Interaction of Droop Control Structures and its Inherent Effect on the Power Transfer Limits in Multi-terminal VSC-HVDC

Thams, Florian; Eriksson, Robert; Molinas, M.

Published in: IEEE Transactions on Power Delivery

Link to article, DOI: 10.1109/TPWRD.2016.2600028

Publication date: 2016

Document Version Peer reviewed version

Interaction of Droop Control Structures and its Inherent Effect on the Power Transfer Limits in Multi-terminal VSC-HVDC

F. Thams, Graduate Student Member, IEEE, R. Eriksson, Senior Member, IEEE, M. Molinas, Member, IEEE

Abstract—Future multi-terminal HVDC systems are expected to utilize dc voltage droop controllers and several control structures have been proposed in literature. This paper proposes a methodology to analyse the impact of various types of droop control structures using small-signal stability analysis considering all possible combinations of droop gains. The different control structures are evaluated by the active power transfer capability as a function of the droop gains, considering various possible stability margins. This reveals the flexibility and robustness against active power flow variations, due to disturbances for all the implementations. A case study analyzing a three terminal HVDC VSC-based grid with eight different kinds of droop control schemes points out that three control structures outperform the remaining ones. Additionally, a multi-vendor case is considered where the most beneficial combinations of control structures has been combined in order to find the best performing combination.

Index Terms—Power system stability, Power transmission, stability, HVDC transmission, AC-DC power converters, Stability analysis, Control system analysis, State-space methods

I. INTRODUCTION

The rising number of offshore wind farm projects far away from the coast, as well as the need to connect those often remote RES to the major load centers, led to an increase of interest in HVDC technology in the last decade. The first commercial application of HVDC transmission was built in 1954 between Gotland and the Swedish mainland based on mercury valves [1]. Since then, most HVDC links based on line commutated converters (LCC) were built in point-to-point connections besides few exceptions (e.g. in Sardinia-Corsica-Italy and Quebec New England [2]).

The appearance and development of HVDC transmission based on voltage source converter (VSC) and its advantages compared to HVDC based on LCC raised the interest against active power flow independently, the capability to supply weak grids and especially the ease of achieving power flow reversal.

In Europe, ten countries of the North sea region formed the North Seas Countries Offshore Grid Initiative (NSCOGI) in order to explore the best way to establish an offshore HVDC grid [3]. In China, however, two multi-terminal HVDC (MT-HVDC) grids have already been built [4], [5].

Due to the little experience with multi-terminal grids, the control of such a HVDC grid is an emerging research topic. The operational reliability is a crucial aspect due to the significant economic impact of any malfunction. In case of a MT-HVDC system it is preferable to have a distributed control architecture, where multiple units are actively participating in the control of the grid based on local measurements. This leads to an inherently higher robustness against outages. Further, a distributed control architecture is more effective in case of power fluctuations that exceed the available control range of a single terminal [6], [7]. This is reflected by the fact that the vendors participating in the European HVDC Study Group prefer droop control or droop control together with deadband as control structure for distributed voltage control [8]. Additionally, the applicability of droop control is proven by its use in the Nanao MT-HVDC grid [4].

In technical literature several alternative droop control schemes have been proposed [6], [9]–[18], which have been categorized in a simple framework in [19].

The general operation principle for all the dc voltage droop implementations is identical, i.e. each implementation contains two control loops, in order to assume a linear relationship between current respectively active power and dc voltage. However, it was shown that the choice of control objective for the first respectively the second loop, as well as the tuning, has a significant impact on the dynamic performances and the stability properties. This is especially important to consider in case of a MT-HVDC grid built by different vendors.

Although small-signal stability analysis has been carried out in MT-HVDC grids, a comparison of different dc voltage droop control structures is still missing. To the best knowledge of the authors, there does not exist any analysis to determine the most beneficial and flexible control structure in the context of a MT-HVDC grid yet. Further, there do not exist any studies on using different kinds of droop control structures within one grid and their impact on each other.

The contribution of this work encloses a methodology for a stability analysis of different droop control implementations, regarding the active power transfer capability as a function

This project is co-funded by the European Unions Seventh Framework Programme for Research, Technological Development and Demonstration under the grant agreement no. 612748.

F. Thams is with the Center of Electric Power and Energy (CEE), Technical University of Denmark (DTU), DK-2800 Kgs. Lyngby, Denmark (e-mail: fth@elektro.dtu.dk).

Robert Eriksson was with the Center for Electric Power and Energy (CEE), Technical University of Denmark (DTU), DK-2800 Kgs. Lyngby, Denmark. He is now with the Swedish National Grid (e-mail: errobban@gmail.com).

M. Molinas is with the Department of Engineering Cybernetics, Norwegian University of Science and Technology (NTNU), 7491 Trondheim, Norway (e-mail: marta.molinas@ntnu.no).
of the droop gains. This methodology is applied to analyse a MT-HVDC grid, which extends the work in [19], to emphasize the impact of different control structures. In the study case the flexibility against active power flow variations and robustness against disturbances will be compared and analyzed for all the various implementations.

Additionally, the stability limits of the most promising configurations will be analyzed and the limitations discussed in more detail. This will also provide further insight on how different droop controlled converters influence each other. Moreover, in contrast to previous publications, this work will investigate the consequences resulting from using different implementations simultaneously at different converter stations.

This paper is structured in four main parts. After the introduction a general model will be introduced and then the used methodology for analyzing the power transfer capability will be explained. Finally, a case study of a three terminal grid will be introduced and the findings will be discussed.

