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Mid-infrared supercontinuum generation to 12.5\(\mu\)m in large NA chalcogenide step-index fibres pumped at 4.5\(\mu\)m

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Abstract: We present numerical modeling of mid-infrared (MIR) supercontinuum generation (SCG) in dispersion-optimized chalcogenide (CHALC) step-index fibres (SIFs) with exceptionally high numerical aperture (NA) around one, pumped with mode-locked praseodymium-doped (Pr\(^{3+}\)) chalcogenide fibre lasers. The 4.5\(\mu\)m laser is assumed to have a repetition rate of 4MHz with 50ps long pulses having a peak power of 4.7kW. A thorough fibre design optimisation was conducted using measured material dispersion (As-Se/Ge-As-Se) and measured fibre loss obtained in fabricated fibre of the same materials. The loss was below 2.5dB/m in the 3.3–9.4\(\mu\)m region. Fibres with 8 and 10\(\mu\)m core diameters generated an SC out to 12.5 and 10.7\(\mu\)m in less than 2m of fibre when pumped with 0.75 and 1kW, respectively. Larger core fibres with 20\(\mu\)m core diameters for potential higher power handling generated an SC out to 10.6\(\mu\)m for the highest NA considered but required pumping at 4.7kW as well as up to 3m of fibre to compensate for the lower nonlinearities. The amount of power converted into the 8–10\(\mu\)m band was 7.5 and 8.8mW for the 8 and 10\(\mu\)m fibres, respectively. For the 20\(\mu\)m core fibres up to 46mW was converted.

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1. Introduction

Mid-infrared (MIR) supercontinuum (SC) sources have great potential for improving spectral analysis tools, because of their spatial coherence and high power density over a broad bandwidth. A 1-4.5 μm SC source was for example used in hyperspectral IR microscopy to demonstrate simultaneous analysis at multiple wavelengths [1]. In the food and pharmaceutical industry, analysis methods, such as fourier transform IR (FTIR) spectroscopy, can be significantly improved by using a broadband high-power SC source [2]. Mid-IR SC sources are also ideal for stand-off detection, where high power density over a broad spectral range is necessary to acquire information about an ensemble of potentially hazardous substances from a safe distance [3]. Some of the current SC lasers yielding the longest IR wavelengths are based on ZBLAN fibres covering the 1-4.75 μm spectral range [4–12], and tellurite fibres covering the 1-4.5 μm range [13].

To further extend the MIR SC beyond the ZBLAN and tellurite results, materials that offer a broader MIR transmission window are needed. Promising candidates for this are chalcogenide glasses (CHALCS) as these transmit further into the infrared [14] and provide a strong nonlinear material response [15, 16] both of which are crucial in extending the SC. Due to these two features, increasing focus on developing MIR SC sources based on CHALC waveguides and fibres is taking place. Theoretically Hu et al. obtained a 2-7 μm MIR SC in optimised As-Se microstructure optical fibre (MOF) when pumping at 2.5 μm with 1kW peak power (P₀) pulses [17]. Experimentally, Gattas et al. obtained a 1.9-4.8 μm MIR SC in an As-S fibre. Picosecond long pulses generated from an erbium (Er³⁺) laser were initially amplified in an erbium/ytterbium (Er³⁺/Yb³⁺) amplifier, red shifted and amplified with a thulium (Tm³⁺) amplifier, and finally red shifted to 2.4 μm in a nonlinear fibre, where after they were coupled into the As-S fibre for generation of SC [18]. Yuan has numerically shown that an As-Se MOF, having an idealised loss without extrinsic impurities, otherwise typically present in a fabricated fibre, can give a 2-10 μm SC when pumped with femtosecond pulses having P₀=10kW at 4.1 μm [19]. Wei et al. likewise numerically obtained a broadband 2-12 μm SC in As₂Se₃ MOF, which was pumped at 2.78 μm with P₀=1kW femtosecond pulses from a mode-locked Er³⁺:ZBLAN laser [20]. In just 15mm of bulk LiInS₂ material, Bache et al. showed numerically that it is possible to obtain a 1-8 μm SC when pumping with femtosecond pulses having peak intensities of 300GW/cm² launched at 3 μm from a tunable Optical Parametric Amplifier (OPA) [21]. Experimentally, Yu et al. used an OPA generating femtosecond pulses having P₀=20MW at 5.3 μm, where they were able to demonstrate a 2.5-7.5 μm SC by pumping a bulk Ge₁₁.₅As₂₄Se₆₄.₅ sample [22]. Exchanging the bulk sample with a waveguide having a core composed of Ge₁₁.₅As₂₄Se₆₄.₅ and a cladding of Ge₁₁.₅As₂₄S₆₄.₅ they were able to generate a MIR SC covering the 1.8-7.5 μm range when pumping with an OPA at 4 μm but now with only P₀=3260W [23]. Similar waveguides have also been successfully utilised in MIR chemical sensing [24]. Likewise, we have also theoretically shown that even a standard, pulsed Tm³⁺ laser operating at 2 μm can be used to generate a 0.9-9 μm MIR SC in dispersion-optimised CHALC MOF by using a ZBLAN fluoride fibre as an intermediate fibre [25].

