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Experimental analysis of pilot-based equalization for probabilistically shaped WDM systems with 256QAM/1024QAM

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Abstract: Pilot based equalization is studied in a 5x10 GBaud WDM transmission experiment. The equalization is independent of the modulation format and is demonstrated for 256/1024QAM with uniform and probabilistically optimized distribution using an optimized pilot insertion rate of 2-5%.

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1. Introduction
The advancement of coherent communications in recent years has enabled modulation formats with high spectral efficiency, such as high-order quadrature amplitude modulation (QAM), to become a major focus of the optical communications community. Such modulation formats, while theoretically sound, pose significant challenge for practical implementation due to the requirement for high optical signal-to-noise ratio (OSNR). Furthermore, optical communications are pushed to operate at lower OSNR and with higher forward error-correction (FEC) overhead in order to operate closer to the optimal OSNR/data rate trade-off (also known as the channel capacity in this context). Time-domain equalization in current receivers relies on the simple constant modulus algorithm (CMA) for QPSK constellations and its modification for QAM - the multi-modulus algorithm (MMA) [1]. The most popular MMA must first decide what amplitude each symbol should have, and then optimizes the equalizer w.r.t. the error between the actual received symbols and the so-defined radius [2]. This is also known as radius directed equalization (RDE). In order to operate near-optimally, the MMA requires that most of the decisions are correct, which is a strong requirement, especially in the lower OSNR/high FEC overhead operating points. Additionally, MMA also poses challenges for advanced modulation formats, e.g. probabilistic constellation shaping formats [3, 5], in which case some of the radii are sparsely populated by the input sequence, thus deteriorating the MMA performance. In order to study the performance of such formats, modulation format- and SNR-independent equalization methods are required.

A pilot-based equalization method which meets the above requirements was used in a simulation [4] and experiment [5] of a probabilistically shaped QAM signal. Recently, similar method was proposed for multi-carrier 1 Tbps channels [6] and evaluated in optical back-to-back with up to 64QAM. In this paper, the method from [4, 5] is demonstrated and optimized experimentally w.r.t. the achievable information rate (AIR) in a 5x10 Gbaud wavelength division multiplexed (WDM) transmission system operating at 256/1024QAM with probabilistic shaping for up to 1600 km.

2. Pilot based CMA equalization and experimental setup
In order to take advantage of the low-OSNR requirement of CMA equalization, the QAM sequence is interleaved with QPSK pilots, which are known at the receiver. A sketch of the system is given on the bottom of Fig. 1. The QPSK symbols appear one at a time with a certain period, $P - 1$ (every $P$-th symbol is pilot), resulting in a pilot overhead (PO) of $1/(P - 1) \cdot 100\%$. Furthermore, a short Zaddof-chu sequence with frequency- and phase-offset independent high correlation properties is used as a frame alignment sequence (FAS). At the receiver side, after alignment the pilot positions are identified. The equalization filter taps $H_{init}$ are first estimated from a training sequence of QAM symbols, which is available at the receiver. At the first pilot position, $P$, the taps $H_{init}$ are updated according to the CMA rule by estimating the error at that time and updating with a proper step $\mu$, which takes into account the distance $P$. The rest of the pilots are equalized in a similar manner. The process is repeated (in our case 20 times) until convergence. Following is linear interpolation between the taps at the pilot positions to estimate the taps $H_{P-1}^{1}, H_{P+1}^{2P-1}, \ldots, H_{kP+1}^{(k+1)P}$. 
where \((k+1)P\) is the length of the block (in our case, we fix the QAM sequence length to \(k \cdot (P-1) = 60000\)). In this work, the equalizer filter length is 101 symbols at 2 samples per symbol.

The experimental setup is shown in Fig. 1. At the transmitter, the pulse-shaped (raised cosine, roll-off 0.5) sequence (QAM + pilots) is sent to a 64 GSa/s arbitrary waveform generator (AWG), which is used to modulate five channels on a 25 GHz grid at 10 Gbaud with two IQ modulators (for channel under test (CUT) and interfering channels).