II. MATHEMATICAL MODEL

A general mathematical model of a VSC-HVDC terminal with simplified ac grid will be presented in the following sections. This model is based on the single VSC configuration introduced in [20]. In order to develop a multi-terminal grid, an arbitrary number of those terminals and lines can be connected.

A. Model Conventions

Upper case letters represent physical values of the electrical circuit, whereas lower case letters define per unit quantities. The apparent power rating of the converter and the peak value of the rated phase voltage serve as base values for the used per unit system. The modelling of the electrical system and the control of the ac-side will be presented in a synchronous reference frame (SRF), using the amplitude-invariant Park Transformation. The d-axis voltage vector is aligned with the voltage vector, \(v_o\), at the corresponding filter capacitor, \(c_f\), and the q-axis is leading the d-axis by 90° [1]. SRF equations will be noted in complex space vector notation according to

\[
x = x_d + j \cdot x_q.
\]

B. Electrical System

As shown in Fig. 1, a simplified but appropriate model for this analysis is used. The focus on the outer control loop, as well as the emphasis on small signal analysis, justifies this simplification for a multi-terminal grid in order to minimize the large computational burden.

1) Electrical System on the AC Side: As shown in Fig. 1, a simplified model of the ac grid is assumed, using an LC filter as the grid interface of the VSC and a Thévenin equivalent representation of the grid. The state-space equations can be obtained as given below, where the per unit grid frequency is denoted as \(\omega_g\) and the base angular frequency as \(\omega_b\) [21], [22].

\[
di_l = \frac{\omega_b}{l_f} v_{cv} - \frac{\omega_b}{l_f} v_o - \left(\frac{r_f \omega_b}{l_f} + j \cdot \omega_g \omega_b\right) i_l
\]

\[
dv_o = \frac{\omega_b}{c_f} i_l - \frac{\omega_b}{c_f} i_g - j \cdot \omega_g \omega_b v_o
\]

\[
di_g = \frac{\omega_b}{l_g} v_o - \frac{\omega_b}{l_g} v_q - \left(\frac{r_g \omega_b}{l_g} + j \cdot \omega_g \omega_b\right) i_g
\]

The power balance between ac and dc side is given below. It is based on the assumption of an ideal lossless average model for the converter.

\[
v_{cv,d} \cdot i_{l,d} + v_{cv,q} \cdot i_{l,q} = v_{dc} \cdot i_{dc,cv}
\]

2) Electrical System on the DC Side: On the dc side, the lines are represented as single pi-equivalents, where the capacitances are incorporated in the dc capacitance of the corresponding converter, as given in (6).

\[
c_{dc} = c_{dc,line} + c_{dc,vsc}
\]

It is worth to note that this is a simplified model, which can approximate only the lowest frequency resonant peak of the cable [12]. But, on the other hand, D’Arco argues in [20], this approach also resembles the worst case scenario with respect to LC oscillations. This is due to the fact that the oscillatory effects are condensed in a single frequency, instead of being spread on several frequencies as in a real cable. This modeling approach can also be justified by the results of [23], indicating that for an appropriate sizing of the capacitor the impedance
seen by the VSC is almost identical. The equations for the dynamics at the dc capacitors are given by:

$$\frac{dv_{dc}}{dt} = \frac{\omega_b}{c_{dc}} i_{dc,cv} - \frac{\omega_b}{c_{dc}} i_{dc, line}$$

(7)

Whereas the dc line dynamics according to the defined current flow are given by:

$$\frac{di_{dc, line}}{dt} = \frac{\omega_b}{i_{dc,b}} v_{dc,b} - \frac{\omega_b}{i_{dc}} v_{dc} - \frac{\omega_b}{i_{dc}} i_{dc, line}$$

(8)

C. Control System

The control system consists of an active damping of LC filter oscillations for the ac side, a current controller, a PLL and an outer controller. The outer control depends on the connected ac grid, which is explained in more detail in the outer loop controller subsection. An overview of the control system is given in Fig. 2. The corresponding equations are given in the following subsections.

1) PLL: The VSC is assumed to be synchronized with the corresponding ac grid through a PLL, modelled as shown in Fig. 3 [22], [24]. An inverse tangent function is used on the low-pass filtered estimated phase voltages $v_{PLL}$ to approximate the actual phase angle error $\Delta \Theta_{v, PLL}$. Followed by a PI controller in order to derive the frequency of the tracked voltages. The corresponding equations are given as:

$$\frac{dv_{PLL}}{dt} = -\omega_{LP, PLL} v_{PLL} + \omega_{LP, PLL} v_o$$

(9)

$$\frac{de_{PLL}}{dt} = \tan^{-1} \left( \frac{v_{PLL,q}}{v_{PLL,d}} \right)$$

(10)

$$\frac{d\Delta \Theta_{v, PLL}}{dt} = \omega_b \Delta \omega_{PLL}$$

(11)

with $\epsilon_{PLL}$ representing the integrator state of the PI controller and $\Delta \Theta_{PLL}$ the phase angle deviation between the grid voltage, $v_o$, and the orientation of the PLL. $\Delta \omega_{PLL}$ describes the grid frequency deviation. The deviation variables are necessary for the modeling of the PLL in the SRF. While the actual voltage vector phase angle, $\Theta_{PLL}$, obtained, as shown in Fig. 3, is needed for the transformation between stationary and rotating reference frame.