In this work simple and robust step-index fibres (SIFs) were considered for the generation of MIR SC, which were based on core/cladding As-Se/Ge-As-Se glasses. In our previous work on designing ZBLAN fluoride SIFs, a single experimentally obtained Sellmeier polynomial was used for the core material together with the assumption of a constant numerical aperture (NA) in order to estimate the dispersion of the cladding material [26, 27]. In contrast, the fibre designs in this work were based on measured bulk material refractive indices for both the core and cladding CHALC materials over the entire wavelength range considered. This is to our knowledge the first design of CHALC SIFs where measured CHALC material refractive indices are utilised for both the core and the cladding leading to a wavelength dependent NA. Furthermore,
we measured the CHALC SIF loss, which in combination with the improved fibre dispersion modeling should make our modeled SC results more accurate in predicting the experimentally obtained MIR SC.

For the formation of MIR SC a MIR laser operating at 4.5 μm based on praseodymium (Pr³⁺) doped CHALC (Pr³⁺:CHALC) fibres was considered [29–31]. For the laser Gaussian shaped pulses were assumed with a temporal duration (T_{FWHM}, full width at half maximum) of 50ps, and a repetition rate of 4MHz. While some of the previously reported CHALC SC were based on very high peak power [19,21,22], the peak power considered here were at 0.75, 1 and 4.7kW in order to keep the intensities below or at the theoretical peak intensity threshold of 3GW/cm² of CHALCs [28, 29]. Furthermore, the pump wavelength of 4.5 μm considered and the high NA of the fibres ensured that the material zero dispersion wavelength (λ_ZDW) could be reached with either the first, the second, or the third Raman line, which makes the Raman-induced broadening process efficient enough to generate a 3-12.5 μm MIR SC.

2. Optical material properties

The glasses and fibres considered here were made at the University of Nottingham, UK. The SIFs had a core made of As₄₀Se₆₀ (As-Se) and a cladding made of Ge₁₀As₂₃.₄Se₆₆.₆ (Ge-As-Se). The compositions had sufficient thermal compatibility so that a SIF preform made of the two could be drawn down to a fibre. In order to model the optical properties of the fibres the refractive indices were measured [32] and compared to the As-Se composition AMTIR-2 from Amorphous Materials Inc. [33].

![Fig. 1. Optical properties of the CHALC glasses. (a) Refractive index (black) and dispersion (red) of bulk As₄₀Se₆₀ (As-Se) (solid), Ge₁₁.₅As₂₄Se₆₄.₅ (Ge-As-Se) (dashed) [32], and AMTIR-2 As-Se (dash-dotted) [33]. (b) Large core (D_c=288 μm) fibre loss measurement with different absorption bands indicated (solid black), and an idealised loss without the two strong O-H and H₂O absorption bands at 2.9 and 6.3 μm (dashed red) as well as AMTIR-2 As-Se bulk material absorption (dotted black) [33]. (c) NA=\sqrt{n_{core}^2 - n_{cladding}^2} of a SIF with As-Se as core and Ge-As-Se as cladding.](image)

The refractive indices, which were measured using ellipsometry (J.A. Wollam Co., Inc. IR-VASE®) are shown in Fig. 1(a) (black). Comparing the As-Se (solid) core material and the Ge-As-Se (dashed) cladding material with AMTIR-2 (dash-dotted) indicates that the measured As-Se composition was in correspondence with the AMTIR-2, as both have comparable refractive index. The Ge-As-Se glass had a significantly lower index than the other two, allowing it to be used as the cladding of high-NA fibres. The close resemblance between the different bulk glasses can be seen when comparing their material dispersions (red), which were calculated from the refractive indices, with the λ_ZDW of core and cladding compositions at 7.4 μm and
7.0μm, respectively, and at 7.2μm for the AMTIR-2. For all glasses the dispersion dropped rapidly at wavelengths below their respective λ_{ZDW}'s. At wavelengths longer than the λ_{ZDW} a pronounced difference between the glasses is seen as the dispersion of our glasses gradually increased up to 10ps/nm/km at 12μm whereas the dispersion for AMTIR-2 increased up to 50ps/nm/km.