The CUT (in this work that is the central channel) uses a sub-kHz linewidth fiber laser (Koheras BasiK C-15) while the four co-propagating channels use standard external cavity lasers (ECL, 100 kHz linewidth). These four channels are decorrelated by more than 40 symbols using a wavelength selective switch (WSS) and combined with the CUT. The signal is detected by an 80 GSa/s coherent receiver followed by offline processing, consisting of (in order) low-pass filtering, down sampling, chromatic dispersion (CD) compensation, frame alignment, frequency offset estimation, time-domain equalization and carrier phase recovery with the algorithm from [7].

### 3. Results

We study the performance of 256/1024QAM for up to 1600 km transmission, where PMD is accumulated (< 1 ps/√km), which strengthens the adaptation speed requirement of the equalizer. The received signal-to-noise ratio (SNR) and the achievable information rate are reported. The SNR is defined as $\text{SNR} = \frac{E_k |x_k|^2}{E_k (|y_k - x_k|^2)}$, where $y_k$ are the received samples after carrier phase recovery and $x_k$ are the transmitted QAM symbols at time $k$. The AIR is the mutual information (MI) $\mathcal{I}(X;Y)$ between $x$ and $y$ assuming circular symmetric Gaussian statistics of the noise. While it is clear that higher PO improves the receiver SNR, the net data rate is reduced, which is indicated in the expression for MI: $\mathcal{I}(X;Y) = (1-1/P) \mathcal{H}(X) - \mathcal{H}(X|Y)$, where $\mathcal{H}$ is the entropy function. Higher PO improves the quality of the signal and reduces the uncertainty around the input given the output ($\mathcal{H}(X|Y)$), but at the same time reduces the entropy of the input $\mathcal{H}(X)$, resulting in a non-trivial trade-off.

The results are given in Figs. 2(a), 2(b), 2(c) and 2(d) for uniform 256QAM, probabilistically shaped 256QAM, uniform 1024QAM and probabilistically shaped 1024QAM. The probabilistic shaping is performed as in [5], and further details are omitted here. We compare the received SNR to the upper bound, achieved by a genie-aided MMA, in which the true transmitted symbols are used for equalization, i.e. all decisions are correct.

For all modulation formats, around 10% pilots are needed to converge to the upper bound (all modulation formats achieve virtually equivalent SNR at each pilot rate). However, the AIR is significantly reduced by such high PO. The optimal pilot rate is found to be between 2% and 5% for all modulation formats, resulting in modulation format-independent performance. The effective SNR at the receiver does not allow for standard RDE MMA equalization due to the high symbol error rate, whereas the studied method is SNR-independent. We note that the received SNR is relatively low for the large modulation formats considered here. Such operating points are of interest since higher FEC overheads can be used and thus a better spectral efficiency can be achieved, as explained in the introduction.

**Discussion.** The complexity of the algorithm is small due to the simplicity of CMA and the fact that the taps...
References

The narrow linewidth fiber lasers. This work was supported by the DNRF Research Centre of Excellence, SPOC, ref. DNRF123. NKT Photonics A/S is acknowledged for providing

SNR relative to the modulation format size and with higher FEC overhead, thus with a better spectral efficiency at a

optimized pilot insertion rate of between 2% and 5%. The equalization scheme allows for operation at low received

ing. Modulation format-independent performance was reported over metro-range distances (800-1600 km) with an

Pilot-based equalization was experimentally studied for WDM systems with high-order QAM and probabilistic shap-

4. Conclusion

Fig. 2: Performance of the pilot-based equalization in a WDM system with 256/1024QAM with uniform and probabilistic shaping as in [5].

are only updated every \( P \) symbols. Thus, \( P \) times less complexity is achieved w.r.t. standard CMA (neglecting the

complexity of the linear interpolation), and even more so w.r.t. RDE MMA. The algorithm also provides a flexible

complexity/performance trade-off by tuning the PO. Since the equalization is only performed on the amplitude of the

pilots, data can be transmitted on those positions using QPSK constellation with 2 bits/symbol efficiency, leading to a

hybrid modulation format with extreme benefits (the equalizer comes for free). An alternative is to use the pilots
during carrier phase recovery, including frequency offset and laser phase noise (as in [4–6]), in which case the pilots

should not carry data. Blind carrier phase recovery can also take advantage of pilots for cycle-slip detection. Finally,

we note that PO of 1% is used in e.g. [6], which is sufficient for back-to-back equalization of 64QAM. As we see in

Fig. 2, fiber impairments (e.g. PMD) result in a fast-varying channel, and thus introduce the need for higher PO.

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References

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