![Fig. 3. Phase Locked Loop](image)

2) Active Damping of LC Filter Oscillations: An active damping of LC filter oscillations is implemented, based on injecting a component, $v_{AD}^*$, to the converter output voltage, which is in counter-phase with the detected oscillations [25], [26].

$$v_{AD}^* = k_{AD} (v_o - \phi)$$

(12)

$$\frac{d\phi}{dt} = \omega_{PLL} v_o - \omega_{AD} \phi$$

(13)

While $\omega_{AD}$ represents the cut-off frequency and $\phi$ the integrator states of the low-pass filter, $k_{AD}$ is used as tuning parameter depending on the dynamic response of the system.

3) Inner Current Control Loop: The inner current control is based on vector control in the synchronous reference frame, tuned by modulus optimum criterion [27]. Considering two conventional PI controllers with decoupling terms and voltage feed-forward, the converter output voltage reference, $v_{cv}$, can be defined as:

$$v_{cv}^* = k_{pc} (i^*_l - i_l) + k_{ic} \gamma + j l f \omega_{PLL} i_l + v_o - v_{AD}$$

(14)

with $\gamma$, $k_{pc}$ and $k_{ic}$ representing the integrator state, the proportional and integral gain of the PI controller.

4) Outer Loop Controller: The outer loop control structure is the main difference between the terminals. Here, a distinction is made between VSC terminals, which are supposed to take part in the dc voltage control, and those which are not. The former are most likely connected to rather strong grids, hence those terminals are called grid side VSC (GSVSC) in the following. The latter is most likely connected to rather weak grids, where the focus lies on maximizing the power output as it is for wind farms, hence those are called wind farm VSC (WFVSC) in the following. This paper focuses on the outer loop control structure of the GSVSCs, in particular how different droop control structures influence the power transfer limits of the whole system.

a) Wind Farm Converter (WFVSC): For a VSC terminal representing a wind farm, a conventional active power controller is providing the d-axis current reference. The q-axis reference is provided by an ac voltage controller. The equations are given as:

$$i^*_{l,d,wf} = k_{pcd,wf} (p^*_{wf} - p_{wf,ac}) + k_{icd,wf} \chi_{d,wf}$$

(15)

$$i^*_{l,q,wf} = k_{pcq,wf} (v^*_{a,wf} - v_{a,d,wf}) + k_{icq,wf} \chi_{q,wf}$$

(16)

with $\chi_{d/wf}$ representing the integrator state, the proportional and integral gain of the PI controller.

b) Grid Side Converter (GSVSC): The q-axis current reference for a VSC terminal connected to a strong grid is provided by a reactive power controller.

$$i^*_{l,q,g} = k_{pcq,g} (q^*_g - q_g) + k_{icq,g} \chi_{q,g}$$

(17)

The d-axis current reference is provided by one of the various dc voltage droop controllers, identified and categorized in [19] and shown in Fig. 4. The block diagrams of the corresponding droop controller indicate that these droop controllers differ regarding:

- power or current based droop implementations
- the choice of the second variable (besides dc voltage): current / power measured on ac or dc side
- the choice on which variable the droop gain $k_{droop}$ is applied, i.e. which variable is controlled in the first and which in the second loop

Copyright (c) 2016 IEEE. Personal use is permitted. For any other purposes, permission must be obtained from the IEEE by emailing pubs-permissions@ieee.org.
shown in Fig. 5. For each combination of these parameters, the movement of certain eigenvalues for a variation of these parameters is analyzed in terms of active power transfer (APTC) in the order of control structure (CS) 1 to 8.

The differences between the various dc voltage droop controllers are analyzed in terms of active power transfer capability as a function of the droop gains of the connected GSVSCs using droop control. That means by using eigenvalue analysis, the eigenvalue movement is analyzed for a variation of the disturbances (= power injection at uncontrolled dc nodes / WFVSCs) and a variation of the droop gains. The sensitivity of certain eigenvalues for a variation of these parameters is shown in Fig. 5. For each combination of these parameters, the nonlinear system is linearized and the steady state is evaluated with respect to the chosen requirements for an acceptable operation point. These requirements can be chosen by the user applying the method and could include e.g. specific stability margins and / or current / voltage limitations. This analysis will basically result in a set of acceptable operation points, which are plotted with respect to the power transferred at a specific terminal. The surfaces of this area of acceptable operation points in this plot illustrate the upper and lower boundary (both directions of power flow) of acceptable operation for a specific combination of droop gains at each terminal. This set of acceptable operation points varies with respect to the chosen requirements. In contrast to other publications using small signal analysis, this methodology helps to determine the range of acceptable operation for a specific terminal within a multi-terminal grid for various control structures with all possible droop gain combinations and any arbitrary requirement. This operating range is expressed as a range of possible power flows at that terminal for a specific droop gain combination. Therefore, it is referred to as active power transfer capability (APTC) in the following.

Finally, the steady states at the boundary of the APTC are analyzed by a participation factor analysis, in order to identify the states associated with the modes causing the violation of a specific stability margin. This provides insight in determining the origin of the boundary and identifies which part of the system is provoking the limit.

Here, this analysis is used to illustrate the focus of this paper: revealing the impact of the choice of the droop control structure on the APTC for different exemplary requirements for an acceptable operation point. Since the models differ only in terms of the droop control structures, this analysis allows to determine which effect each control structure has on the APTC of each terminal and the whole system. Further, it reveals which control structures are more beneficial than others in terms of the APTC. Additionally, in the planning phase of a multi-vendor multi-terminal HVDC grid, probably

III. METHODOLOGY

The corresponding equations of those controllers are given in (18)-(25) in the order of control structure (CS) 1 to 8.