Figure 1(b) shows the fibre loss of a large core SIF having a core diameter (D_c) of 288μm and cladding diameter of 300μm, measured with a FTIR spectrometer in the 1.6-12.5μm range based on the standard cut-back technique [34]. The large core fibre was deliberately chosen in order to couple the low intensity light from the globar in the FTIR into the fiber. The lowest measured loss was 1.68dB/m at 6.97μm and in general a loss below 2.5dB/m was obtainable in the 3.3-9.4μm range. Even lower losses were achieved with further purification [35]. At shorter and longer wavelengths the loss increased sharply. Strong absorption bands at 2.9 and 6.3μm were present due to water impurities (O-H, H₂O). We investigate the influence of these water absorption bands on the developing SC by comparing the modeled spectra obtained with the full loss (solid black curve) and a idealized loss where the two peaks at 2.9μm and 6.3μm were removed (dashed red curve). For fibres fabricated from the As-Se core and Ge-As-Se cladding glasses the 1.6-12.5μm was considered the effective transmission region of the fibre. Beyond that we extrapolated the loss to 250dB/m at all wavelengths, which was the same as the theoretically estimated loss of the As-Se composition at 16μm by Maklad et al. [36].

A comparison of the As-Se/Ge-As-Se fibre loss with that of the AMTIR-2 As-Se bulk glass [33] shown in Fig. 1(b) revealed noticeable differences. The AMTIR-2 had an almost constant loss of 4.34dB/m in the 1-10μm region with a strong peak of 8.7dB/m at 5μm making the AMTIR-2 loss generally higher than the loss of the Nottingham glasses. Some of the current numerical and experimental results on broadband CHALC SC were obtained with a few millimeters or centimeters of waveguide when pumping with very high peak powers [21, 22]. Over such short lengths of waveguide the losses could in practice be neglected. However, such high peak powers are rarely available from lasers outside specialised optical laboratories, so lengths on the order of several centimeters or even meters of fibre need to be considered to obtain the same broadening with lower pump peak powers. Also, in any system of practical interest it is desirable to have a piece of fibre with a reasonable length for fibre handling. Increasing the length of the fibre to accommodate these requirements and the broadening processes will inevitably start to become impaired by loss.

The rate of change in the refractive index with wavelength between the core As-Se and cladding glass Ge-As-Se in Fig. 1(a) was comparable. When calculating the NA=√n_{core}²−n_{cladding}² of a SIF made of the two glasses is shown in Fig. 1(c), which demonstrated a reasonably constant NA around one in the 2-13μm range. The high NA would make sure that the Fundamental Mode (FM) was properly confined to the core at all wavelengths, so the generation of SC could proceed unhindered.

### 3. Chalcogenide step-index fibre design

Broadband MIR SC sources require a λ_{ZDW} close to the pump wavelength λ_p, a dispersion that is low and anomalous, and a nonlinearity and confinement that is as strong as possible over the entire bandwidth [27]. Furthermore, the fibre should preferably be single mode at λ_p in order to avoid distributing the pump power into higher order modes [37, 38, 50, 52].

For the initial design optimisation SIFs having a core diameter between 5-20μm, and a constant NA between 0.2 and 1.0 were considered. The initial predictions of the optimum NA=1.0 SIFs were finally checked using the measured wavelength dependent NA. Chalcogenide SIFs with lower NAs down to 0.2 were also considered since these had already been fabricated using other compositions such as the ones given by Savage et al. [39]. Additionally, glass fibre
Properties may differ from those of a well-annealed bulk glass sample because the high cooling rate encountered during fibre drawing tends to bestow a higher glass fictive temperature, and so potentially a lower refractive index. This had been observed for fluoride glasses by Nakai et al. [40]. Moreover, drawing-induced re-orientation may occur in the case of chain molecular structures which can be present in glasses for instance Se-chains in CHALC glasses [41]. The resulting fibres could thus have a lower NA than the one shown in Fig. 1(c), which can result in noticeable changes in the optical properties of the fabricated fibres. This was thus an additional reason for studying generation of SC in lower NA SIFs.

