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Improved reconstruction for IDEAL spiral CSI

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Synopsis

In this study we demonstrate how reconstruction for IDEAL spiral CSI (spectroscopic imaging scheme developed for hyperpolarized dynamic metabolic MR imaging) can be improved by using regularization with a sparsity constraint. By exploiting sparsity of the spectral domain, IDEAL spiral CSI can achieve chemical shift encoding by acquisition of only few time-shifted echoes. The minimum number of echoes required to avoid noise amplification can be decreased by means of regularization enforcing spectral sparsity, hereby reducing scan time. Improvements achieved by using regularized reconstruction are demonstrated for in vivo data from a hyperpolarized cardiac study of a pig.

Introduction

IDEAL spiral CSI\textsuperscript{1} is a spectroscopic imaging scheme developed for hyperpolarized dynamic metabolic MR imaging. The spectral-spatial encoding is based on a single-shot spiral, whereas the chemical shift encoding is based on echo-time shifting between excitations. Hereby, the sparsity of the spectral domain is exploited for faster imaging. To avoid noise amplification in the reconstruction, a certain number of echoes is required. Here we propose, however, that noise amplification from acquiring less echoes can be decreased by using regularization with a sparsity constraint instead of using matrix inversion in the reconstruction. By acquiring less echoes, the individual image scan time is decreased, which can be utilized for better dynamic resolution or more slices in hyperpolarization studies.

Methods

Figure 1 shows the spectral encoding scheme of IDEAL spiral CSI. The chemical shift encoding for the IDEAL scheme is:

\[ y_{m,n} = \sum_{q} E_{m,q} e^{i\omega_q T} \xi_q(k_n) \]

with \( E_{m,q} = e^{i\omega_q T} \), where \( y_{m,n} \) is the measured data for the \( m \)th echo and the \( n \)th k-space sample and \( \xi_q(k_n) \) is the \( q \)th metabolite distribution in k-space. If \( E \) is well-conditioned, \( \xi_q(k_n) \) can be reconstructed by matrix inversion:

\[ \hat{\xi}_q(k_n) = e^{-i\omega_q T} (E^\dagger y_n)_q \]

\( \dagger \) denotes the Moore-Penrose pseudo-inverse. Saving scan time by acquiring less echoes, increases the condition number of \( E \), which leads to noise amplification when it is inverted. To limit this, the reconstruction can be regularized by enforcing a sparsity constraint using the L1-norm and by solving the minimization problem given by the following objective function:

\[ \min \|E \hat{x}_n - y_n\|_2^2 + \lambda \|x_n\|_1 \]

where \( x_n = \xi_q(k_n) e^{i\omega_q T} \), and \( \lambda \) is a regularization parameter weighting the constraint enforced by the L1-norm. This reconstruction approach was implemented in the pre-existing IDEAL spiral CSI reconstruction pipeline iteratively for each k-space sample using \texttt{fminsearch} in Matlab. The regularization parameter was empirically selected to \( \lambda = 100.000 \).

The method was demonstrated using in vivo data from a hyperpolarized [1-\textsuperscript{13}C]pyruvate cardiac study of a healthy female Danish domestic pig weighing 30 kg. For the hyperpolarization experiment, the pig was first sedated with an intramuscular injection of Stressnil (2.0 mg/kg bodyweight) and Midazolam (0.1 mg/kg) and subsequently anaesthetized via continuous intravenous infusion of both Propofol (12 mg initial bolus dose, 0.4 mg/kg/h thereafter for maintenance) and Fentanyl for analgesia (8 µg/kg/h). The pig was intubated and mechanically ventilated (60 % O\textsubscript{2}-air mix) using a respirator system (GE Healthcare, Broendby, Denmark). A whole-body clinical 3T GE HDx MR scanner (GE Healthcare, Milwaukee, WI, USA) was used for imaging together with a bore-insertable \textsuperscript{13}C volume resonator (clamp shell design) integrated into the patient table for excitation (GE Healthcare, Milwaukee, WI, USA). Two arrays with 8 receive channels each were placed to cover the heart (rapid Biomedical, Rimpar, Germany). The IDEAL spiral CSI was cardiac triggered with 4 excitations per trigger, 11 echoes, echo-time shifting of 0.9 ms, 12 excitations per image, and 8 image repetitions [TE/TR 1.1/100 ms, flip angle 15°, matrix 60x60, FOV 240x240 mm\textsuperscript{2}, in-plane nominal resolution 4 mm, slice thickness 50 mm]. Data were averaged over the 8 repetitions before reconstruction.

Results

Figure 2 shows the reconstruction results from using all 11 echoes, using only 7 echoes with matrix inversion reconstruction, and from using 7 echoes with regularized reconstruction. The condition number of \( E \) was equal to 1.4 with 11 echoes and 2.8 with 7 echoes. The higher condition number is evident from the greater noise level in some of the metabolite images in Figure 2(b), especially for alanine and lactate. The relative error for using 7 echoes compared to 11 for matrix inversion reconstruction was 24 %. Figure 2(c) shows how the reconstruction using regularization is qualitatively improved in terms of less noise. This is supported quantitatively by means of a relative error of 19 %.

Discussion

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\( E \): efficient excitation matrix.

\( \xi_q(k_n) \): \( q \)th metabolite distribution at k-space sample \( k_n \).

\( y_{m,n} \): measured data for the \( m \)th echo and \( n \)th k-space sample.

\( T \): echo time.

\( \omega_q \): frequency of the \( q \)th metabolite.

\( E \): well-conditioned.

\( \hat{x}_n \): reconstructed metabolite distribution.

\( \lambda \): regularization parameter.

\( \|x_n\|_1 \): L1-norm.

\( \|E \hat{x}_n - y_n\|_2^2 \): objective function.
Using regularization in the IDEAL spiral CSI reconstruction can reduce noise amplification as demonstrated in the lactate images of Figure 2. Signal distribution in the pyruvate-hydrate images in Figure 2(a) was, however, not retrievable using regularization. In this study the regularization parameter $\lambda$ was empirically selected, but a more thorough investigation of parameter choice could potentially improve the reconstruction. Compared to matrix inversion in IDEAL spiral CSI a longer reconstruction time is expected.

**Conclusion**

Regularization of the IDEAL spiral CSI reconstruction can improve results, by reducing noise amplification from matrix inversion. This was demonstrated in vivo through qualitatively and quantitatively overall improved metabolite images. Shorter scan times can hereby be pursued with low penalty.

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**References**


**Figures**

Figure 1: Acquisition scheme for IDEAL spiral CSI from$^1$.

Figure 2: Reconstruction results for IDEAL spiral CSI of the short-axis of the heart for the five metabolites (from top down): lactate, pyruvate-hydrate, alanine, pyruvate, and bicarbonate. (a) Matrix inversion reconstruction using 11 echoes, (b) matrix inversion reconstruction using 7 echoes, and (c) regularized reconstruction using 7 echoes.