CS1: \[ i_{i,d,g}^* = \left( \frac{v_{dc} - v_{dc}^*}{k_{dgroup}} + i_{dc}^* \right) \cdot v_{dc} \] (18)

CS2: \[ i_{i,d,g}^* =\frac{v_{dc} - v_{dc}^*}{k_{dgroup}} + i_{ac}^* \] (19)

CS3: \[ i_{i,d,g}^* = k_{ped,g} \left( (i_{dc}^* - i_{dc}) \cdot k_{dgroup} + v_{dc} - v_{dc}^* \right) \] (20)

CS4: \[ i_{i,d,g}^* = k_{ped,g} \left( (i_{ac}^* - i_{ac}) \cdot k_{dgroup} + v_{dc} - v_{dc}^* \right) + k_{icd,g} \cdot \chi_{d,g} \] (21)

CS5: \[ i_{i,d,g}^* = k_{ped,g} \left( \frac{v_{dc} - v_{dc}^*}{k_{dgroup}} + p_{dc}^* - p_{dc} \right) \] (22)

CS6: \[ i_{i,d,g}^* = k_{ped,g} \left( \frac{v_{dc} - v_{dc}^*}{k_{dgroup}} + p_{ac}^* - p_{ac} \right) \] (23)

CS7: \[ i_{i,d,g}^* = k_{ped,g} \left( (p_{dc}^* - p_{dc}) \cdot k_{dgroup} + v_{dc} - v_{dc}^* \right) \] (24)

CS8: \[ i_{i,d,g}^* = k_{ped,g} \left( (p_{ac}^* - p_{ac}) \cdot k_{dgroup} + v_{dc} - v_{dc}^* \right) \] (25)
Disturbances will define the power flow, while the droop gains controlled dc node, need to be defined. Here, the values of the disturbance resembled by the power injection of the unconstrained terminal. First, a range of values for the droop gains, as well for the output. The analyzed inputs and outputs are the disturbance of the corresponding inputs by the system seen from a specific singular value, where the singular value representation can be obtained as:

\[ \sigma_i(E(w(j\omega))) = \sqrt{\lambda_i(E^*(w(j\omega))E(w(j\omega)))} \]  \hspace{1cm} (26)

The final version of record is available at [http://dx.doi.org/10.1109/TPWRD.2016.2500028](http://dx.doi.org/10.1109/TPWRD.2016.2500028)

**Fig. 5. Visualization of the sensitivity of certain eigenvalues and the stability margin of a minimum damping ratio of 3%.** The pole movement is shown for a variation from 0 p.u. (blue) to 1 p.u. (red), a) \( p_{w,f} \), b) \( k_{droop} \) from 0 (blue) to 0.1 (red) and c) \( k_{droop}\gamma_2 \) from 0 p.u. (blue) to 0.1 p.u. (red) for otherwise fixed values of \( p_{w,f} = 0 \) p.u., \( k_{droop} = 0.1 \) p.u. and \( k_{droop}\gamma_2 = 0.1 \) p.u.

using different kind of droop control structures, the analysis facilitates to determine more or less beneficial combinations of control structures. Moreover, by analyzing these boundaries along the variation of the droop gains, it provides insight on how the choice of the droop gain values affects the APTC during operation. Additionally, it indicates whether a certain ratio of the droop gain values may be beneficial for maximizing the APTC.

**A. Flowchart of the Methodology**

The methodology is shown in detail in Fig. 6, as an example for a three terminal model, as it is used in the case study. The methodology can, however, also be applied to other topologies, the visualization of the APTC just becomes more challenging in case of a higher number of terminals.

First, a range of values for the droop gains, as well for the disturbance resembled by the power injection of the uncontrolled dc node, needs to be defined. Here, the values of the disturbances will define the power flow, while the droop gains will define the power sharing between the terminals. In the case study, a value range of 0.0001 p.u. \( \leq k_{droop} \leq 0.1 \) p.u. and \(-2\) p.u. \( \leq p_{w,f} \leq 2\) p.u. was chosen, however, the ranges can be chosen by the user applying the method according to the analyzed system. Additionally, any arbitrary requirement for an acceptable operation point can be chosen, which can include (several) stability margins and/or current/voltage requirements. Then, the first combination of values is chosen and the nonlinear system obtained from the aforementioned equations is linearized for the given inputs. It is analyzed whether the steady state meets current and voltage limits and whether the eigenvalues satisfy the requirements of various possible stability margins. Depending on the results, the operation points are saved correspondingly and the next combination of values is analyzed.

**B. Requirements for an acceptable Operation Point**

As aforementioned any arbitrary requirement for an acceptable operation point can be chosen by the user applying the method. Since there are no grid codes or standardized requirements for acceptable operation points in MT-HVDC grids defined yet, in the case study the APTC is analyzed for three possible requirements in order to investigate whether a certain requirement (current/voltage limit or stability margin) limits specific control structures more than others.

1) **Voltage and Current Limits:** First, the APTC are analyzed only with respect to fulfill the current and voltage limits. Here, these limits are chosen according to the Cigré B4 DC Grid test system, i.e. the dc voltage operational frame is assumed to be between 0.95 p.u. and 1.05 p.u., while the maximum current in the dc cable is set to 2265 A [38].