Figure 2 shows a series of calculated fibre dispersions where the dispersion experienced pronounced changes with changing core size and NA. In Fig. 2(a) NA=0.5 and the core size was varied. The dispersion for the 5µm core diameter SIF (solid) was steep with λZDW=10µm. When increasing the core diameter to 10µm (dashed), the dispersion became low and normal from 5 to above 12µm. Such a fibre could be very interesting for all-normal dispersion Self-Phase Modulation (SPM) based coherent SC obtained using femtosecond pump pulses [42]. Here we used picosecond pump pulses to obtain high average power, which meant that the formation of SC was dominated by noise-seeded Raman scattering with no improvement in noise performance similar to anomalously pumped MI-based SC [43]. A further increase in the core diameter to 20µm (dash-dotted) moved the λZDW by 4µm to 6.2µm. Additional pronounced changes in fibre dispersion were observed when changing the NA as seen in Fig. 2(b). Here the core diameter was kept at 10µm and the NA was increased from 0.2 to 1.0. The lowest NA=0.2 (solid) dispersion had a λZDW=7.9µm and was monotonically increasing. The NA=0.6 fibre (dashed) had a weak all-normal dispersion similar to the NA=0.5 fibre in Fig. 2(a). By increasing the NA to 1.0, the dispersion changed substantially where it became weak and anomalous above λZDW at 5.2µm.

Due to these quite pronounced changes in fibre dispersion, a more extended analysis of the optical properties was conducted as shown in Fig. 3. In Fig. 3(a) we see the fibre loss edge defined as the wavelength where the calculated fibre confinement loss reached a loss of 3dB/m [27]. For the smallest core of 5µm with a low NA=0.2, the λ3dB was below 4µm, meaning that the design would not be able to guide even the pump at 4.5µm. Increasing the core diameter moved the λ3dB above 8µm. Increasing NA gradually moved λ3dB for all core geometries to longer wavelengths and for NA≥0.6 even the smallest core of 5µm was guiding light beyond 10µm.

The pump at λp=4.5µm was in the normal dispersion regime for all of the different designs considered, as seen in Fig. 3(b). Starting with the 20µm core the dispersion was around -20ps/nm/km for all the different NAs. The normal dispersion for the SIFs with NA=1.0 and 0.8 became weaker as the core diameter was decreased, until reaching a minimum value and then rapidly increasing again. For NA=1.0 the minimum normal dispersion was close to zero, indicating that the λZDW approached λp. For SIFs with NA at 0.6 and 0.4 the dispersion remained...
Fig. 3. Detailed analysis of fibre optical properties. (a) Fibre confinement loss edge $\lambda_{3dB}$, (b) dispersion $D$ at $\lambda_p=4.5\mu m$, and (c) nonlinearity $\gamma$ at $\lambda_p$ vs. core diameter for different NA. (d) Zero Dispersion Wavelengths for different core diameter and NA. The solid red line indicates the pump at 4.5$\mu m$ and dotted red lines are the first three Raman Stokes lines based on the model by Ung et al. [44].

constant around -20ps/nm/km for the larger core diameters where after it became stronger for core diameters below 10 and 12$\mu m$, respectively. For the fibre with NA=0.2, the dispersion decreased as the core size was decreased, but started to increase again for core size below 7$\mu m$.

The nonlinearity, given as $\gamma = \frac{2m_2}{A_{eff}(\lambda)}$ with $m_2 = 5.2 \cdot 10^{-18} m^2/W$ at 4.5$\mu m$ [15, 16] and $A_{eff}(\lambda) = \frac{\int \int |E(\lambda)|^2 dxdy}{\int \int |E(\lambda)|^4 dxdy}$ [45], was evaluated at $\lambda_p$ and is shown in Fig. 3(c). It increased with decreasing core size and increasing NA as expected, since both would decrease $A_{eff}(\lambda)$ of the mode. This is the case for all the NAs but the two lowest, which could not confine the mode properly at 4.5$\mu m$. The nonlinearity for the smaller cores and the lowest NAs of 0.2 and 0.4 decreased, which was due to poor mode confinement. This corresponded well with the low mode confinement seen in the short $\lambda_{3dB}$ for the same NAs in Fig. 3(a).

A detailed summary of $\lambda_{ZDW}$ is shown for core diameters in the 5-20$\mu m$ range and NA=0.2, 0.5, 0.8, and 1.0 in Fig. 3(d). The solid red line is the pump at 4.5$\mu m$ and the dotted red lines are the first three Raman Stokes lines calculated from the measured As-Se Raman response reported by Ung et al. [44]. For all the fibres considered there was a spectral gap between $\lambda_p$ and the first $\lambda_{ZDW}$. Given that the pump considered had long picosecond pulses it would be the strong Raman scattering generating a cascade of Raman stokes similar to that reported by White et al. [46] that would be responsible for pushing light above the $\lambda_{ZDW}$, similar to the example experiments by Shi et al. in tellurite fibres [47] and Møller et al. in silica fibres [43].

