig. 6 gives the phase distribution which results from this procedure and as can be seen it is in good agreement with the phase distribution resulting from the BPM calculation.

IV. COUPLING BETWEEN AMPLIFIER AND FIBER

In this section the coupling efficiency between tapered lens-ended fibers and angled-facet amplifiers is investigated theoretically and experimentally. The investigation is concerned with the influence of the beam parameters of the tapered lens-ended fiber and of the amplifier, the fiber position, and direction. The excess coupling losses due to the facet angle and due to the variation of the fiber lens radius are also investigated.

V. ANALYSIS

The schematic of the coupling from an angled-facet amplifier to a tapered lens-ended fiber is shown in Fig. 8. The reference plane for the analysis is chosen at the tip of the fiber as indicated. The coupling efficiency $K_i$ can be expressed by the overlap integral between the fields $E_a$ and $E_f$ of the amplifier and the fiber taken in the reference plane

$$K_i = \frac{\int \int_{-\infty}^{\infty} E_a(x_1, y_1) E_f^*(x_1, y_1) \, dx_1 \, dy_1}{\int \int_{-\infty}^{\infty} |E_a(x_1, y_1)|^2 \, dx_1 \, dy_1 \int \int_{-\infty}^{\infty} |E_f(x_1, y_1)|^2 \, dx_1 \, dy_1}$$  (11)

The field distribution of the tapered lens-ended fiber $E_f$ is obtained from the BPM calculation as described in Section III. The field distribution $E_a(P_0)$ of the angled-facet amplifier in the reference plane, is given by [13]

$$E_a(P_0) = \int \int S h(P_0, P_1) E(P_1) \, dS_1$$  (12)

where $E(P_1)$ is the field distribution at the facet as given by (2), $S$ designates the reference plane, and $h(P_0, P_1)$ is given...
the experiment, the tapered lens-ended fiber is coupled to one end of the amplifier as a function of the lens radius of the tapered lens-ended fiber. The solid curve in Fig. 11 gives the theoretical results and the experimental results in Fig. 9.

The coupling efficiency estimated by (11) will be modified by the Fresnel reflection at the lens surface to give the coupling efficiency

\[ K = K_I + \Delta K \]

where \( \Delta K \), which is due to the Fresnel reflection, is a function of the beam parameter of the amplifier, the lens radius, and the index of the fiber. For lenses with a radius larger than the core diameter of the fiber, the excess coupling loss is approximately 0.4 dB [16].

VI. RESULTS

In the calculations we simulated the angled-facet ridge waveguide amplifiers for which good performance has been obtained in our previous experiments [5]. The \( 1/e \) widths \( W_x \) and \( W_y \) for the beam of the amplifier are determined from measurements of the far-field pattern. The estimated values for \( W_x \) and \( W_y \) are 0.6 and 1.3 \( \mu \)m, respectively, and the effective refractive index obtained from (4) is 3.28 [17]. As mentioned in Section III the \( 1/e \) width for the beam of the tapered lens-ended fiber in the reference plane is \( W_y = 8.8 \mu \)m.

Fig. 9 gives the coupling efficiency versus the angle \( \theta \) between the fiber and the facet normal of the amplifier. Amplifiers with facets angled at \( \theta_f = 7^\circ \) and \( \theta_f = 10^\circ \) and fibers with a lens radius of 15 \( \mu \)m are considered. For each value of \( \theta_f \) the distance between the fiber and the amplifier is optimized for maximum coupling efficiency. In the case of an amplifier with a facet angle of \( \theta_f = 7^\circ \) the calculated coupling efficiency is approximately -7.5 dB in the direction of the facet normal while it can be as high as -2.7 dB for \( \theta_f = -34^\circ \). For an amplifier with a 10° facet angle the highest coupling efficiency is approximately -2.9 dB for an angle of \( \theta_f = -34^\circ \). The experimental results obtained from spontaneous emission measurements for the 7° and 10° amplifiers are given by circles and squares. The maximum coupling efficiencies are -3.5 and -3.8 dB in the two cases. In the experiment, the tapered lens-ended fiber is coupled to one facet of the amplifier, while a broad-area detector which collects all the light is used at the other facet (equal power from both facets). The coupling efficiency measured for the spontaneous emission from the amplifier depends on the bias current of the amplifier, especially at a low current level, as shown in Fig. 10. When the bias current changes from 50 mA to 150 mA, the coupling efficiency increases approximately 1.5 dB. A further increase of the bias current will not increase the coupling. This current dependence of the coupling efficiency is due to the fact that the amplified spontaneous emission does not exist inside the amplifier as a single well-defined guided mode for low gain. However, for high gain most of the amplified spontaneous emission is guided in the fundamental mode at the output facet. In Fig. 10 we also show the coupling efficiency for the signal (shown as \( \bullet \) in Fig. 10), which is measured as follows: a chopped signal is coupled to one facet of the amplifier while a broad-area detector collects all the amplified signal at the other facet. The coupling efficiency can be estimated from comparison of the power measured with the broad-area detector to the power measured when the tapered lens-ended fiber collects the amplified signal. The coupling efficiency for the signal is about 0.5 dB higher than the coupling efficiency for the spontaneous emission at a high-bias current level. The lower coupling efficiency for spontaneous emission is attributed to chromatic aberration. This can partly explain the difference between the theoretical results and the experimental results in Fig. 9.