2) **Damping Ratio \( \geq 3\%\):** A minimum damping ratio of 3% is demanded for all eigenvalues [39].

3) **Maximum DC Voltage deviation of 5%:** The performance of the control structures can be analysed by means of the singular value representation of the system transfer function matrices, \( E_w(j\omega) \), according to [40]. The singular value representation can be obtained as:

\[ \sigma_i(E_w(j\omega)) = \sqrt{\lambda_i(E^*_w(j\omega)E_w(j\omega))} \]  \hspace{1cm} (26)

where \( \lambda_i \) is the \( i \)-eigenvalue of the matrix. The maximum singular value, \( \sigma(G(j\omega)) \), indicates the maximum amplification of the corresponding inputs by the system seen from a specific output. The analysed inputs and outputs are the disturbance

**Copyright (c) 2016 IEEE. Personal use is permitted. For any other purposes, permission must be obtained from the IEEE by emailing pubs-permissions@ieee.org.**
(wind power input) and the dc voltage errors at the GSVSCs. In [40] the authors derive the maximum gain the singular value representation should not exceed, in case a maximum voltage error of 10% of the nominal value at each terminal is assumed. Here, it is adapted to the per unit system and a maximum deviation of 5% is chosen as stability margin:

\[
\sigma(E_w(0)) \leq \frac{\|e(0)\|_2}{\|w(0)\|_2} = 20 \log_{10} \left( \frac{\sqrt{e_{gsvsc1} + e_{gsvsc2}}}{p_{wf,vsc}} \right) = 20 \log_{10} \left( \sqrt{1 \cdot (0.05)^2} \cdot \frac{2}{1} \right) = -23.01 \text{ dB}
\]

(27)

IV. CASE STUDY

A symmetric three terminal grid is derived from the aforementioned model, as shown in Fig. 8 (the ac sides are equal for all terminals as indicated by the ac system equivalent of the general model).

The GSVSCs use each one of the eight different droop control structures. First, both GSVSCs use the same CSs in order to detect the ones with highest APTC and highest damping ratios. Then, the most promising ones are combined with each other in order to determine the most beneficial combination of droop control structures. Each of these models consists of 52-54 states depending on the dc voltage droop implementations used. All models have been derived using Maxima [41].

The analysis depends obviously on the given parameters and should therefore be selected as they appear in the system. In this case study, the dc voltage reference values for both GSVSCs are set to 1 p.u., while the current and active power reference values of the GSVSCs are set to 0.1 p.u.. The numerical values for the gains of the droop controller have been selected with respect to the aforementioned reference values to ensure comparable performances. In particular, if a PI controller is present, its tuning has been set to achieve a 5% overshoot for a 5% step in the dc voltage reference with a fast rise time of approx. 8 ms and a settling time of a few tens of milliseconds. Thus, it is chosen to be very fast compared to suggestions in the literature of up to few 100 ms [8] in order to approach the limits of the VSC. Additionally, a second tuning with a rise time in the range of tens of milliseconds and a settling time of 100 ms is used as reference case.

In order to ensure comparability but also not to be limited by the VSC representing the wind farm, the active damping of both GSVSCs are tuned equally, whereas a higher damping factor is chosen for the WFVSC.

All parameter and base values are given in appendix. The dc parameters are scaled into per unit by using the same base frequency as for the ac side, as shown in appendix. This results in apparently high values for per unit inductance and capacitance, however, these parameters are corresponding to a dc cable of about 67 km [20].

All used models are verified by time domain simulations with equivalent non-linear models built in Matlab SimPowerSystems, two validation plots are shown in Fig. 7.

A. Analysis of the Case where both GSVSCs use the same CS

In this scenario the same control structure is used at GSVSC1 and GSVSC2. This is done in order to determine the operation ranges for each CS for the various requirements. In the following the APTCs are given for the case where the only requirements considered are the system stability $Re\{\lambda\} \leq 0$ and the voltage and current limits given in the respective tables. The APTC of the case in which both GSVSCs use CS 8 is shown in Fig. 9. Fig. 9a shows the maximum power transfer in both directions of one terminal for all combinations of $k_{\text{droop}}$ and $k_{\text{droop,gs}}$. That means with the given current definition shown in Fig. 1, the upper surface resembles the inverter limit of that GSVSC while the lower surface resembles the rectifier limit of that GSVSC. The area between both surfaces is the area of stable and acceptable operation points. Thus, the APTC of a single
terminal indicates for which power flow variations a stable and acceptable operation can be achieved for that terminal for all droop gain value combinations. In the optimal case, each terminal should achieve an APTC ≥ 2 p.u. for a wide range of droop gain combinations in order to be able to withstand disturbances and power flow variations up to its rated power in both power flow directions. The APTC for the sum of both GSVSCs (p_{gridside}), shown in Fig. 9b, indicates how much power can be transferred from the WFVSC to the GSVSCs (upper limit) and how much could be transferred from both GSVSCs to an uncontrolled dc node (lower limit). In this scenario the WFVSC should be imagined not as wind farm, but as a weak grid not participating in the dc voltage control.