For NA=0.2 the $\lambda_{ZDW}$ was around 7.5-8.5$\mu m$. Increasing the NA to 0.5 made the changes in $\lambda_{ZDW}$ more sensitive to changes in the core diameters. In particular the $\lambda_{ZDW}$ now came closer to the third Raman line for the core diameters over 15$\mu m$. For a core diameter of 10$\mu m$ the $\lambda_{ZDW}$ shifted to 13.5$\mu m$, which in fact provided a low and normal dispersion from 5 to 13.5$\mu m$ as seen in Fig. 2(b). Increasing NA moved the $\lambda_{ZDW}$ to shorter wavelengths as seen for NAs 0.8 and 1.0, where the $\lambda_{ZDW}$ was shifted down to 5$\mu m$ for core diameter of 8$\mu m$ and NA=1.0. For the two highest NAs an additional $\lambda_{ZDW}$ appeared for the smallest core diameters. These type of changes in soft glass fibre dispersion seem to be generic when changing their core size and NA, as we reported similar trends for ZBLAN SIFs for MIR SC in the 1-5$\mu m$ region [27].

The NA=1.0 and 8$\mu m$ core fibre has the best confinement, the strongest nonlinearity, the
lowest dispersion at the pump, and the shortest $\lambda_{ZDW}$. The fibre therefore seemed as the obvious choice for efficient generation of broadband MIR SC. However, the fibre had a second $\lambda_{ZDW}$ at 9.7 $\mu$m, which would stop the soliton based spectral broadening due to spectral recoil [48]. With this in mind the SIF with a core diameter of 10 $\mu$m and NA=1.0 could be a more suitable choice as it did not have a second $\lambda_{ZDW}$, thereby allowing the spectral broadening to proceed to the long wavelength transmission edge of the CHALC fibre. In the 8 $\mu$m core and NA=1.0 fibre the long wavelength edge of the developed SC, the IR edge, will be comprised of Dispersive Waves (DWs) due to the second $\lambda_{ZDW}$ whereas in the 10 $\mu$m and NA=1.0 fibre it would consist of solitons. This would result in two different SC spectra, which are tested in the following. Similar investigation has been conducted for near-IR SC in silica PCFs showing an almost equal efficiency of generation [49].

For larger core diameters of 20 $\mu$m or above, both the nonlinearity and the $\lambda_{ZDW}$ of the NA=0.5-1.0 fibres approached each other, as seen in Figs. 3(c)–3(d), respectively. The only difference was that the $\lambda_{ZDW}$ of the NA=0.5 fibre moved just above the 3rd Raman line. With the aim scaling up the SC power the performance of the 20 $\mu$m NA=0.5 and 0.8 fibres was therefore considered in the following.

4. Small core and large nonlinearity fibre for mid-infrared supercontinuum generation

First, MIR SCG was investigated in CHALC SIFs having the wavelength dependent NA=1.0, and the smallest core diameters of 8 and 10 $\mu$m. These core geometries c.f. Fig. 3 offer the shortest $\lambda_{ZDW}$ and highest nonlinearities, hence these should be the ones that lead to most efficient formation of broadband SC. The pump pulses were 50ps and had peak power of 0.75 and 1kW for the two cores respectively, in order to stay at or below the previously mentioned theoretical damage threshold of 3GW/cm² [28, 29].

The pulse propagation in CHALC fibres was modeled using the Generalised Nonlinear Schrödinger Equation (GNLSE) for single mode and single-polarisation, as detailed in [26,27] for fluoride fibres. For the nonlinear material response a wavelength depended Kerr coefficient $n(\lambda)$ found in [16] was used together with the Raman profile taken from [44]. The high NA of the fibres allowed them to guide multiple modes with around 20 guided modes at 4.5 $\mu$m for the $D_c=10$ $\mu$m and NA=1.0 fiber, which had a V-number around 7, so some of the pump power could be lost to higher order modes. However, proper incoupling can ensure excitation of the FM only, which would be responsible for the majority of the broadening [49-51]. Since the fibres considered were not polarisation maintaining, during propagation the power would be distributed between the two polarisations of FM due to Cross-Phase Modulation (XPM) [53], which would effectively reduce the available peak power by a factor of two thereby limiting the potential broadening. However, the model was still be able to point out the optimum fibre design for efficient generation of broadband MIR SC.