We have investigated the excess coupling loss for the 10° amplifier as a function of the lens radius of the tapered lens-ended fiber. The solid curve in Fig. 11 gives the theoretical result, which predicts the highest coupling efficiency for a lens.
radius of 11 μm. As seen, the excess coupling loss varies slowly with the lens radius, and for lens radii of 6 and 20 μm the excess coupling losses are 1.1 and 2.3 dB, respectively. Similarly, for Rf = 10 μm, the excess coupling loss will be 0.2 and 0.5 dB. The experimental results are in agreement with the numerical results within 0.2 dB. Similarly, Fig. 12(b) and (c) gives the dependences of the excess coupling on facet angle with Rf as a parameter, Wy = 6 μm (---), Wy = 7.5 μm (-----), and Wy = 9 μm (-------). (c) The excess coupling loss versus the facet angle of the angled-facet amplifier with the 1/e beamwidth of the amplifier in transverse direction Wy as a parameter, Wy = 1.0 μm (---), Wy = 1.3 μm (-----), and Wy = 1.6 μm (-------).}

The coupling efficiency versus the separation between a 7° angled-facet amplifier and a tapered lens-ended fiber is shown in Fig. 13, with the fiber in the direction of θy = -24°. The three curves are for Rf = 6, 12, and 20 μm. The coupling efficiency reaches the maximum values for separations of 9, 23, and 44 μm, respectively. Our results are in qualitative agreement with the experimental results published in [1] for coupling to a laser diode. Especially, our model explains the behavior of the coupling efficiency for a short fiber-amplifier distance.

The coupling efficiency versus the displacement in the y, direction (see Fig. 8) is also investigated. The sensitivity is nearly the same in the x, and the y, directions and as an example Fig.
C. Vasallo, "Gain ripple minimisation and higher order modes pling loss of less than 0.5 dB for the lateral direction was studied theoretically.

due to the variation of the fiber lens radius, were also investi-
tagions. Coupling efficiency to amplifiers with facet angles of 7 and 10 were investigated experimentally, and maximum coupling efficiencies of -3.5 and -3.8 dB were obtained in the fibers and also with respect to the fiber position and direc-
tions. Coupling efficiency to amplifiers with facet angles of 7 and 10 were investigated experimentally, and maximum coupling efficiencies of -3.5 and -3.8 dB were obtained in the two cases with the fiber angle at -23.6 and -34.5, respectively. The excess coupling losses, due to the facet angle and due to the variation of the fiber lens radius, were also investigated theoretically and experimentally. With an excess coupling loss of less than 0.5 dB for the 10° angled amplifier, this structure is considered very attractive for fabrication of traveling wave amplifiers. Furthermore, the coupling sensitivity in the lateral direction was studied theoretically.

VII. CONCLUSION

We have established a theoretical model which allows calculation of the coupling efficiency between an angled-facet amplifier and a tapered lens-ended fiber. The coupling efficiency was investigated theoretically with respect to the beam parameters of the amplifiers and the fibers as well as the lens radii of the fibers and also with respect to the fiber position and directions. Coupling efficiency to amplifiers with facet angles of 7 and 10° were investigated experimentally, and maximum coupling efficiencies of -3.5 and -3.8 dB were obtained in the two cases with the fiber angle at -23.6° and -34.5°, respectively. The excess coupling losses, due to the facet angle and due to the variation of the fiber lens radius, were also investigated theoretically and experimentally. With an excess coupling loss of less than 0.5 dB for the 10° angled amplifier, this structure is considered very attractive for fabrication of traveling wave amplifiers. Furthermore, the coupling sensitivity in the lateral direction was studied theoretically.

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REFERENCES


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