When analyzing the APTC of the various CSs, it is of main interest to find the maximum APTC value of a single terminal, i.e. exemplary for CS 8 to determine the droop gain combination where the range between the upper and lower limit is the highest in Fig. 9a. Further, it is of main interest to find the maximum APTC value for the whole p_{gridside} (Tab. I & Tab. III), since in the case of just maximizing the APTC of a single terminal the APTC of the second terminal will be minimized at the same time, as shown in Fig. 9a (maximum at k_{droop} = 0.0001 and k_{droop,g2} = 0.1, but minimum at k_{droop} = 0.1 and k_{droop,g2} = 0.0001). Thus, the maximum APTC for the whole p_{gridside} is resembled by the maximum range between the upper and lower boundary in Fig. 9b. Additionally, the eigenvalues with the lowest damping ratio at both limits have been analyzed in order to determine possible limitations and differences between the CSs (Tab. II, Tab. IV). Both analyses have been carried out once for each investigated tuning in order to be able to point out the consequences of a different tuning.

1) Analysis of the maximum APTC of a single terminal: The results of the analysis of the maximum APTC of a single terminal in the case both terminals use the same CS is given in Tab. I. The participation factor analysis of the lowest damped eigenvalues at both limits is given in Tab. II.

The results indicate that the four CSs, where the dc voltage is controlled in the second loop, outperform the remaining CSs. That means, CS 3, 4, 7 and 8 achieve a significantly larger APTC. Additionally, they achieve significant lower maximum singular values in steady state, \( \sigma(E_w(0)) \). However, all CSs fulfill the requirements of the stability margin minimizing the voltage deviation (\( \sigma(E_w(0)) \geq -23.01 \text{dB} \)). The results indicate further that the results are almost the same for the slow tuning.

For all CSs the APTC of a single terminal is maximized in case the difference of the droop gains is high, which minimizes the APTC of the second terminal at the same time, as shown above.
in Fig. 9a. The reason for this is the current limit of 2265 A (= 0.755 p.u.), which limits the current for each line and therefore makes it necessary to minimize the power transfer of the second terminal, in order to transfer as much power as possible from the WSVSC through all three cables to one specific terminal. This might make the results rather specific for this topology, however, the analysis still points out which CSs are capable of withstanding large droop gain deviations within a MT-HVDC grid without leading to instability (in rectifier mode). This is indicated by the very low damping ratios of the lowest damped eigenvalues at the lower limit for CS 1, 2. 5 and 6, as shown in Tab. II. This means further that the APTC of those CSs decreases further for a stability margin demanding a minimum damping ratio of 3%, which leads to an even bigger deviation between the highest and lowest APTC of the various CSs.

The participation factor analysis in Tab. II shows further, which states have a participation in the modes of those eigenvalues with the lowest damping ratio. In fact, in case of the fast tuning, the eigenvalues corresponding to the very low damping ratios at the lower limit (CS 1, 5&6) are related to the GSVSC1, i.e. the GSVSC transferring as much power as possible from the ac to the dc side. Hence, the instability is caused by the terminal and the connected ac grid.

While in case of the slower tuning, the damping ratios at the lower limit do not differ so much anymore, i.e. the ones of the better performing CSs decrease while the damping ratios of the remaining ones remain low. Only CS 7 still fulfills the stability margin in this case. Further, with the slower tuning, the lower limit is related to oscillation within the dc grid for all CSs, as the participation factor analysis indicates (Tab. II). Thus, a faster tuning leads to better damped dc oscillations.

2) Analysis of the maximum APTC of the sum of both GSVSCs: The results of the maximum APTC of all GSVSCs are given in Tab. III. It is shown that the CSs 3 and 8 still outperform the others in case of the fast tuning. While CS 4 still achieves a comparable APTC, CS 3 and 8 achieve significant lower maximum singular values in steady state, $\sigma(E_w(0))$, i.e. smaller voltage deviation induced by a variation of the active power of the WFVSC. The results indicate further that in order to maximize the APTC of all GSVSCs equal droop gains (or small deviations) are preferable, the only exception here is CS 7.

The analysis additionally shows that with slower tuning the maximum singular values of CS 3, 4, 7 and 8 decrease, while the ones of CS 5 and 6 remain approximately constant. Further, with that tuning, the APTC of the CSs 5, 6 and 7 increase while the ones of 3 and 8 decrease, which brings the APTC of all CSs closer to each other. Hence, the various CSs tend to favor different tunings / the impact of the tuning on the CSs.

TABLE III

<table>
<thead>
<tr>
<th>Control Structure</th>
<th>Max Range $\rho_{gridside}$</th>
<th>Damping Ratio of lowest damped EV $\sigma(E_w(0))$</th>
<th>Max Range $\rho_{gridside}$</th>
<th>Damping Ratio of lowest damped EV $\sigma(E_w(0))$</th>
</tr>
</thead>
<tbody>
<tr>
<td>CS 1</td>
<td>1.97 p.u. 0.23%</td>
<td>13.92% -26 dB -27.3 dB</td>
<td>CS 2</td>
<td>1.95 p.u. 0.16% 0.1%</td>
</tr>
<tr>
<td>CS 3</td>
<td>3.02 p.u. 0.19%</td>
<td>18.32% -24 dB -27.3 dB</td>
<td>CS 4</td>
<td>2.97 p.u. 0.25% 0.19%</td>
</tr>
<tr>
<td>CS 5</td>
<td>2.48 p.u. 0.26%</td>
<td>18.49% -27 dB -27.3 dB</td>
<td>CS 6</td>
<td>2.55 p.u. 0.05%</td>
</tr>
<tr>
<td>CS 7</td>
<td>2.47 p.u. 0.1%</td>
<td>26.89% -33 dB -32.3 dB</td>
<td>CS 8</td>
<td>3.02 p.u. 0.6% 0.3%</td>
</tr>
</tbody>
</table>