Formation of SC in fibres having the wavelength dependent NA of 1.0 is given in Fig. 4. Generation of MIR SC in the first fibre with the 8 $\mu$m core is seen in Fig. 4(a), which had two $\lambda_{ZDW}$s at 5.1 and 9.43 $\mu$m (solid black), and a dispersion and nonlinearity at $\lambda_p$ of $-7.35$ps/nm/km and 0.2 $m^{-1}W^{-1}$, respectively. The contour plot shows how the SC developed over 2m of fibre. As the pump pulse propagated down the fibre it generated a cascade of Raman Stokes lines, which in turn generated a cascade of Raman anti-Stokes lines through non-phase matched parametric amplification [53]. The Raman induced broadening was gradually exchanged with soliton based broadening, which in turn generated DWs across the second $\lambda_{ZDW}$ where the full broadening developed over 1m of fibre. The final spectra of the developed SC with the full (black) and reduced (red) loss profiles indicated no noticeable difference, so for this SIF and pump specifications the O-H and H$_2$O absorption bands at 2.9 and 6.3 $\mu$m (see Fig. 1(c)) did not seem to pose any significant hindrance for the developing of SC.
Fig. 4. Ensemble averaged (five seed) MIR SC generated in CHALC SIFs with wavelength dependent NA of 1.0. (a) Generation of SC in the 8μm fibre. Top: SC output spectra for the full (black) and reduced (red) fibre loss profile at the end of the fibre. Middle: Contour plot of the SC as it developed over 2m. Bottom: Fibre dispersion. The &lambda;p, &lambda;ZDW, and -20dB IR edge are given as dashed black, solid black, and solid red vertical lines, respectively. (b) The IR power (8-10μm band) (black) and IR edge (red) with the full (solid) and reduced (dashed-dotted) fibre loss profiles. Below is the total optical power for the full (solid) and reduced (circles) loss profiles. (c-d) Generated MIR SC in the Dc=10μm fibre with the same notation.

Figure 4(b) shows how the SC developed in terms of the accumulated IR power in the 8-10μm range (black) and the -20dB IR edge (red) with the full (solid) and reduced (dashed) fibre loss. It is seen how onset of broadening began around 50cm of propagation and continually extended the spectrum out to the long wavelength transmission edge of the fibre of 12.5μm, which was initially due to Raman scattering followed by soliton self-frequency shifting. The accumulated IR power, in the 8-10μm range, peaked at approximately 1.7m with around 6.6 and 7.5mW converted power for the full and reduced fibre losses, respectively. Unlike the IR edge the converted IR power was affected by the prominent water bands. The total optical power seen below in the figure for both the full (solid) and reduced (circle) fibre losses decreased from around 150 to around 30mW with slight increase in the loss with the onset of broadening. In terms of total power there were no noticeable difference in the loss between the full and reduced loss profiles.

Figure 4(c) shows how the MIR SC was generated in the Dc=10μm fibre. This fibre had a single &lambda;ZDW at 5.2μm and the dispersion and nonlinearity at &lambda;p of -10.2ps/nm/km and 0.15 m−1W−1, respectively. With the slightly longer &lambda;ZDW and lower nonlinearity, 2m of fibre was needed to obtain the full broadening, and for this fibre the SC extended out to 10.7μm, which was the wavelength region where the fibre loss increased locally due to Se-O impurities [54] and intrinsic material losses [36] as seen in Fig. 1(b). The contour plots of the developing of SC
shows that in the 8μm fibre there was no noticeable broadening the first 50cm followed by a gradual broadening out to 10.7μm over the remainder of the 2m fibre. Comparing the developed SC with the full and reduced fibre loss profiles given as black and red spectra, respectively, seen in Fig. 4(d), again did not reveal any noticeable changes in terms of the development of the SC due to the two strong water absorption bands as in the 8μm fibre.

The evolution of the IR power and edge of the developing SC in Fig. 4(d) shows that the maximum power conversion into the 8-10μm band was 7.6 and 8.6mW for the full and reduced fibre losses, respectively, and was obtained in around 1.6m of fibre. This was slightly shorter than the 1.64m necessary in the 8μm fibre for the maximum power conversion, which is due to higher peak power utilised. Just as in the 8μm core fibre the loss bands at 2.9 and 6.3μm lead to small deviation in converted power due to the loss bands at 2.9 and 6.3μm.

Comparing the SC spectrum of the two fibres as seen in Figs. 4(a)–4(c) shows a more uniform SC spectrum being obtained in the 10μm fibre out to 10μm with the absence of the second λZDW. This was because the solitons in the 8μm fibre experienced cancellation of soliton self-frequency shift due to spectral recoil and formation of DWs across the second λZDW [48, 49], which depleted their energy and the whole SC around the second λZDW. Apart from the difference in shape of the SC spectrum the two different pump and fibre configurations yielded almost the same IR powers.

5. Large core and high average power fibre for mid-infrared supercontinuum generation

For applications such as stand-off detection and IR counter measures, not only a broad bandwidth but also a high average power in the MIR spectral range is required. In order to accommodate this, large core fibres are needed, as increasing the core size increases the power handling ability of the fibres. Increasing the average power of the MIR SC was done by increasing the average power of the pulsed pump source given as P_{avg}=1.06P_0T_{FWHM}νr for a Gaussian pulse. With νr=4MHz and T_{FWHM}=50ps pulses with an increased peak power of 4.7kW were considered that yielded an average pump power of around 1W. Apart from the increased average power the increased peak power was crucial in overcoming the much lower nonlinearity of the larger core fibres.

The fibres considered had a core size of 20μm and NA={0.5, 0.8, 1.0}. As seen in Fig. 3, scaling up the core size and reducing the NA shifted the λZDW to longer wavelengths and decreased the nonlinearity. Both changes in fibre dispersion and nonlinearity impaired the fibre in broadening the SC spectrum out to the long wavelength transmission edge of the fibre.

Figure 5 shows generated MIR SC in the 20μm fibres that had a wavelength dependent NA of 1.0. Figure 5(a) shows the generated MIR SC at the end of 2m of fibre, pumped with the 1kW peak power pulse used previously to study the small core fibre designs. The fibre had a λZDW=6.11μm, and dispersion and nonlinearity at λp of -19ps/nm/km and 0.04m⁻¹W⁻¹, respectively. The SC spectrum for both the full (black) and reduced (red) fibre loss profiles extended to 7μm, which was due to a single Raman line building up followed by its own SPM broadening. Figure 5(b) shows a completely unchanged IR edge (red) and an IR power (black) at zero, which shows that the 1kW peak power pump was not able to generate any noticeable broadening in this large core fibre. The evaluated total power shown below in Fig. 5(b) for both full (solid) and reduced (circles) fibre loss profiles continually decreased over the entire length of fibre from 200 down 45mW. A longer length of fibre would not yield any more broadening as any formation of higher order Raman lines would decrease in power due to the fibre losses thereby effectively stopping the broadening processes.

Figure 5(c) shows the generated SC the same fibre but with 4.7kW peak power pulses, which were still below the theoretical damage threshold. In this case a broadening out to 10.6μm was obtained over 2m of fibre. Compared to the small core fibres the increased peak power resulted
Fig. 5. Ensemble averaged (five seed) MIR SC in CHALC SIFs with $D_c=20\mu m$ and wavelength depended NA around one. (a) The generated SC when using $P_0=1kW$ and $L=2m$. Top: Output SC spectrum for the full (black) and reduced (red) loss profile. Middle: Contour plot of the SC as it developed over 2m. Bottom: Fibre dispersion. The $\lambda_{p}$, $\lambda_{ZDW}$, and -20dB IR edge are given as dashed black, solid black, and solid red lines, respectively. (b) The IR power (8-10 $\mu m$ band) (black) and IR edge (red) with full (solid) and reduced (dash-dotted) loss profile. At the bottom is given the total optical power for the full (solid) and reduced (circles) loss profiles. (c-d) Generated MIR SC in the same fibre with a length of 2m and $P_0=4.7kW$. 

also in an increased power spectral density over the entire SC. The evaluated IR edge of the SC in Fig. 5(d) shows how it extended out to 10.6 $\mu m$ where it too stopped due to the intrinsic and extrinsic fibre losses [36, 54] just like the 10$\mu m$ fibre. Due to the larger average power, the maximum converted IR powers were 41 and 46mW for the full and reduced fibre losses, respectively, and were in 1.6 and 1.8m of fibres. The total power in Fig. 5(d) was continuously decreasing from around 996 to 200mW. The total output power was still higher than the output power when utilising the smaller core fibres. Employing larger fibre cores thus allowed for utilisation of high peak powers pulses, which lead to a higher spectral power density as well as a higher IR power.

Formation of MIR SC in the 20$\mu m$ core lower NA fibres of 0.8 and 0.5 is shown in Fig. 6. The MIR SC at the end of the NA=0.8 SIF fibre is seen in Fig. 6(a) where a pulse with $P_0=4.7kW$ was propagated over 2.25m. The fibre had the $\lambda_{ZDW}=6.28\mu m$ while the dispersion and nonlinearity at $\lambda_p$ were at -19.2ps/nm/km and 0.04m$^{-1}$W$^{-1}$, respectively. For both the full and reduced fibre loss profiles the spectrum extended out to 10.3 and 10.4 $\mu m$, respectively.