TABLE IV

<table>
<thead>
<tr>
<th>Control Structure</th>
<th>Highest participation factors of lowest damped EV</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>lower limit</td>
</tr>
<tr>
<td>CS 1</td>
<td>37% $i_g,d,q$, 30% $v_o,q,d$, 11% $v_o,q,g$</td>
</tr>
<tr>
<td>CS 2</td>
<td>46% $v_o,c$, 24% $v_o,d,q$, 24% $v_o,d,g$</td>
</tr>
<tr>
<td>CS 3</td>
<td>26% $v_o,c$, 15% $X_d,q$, 15% $X_d,g$</td>
</tr>
<tr>
<td>CS 4</td>
<td>19% $v_o,c$, 18% $X_d,q$, 17% $v_o,d,g$</td>
</tr>
<tr>
<td>CS 5</td>
<td>19% $v_o,c$, 19% $i_o,q,d$, 15% $v_o,d,g$</td>
</tr>
<tr>
<td>CS 6</td>
<td>19% $v_o,c$, 19% $i_o,q,d$, 15% $v_o,d,g$</td>
</tr>
<tr>
<td>CS 7</td>
<td>34% $v_o,c$, 31% $v_o,d,g$, 16% $v_o,d,g$</td>
</tr>
<tr>
<td>CS 8</td>
<td>25% $v_o,c$, 15% $X_d,q$, 15% $i_o,q,d$</td>
</tr>
</tbody>
</table>

Slow Response Time

<table>
<thead>
<tr>
<th>Control Structure</th>
<th>Highest participation factors of lowest damped EV</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>lower limit</td>
</tr>
<tr>
<td>CS 3</td>
<td>23% $v_o,c$, 19% $i_o,c,w$, 19% $i_o,d,w$</td>
</tr>
<tr>
<td>CS 4</td>
<td>24% $v_o,c$, 17% $X_d,q$, 20% $v_o,d,g$</td>
</tr>
<tr>
<td>CS 5</td>
<td>38% $v_o,c$, 16% $X_d,q$, 16% $X_d,w$</td>
</tr>
<tr>
<td>CS 6</td>
<td>38% $v_o,c$, 16% $X_d,q$, 16% $X_d,w$</td>
</tr>
<tr>
<td>CS 7</td>
<td>37% $i_o,q,d$, 32% $v_o,d,w$, 12% $i_o,q,d$</td>
</tr>
<tr>
<td>CS 8</td>
<td>21% $v_o,c$, 19% $i_o,c,w$, 19% $i_o,d,w$</td>
</tr>
</tbody>
</table>

Copyright (c) 2016 IEEE. Personal use is permitted. For any other purposes, permission must be obtained from the IEEE by emailing pubs-permissions@ieee.org.
The damping ratios of the lowest damped eigenvalues, given in Tab. IV, indicate significant difference between the CSs. In fact, a stability margin demanding a minimum damping ratio of 3% with a fast tuning will further decrease the APTC of all CSs except 3, 4 and 8. This will lead to even higher APTC deviation between the various CSs. The lowest damped eigenvalues of the lower limit of all these three cases are related to the dc grid and the droop controller. Whereas in all other cases (except CS 2) the lowest damped eigenvalues of the lower limit are related to ac values of either GSVSC1 or GSVSC2. Given the low damping ratios of those eigenvalues, for CSs 1, 5, 6 and 7 the lower limit is caused by the ac side oscillations of one of the GSVSCs. The lowest damped eigenvalues of the upper limit on the other hand have for all CSs a comparable high damping ratio, except for CS 2, where the upper limit is apparently related to oscillations within the ac grid of the WFVSC.

3) Conclusion for both GSVSCs using the same CS: Two important aspects of the APTC have been analyzed, first the maximization of power transfer of a single terminal and then the maximization of APTC of the whole system. The CSs 3, 4 and 8 outperform the remaining CSs in both aspects. In both cases, they obtain wider APTC, higher damping ratios and faster damping leads to better damped dc oscillations. This is indicated by the comparison of the eigenvalue movement for a variation of \( k_{\text{droop}} \) in Fig. 10. It is obvious that both pairs of complex eigenvalues with \( \text{Im}\{\lambda\} \approx \pm 400 \) are moved to regions with higher damping ratio in the left half-plane. A participation factor analysis indicates that these eigenvalues are related to dc states.

Further, it has been shown that all CSs are not limited by a set of maximum singular values. The damping ratio stability margin on the other hand is limiting specific CSs while others are fulfilling this stability margin without further limitation of the APTC. Hence, in case of demanding a minimum damping ratio of 3%, the differences between the APTC of the various CSs will be even more significant.