The IR power and IR edge of the developing SC is seen in Fig. 6(b). The IR edge indicated that the broadening began to stagnate at the end of the 2.25m of fibre, which was comparable to the NA=1.0 fibre (see Fig. 5(d)). The highest IR power was 38mW in 1.9 and 42mW in 2m of fibre for the full and reduced losses, respectively, and it required slightly longer length of fibre
due to the lower nonlinearity and longer $\lambda_{ZDW}$. The change in total power of the NA=0.8 fibre was comparable to the NA=1.0 when pumping with the same pulses, as 2.25m of fibre reduces the power from 996 to 200mW.

The generated MIR SC at the end of 3m of the NA=0.5 fibre is seen in Fig. 6(c). The fibre had a $\lambda_{ZDW}=6.8\mu m$, and a dispersion at $\lambda_p$ of -20.7ps/nm/km and nonlinearity at $\lambda_p$ of 0.04m$^{-1}$W$^{-1}$, which was the lowest of the fibres considered. The SC extended to around 9.5\mu m where the SC IR edge stopped for both the full and reduced fibre loss profiles. Evaluating the IR power and IR edge was done in Fig. 6(d). Both the largest broadening and the highest power conversion was obtained over three meter of fibres due to the much lower nonlinearity than the NA=0.8 and NA=1.0 fibres. The obtained IR powers were 11mW and 17mW for the full and reduced fibre losses, respectively, which was the largest deviation between the full and reduced loss of the fibres considered. Just like the previous two fibres the total power decreased continually from around 996 to 200mW.
6. Conclusions

We have presented a detailed study of 4.5 \( \mu \)m pumped MIR SC generation in CHALC SIFs based on measured material dispersion and fibre loss data covering the 1.6-12.5 \( \mu \)m wavelength region. The considered fibres were made from a unique thermally compatible As-Se and Ge-As-Se glass pair promising ultra-high NA's around one. The pump source was proposed to be a Pr\(^{3+}\):CHALC fibre laser with a repetition rate of 4MHz, giving 50ps pulses with a peak power of 4.7kW, in order to satisfy the physical limit on the applicable peak power imposed by the CHALC material [28, 29].

Fibre design studies revealed two interesting regimes. The NA=1.0 fibres were demonstrated always to be the optimum compared to lower NA fibres, with a lowest possible \( \lambda_{ZDW} \) of 5\( \mu \)m being obtained for a core diameter of 8\( \mu \)m. Due to the presence of a second \( \lambda_{ZDW} \) at 9.43\( \mu \)m for the 8\( \mu \)m fibre it was shown that the NA=1.0 fibre with a 10\( \mu \)m core diameter seemed to be the optimum in terms of generating a flat SC spectrum because it had no second \( \lambda_{ZDW} \). However, the 8\( \mu \)m core was the only design that was able to extend the spectrum out the long wavelengths transmission edge of the fibres at 12.5\( \mu \)m. This was because the second \( \lambda_{ZDW} \) allowed for formation of MIR DWs that were able to push the light further past the point where soliton self-frequency shifting stopped extending the spectrum in the 10\( \mu \)m fibre at 10.7\( \mu \)m. For both fibres Raman scattering was necessary for the spectrum to cross \( \lambda_{ZDW} \) as the pump was located in the normal dispersion regime. Both for the 8 and 10\( \mu \)m core two Raman lines were necessary to cross \( \lambda_{ZDW} \), although the first Raman line was very close to \( \lambda_{ZDW} \) for the 8\( \mu \)m core fiber. The fibres were able to convert 7.5 and 8.6mW, respectively, into the 8-10\( \mu \)m band. The broadest bandwidth obtained was from 3 to 12.5\( \mu \)m in the 8\( \mu \)m fibre.

The second interesting fibre design regime was for core diameters of 20\( \mu \)m or above, for which the nonlinearity and \( \lambda_{ZDW} \) of the fibres with NA between 0.5 and 1.0 approached each other. The \( \lambda_{ZDW} \) was then below the third Raman Stokes line for the NA=1.0 and 0.8 fibres, but just above for the NA=0.5 fibre. This could potentially provide a convenient design freedom in terms of the NA and the larger core could improve the power handling capabilities of the fibre. Due to the lower nonlinearity of the large core fibres an increased peak power of 4.7kW was considered in order to push the spectrum into the mid-IR, which was comparable to the theoretical damage intensity threshold of 3GW/cm\(^2\) [28, 29]. The NA=1.0 and 20\( \mu \)m core diameter fibre were demonstrated to be able to generate a 3-10.6\( \mu \)m SC with around 46mW in the 8-10\( \mu \)m region. The NA=0.8 fibre was demonstrated to have similar performance, while the NA=0.5 fibre did not perform nearly as efficient as it needed four Raman Stokes lines to cross the \( \lambda_{ZDW} \).

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