![Fig. 10. Movement of the EV and the damping ratios for a variation of \( k_{\text{droop}} \) from 0 p.u. (blue) to 0.1 p.u. (red) in case both GSVSCs use CS 3](image)

**TABLE V**

<table>
<thead>
<tr>
<th>Control Structures</th>
<th>Max Range</th>
<th>( \sigma(E_w(0)) )</th>
<th>Low. Damp. Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>4 &amp; 3</td>
<td>3.02 p.u.</td>
<td>-61.33 dB</td>
<td>6.2% 8.2%</td>
</tr>
<tr>
<td>8 &amp; 3</td>
<td>3.02 p.u.</td>
<td>-53.5 dB</td>
<td>6.7% 8.4%</td>
</tr>
<tr>
<td>8 &amp; 4</td>
<td>3.02 p.u.</td>
<td>-61.99 dB</td>
<td>6.2% 8.2%</td>
</tr>
</tbody>
</table>

**B. Analysis of the Case where both GSVSCs use different CSs**

In order to determine the consequences of combining different CSs within one grid and finding the most beneficial combination, the most promising CSs from the previous analysis have been combined. Thus, GSVSC1 and GSVSC2 will use different droop control structures with the fast tuning in the following. In particular, the combinations of CS 3, 4 and 8 have been analyzed in detail, due to the most promising results in the previous section.

The analysis indicates that the results for a maximization of the APTC of the single terminal do not differ from the previous analysis for the specific CSs. Thus, the focus is put on the maximization of the APTC of the whole system, the results are given in Tab. V. All the three combinations fulfill all requirements and achieve the same APTC. However, both combinations including CS 4 achieve lower maximum singular values than the combination of CS 8 & 3, which leads to lower voltage deviation at the GSVSCs induced by a power variation of the WFVSC. The maximum APTC of all these three combinations is limited by the current limit. Thus, with cables enabling a higher current limit the APTC will be further increased. However, this does not imply that for other current limitations different combinations of CSs might be more beneficial, since in the previous analysis it was already shown that these three CSs outperform the remaining once already with this current limit.

**V. Conclusion**

This paper presented a methodology to determine the active power transfer capability of single terminals within a MTDC grid. A case study was used to analyze deviations in the APTC, considering different stability margins due to the use of various dc voltage droop control structures and two different tunings. It was shown that fast tuning leads to better damping of dc oscillations. Further, it was shown that three different CSs outperform the remaining five. These three have been combined with each other in order to determine the most beneficial combination. In fact, a combination of a control structure using the dc voltage and the current (CS 4) and either a control structure using dc voltage and active power measured on the ac side (CS 8) or using dc voltage and current (CS 3) leads to even lower voltage deviation induced by power variations of the wind farm. However, additional studies are needed to verify the results for other topologies.

**REFERENCES**


APPENDIX

TABLE VI
BASE VALUES OF PER UNIT SYSTEM AND PARAMETERS

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated voltage, $V_{S,LL,RMS}$</td>
<td>220 kV</td>
</tr>
<tr>
<td>Rated power, $S_{b,gsvsc}$</td>
<td>1200 MVA</td>
</tr>
<tr>
<td>Rated power, $S_{b,wfvsc}$</td>
<td>2 · 1200 MVA</td>
</tr>
<tr>
<td>Rated dc voltage, $V_{dc}$</td>
<td>400 kV</td>
</tr>
<tr>
<td>Rated angular frequency, $\omega_0$</td>
<td>$2\pi 50 \text{s}^{-1}$</td>
</tr>
<tr>
<td>Base value for voltage defined as peak value of phase voltage, $V_b$</td>
<td>$\sqrt[2]{\frac{V_{S,LL,RMS}}{\sqrt{3}}} S_b$</td>
</tr>
<tr>
<td>Base value for currents defined as peak value or rated RMS, $I_b$</td>
<td>$\frac{V_b}{\sqrt{2}}$ $\frac{V}{\sqrt{2}}$ $\frac{A}{\sqrt{2}}$</td>
</tr>
<tr>
<td>Base value for impedance, $Z_b$</td>
<td>$\frac{V_b}{I_b}$ $\frac{V}{A}$ $\frac{V}{A}$</td>
</tr>
<tr>
<td>Base value for filter inductance, $L_b$</td>
<td>$0.011 \Omega/\text{km}$</td>
</tr>
<tr>
<td>Base value for filter capacitance, $C_b$</td>
<td>$2.615 \text{mH/km}$</td>
</tr>
<tr>
<td>Line resistance, $R$</td>
<td>$0.1908 \mu F/\text{km}$</td>
</tr>
<tr>
<td>Line inductance, $L$</td>
<td>$67 \text{km}$</td>
</tr>
<tr>
<td>Grid capacitance, $C_g$</td>
<td>4.2 p.u.</td>
</tr>
<tr>
<td>Grid resistance, $r_g$</td>
<td>0.08 p.u.</td>
</tr>
<tr>
<td>Filter capacitance, $C_f$</td>
<td>0.074 p.u.</td>
</tr>
<tr>
<td>Filter inductance, $L_f$</td>
<td>0.2 p.u.</td>
</tr>
<tr>
<td>Filter resistance, $r_f$</td>
<td>0.01 p.u.</td>
</tr>
<tr>
<td>Reactive power reference, $q^*$</td>
<td>0 p.u.</td>
</tr>
<tr>
<td>Ac voltage reference, $v_{a,d,wf}$</td>
<td>1 p.u.</td>
</tr>
<tr>
<td>Low-Pass filter frequency, $\omega_{AD}$</td>
<td>20 p.u.</td>
</tr>
<tr>
<td>Active damping parameter (GSSVCs), $k_{ad,gsvsc}$</td>
<td>0.2 p.u.</td>
</tr>
<tr>
<td>Active damping parameter (WFVSC), $k_{ad,wfvsc}$</td>
<td>1 p.u.</td>
</tr>
</tbody>
</table>

Copyright (c) 2016 IEEE. Personal use is permitted. For any other purposes, permission must be obtained from the IEEE by emailing pubs-permissions@ieee.org.