The Analysis and Comparison of Leakage Inductance in Different Winding Arrangements for Planar Transformer

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Abstract -- The coupling of the windings can be easily increased by using multiply stacked planar windings connection. Interleaving is a well-known technique used to reduce leakage inductance and minimize high-frequency winding losses. The paper aims to analyze leakage inductance based on magneto motive force (MMF) and energy distribution in planar transformer and correct the formula of leakage inductance proposed by previous publications. The investigation of different winding arrangements shows significant advantages of interleaving structure. In this work, a novel half turn structure is proposed to reduce leakage inductance further. Some important issues are presented to acquire desired leakage inductance. The design and modeling of 1 kW planar transformer is presented. In order to verify the analytical method for leakage inductance in this paper, finite element analysis (FEA) and measurement with impedance analyzer are presented. Good matching between calculation, FEA 2D simulation and measurement results is achieved.

Index Terms— leakage inductance, magneto motive force (MMF), finite element analysis (FEA), interleaving, half turn, planar transformer

I. INTRODUCTION

In recent years, planar transformers have become increasingly popular in high frequency power converter design because of the advantages they achieved in terms of increased reliability, reproducibility, and increased power density. In terms of circuit performance one of the advantages of planar transformer is low profile and repeatable leakage inductance [1]. The leakage inductance causes the main switch current at the device input to vary at a low slope between zero and rated value and reduces the rate of commutation between output diodes. In addition, the stored energy in the leakage inductance leads to the generation of voltage spikes on the main switch which, besides creating EMI problems, increases the switching losses and lowers the efficiency [2]. Therefore, most designers expect the leakage inductance to be as small as possible. However, in some applications such as a phase-shift-modulated soft switching DC/DC converter, the magnitude of the leakage inductance determines the achievable load range under zero-voltage operation, and a relatively large leakage inductance is desirable. This paper aims to calculate the leakage inductance stored in planar transformer by analyzing magneto motive force (MMF) and energy distribution. Section II defines leakage inductance using the perspective of energy. The energy associated with leakage inductance should be equal to the sum of energy stored in each element layer inside the core window. The section also analyzes the magnetic field strength in each layer and finite element analysis 2D model is simulated to demonstrate the correctness of the analytical method. As presented in previous publications [3-5], the formula (see eqn.6) is generally used to calculate the leakage inductance. However, it must be noted that the formula doesn’t provide precise results. It assumes that the magnetic field strength along the height of insulator layer between non-interleaved sections varies linearly but actually it should keep constant during the whole area of insulator layer. In order to correct the previous formula, a new formula suited for symmetrical winding arrangement is proposed in this paper. The error analysis on the two calculations is also presented. Section III proposes a novel half turn structure to reduce leakage inductance further. The MMF distribution curve for half turn arrangement is analyzed and leakage inductance is computed. Section IV describes some important issues to require desired leakage inductance including copper thickness, the thickness of insulator layer and the number of turns. Section V evaluates the good matching between calculation, FEA 2D simulation and measurement with impedance analyzer (PSM1735+ Impedance Analysis Interface and Kelvin Fixture) which indicates the correctness of the analytical method and the proposed calculation. Section V provides the conclusion.

II. BASIC DEFINITION AND CALCULATION FOR LEAKAGE INDUCTANCE

A. Basic Definition of Leakage Inductance

Not all the magnetic flux generated by AC current excitation on the primary side follows the magnetic circuit and link with the other windings. The flux linkage between two windings or parts of the same winding is never complete. Some flux leaks from the core and returns to the air, winding layers and insulator layers, thus these flux causes imperfect coupling. If the secondary is short-circuited, the main flux which links both windings will be negligible because the primary and secondary ampere turns almost cancel. So the leakage flux parts don’t lose their individual identities. It is seen from Fig.1 that within the winding area the mutual repulsion causes the leakage flux to lie approximately parallel to the winding interface. The leakage inductance referred to the primary can be accessed by the energy stored in a
magnetic field,

\[ E_{\text{energy}} = \frac{1}{2} \int_{V} B \cdot H \cdot dV = \frac{1}{2} \cdot I L \cdot I_p^2 \]  
\[ (1) \]

Fig. 1 The leakage flux paths and magneto motive force variation (MMF)

**B. Leakage Inductance Calculation**

For simplification to analyze MMF created by the windings, turns ratio 1:1 and total number of turns 8 are used as example. The MMF varies linearly in winding layers (see Fig. 2) can be assumed when operation frequency is not very high. When the frequency is increased, MMF distribution will become non-symmetrical winding arrangement (symmetrical MMF distribution) is proposed which can be expressed by, 

\[ \text{MH} = \frac{1}{b_w} \frac{1}{b_1} \frac{I_1}{I_p} \]

where \( b_1 \) and \( b_2 \) are the thickness of primary and secondary respectively, \( b_3 \) is the height of insulator layers.

The analytical scheme of MMF distribution for non-interleaving structure can be calculated as follows:

\[ F_{\text{energy}} = \frac{\mu_0}{2} \int w_b \cdot h \cdot dx \]
\[ (2) \]

where \( w_b \) is the width of each turn, \( b_w \) is the width of each turn, \( h \) represents the thickness of each winding layer. Fig. 2 shows the thickness \( d_x \), situated at a distance \( x \) from the inner surface of the secondary winding. The field strength along the flux path which includes this layer depends on the number of ampere turns linked by the path. Since the flux disperses rapidly on leaving the winding, the associated energy is much reduced and the reluctance of the path within the magnetic core can be ignored compared with that of the path in the winding, therefore the flux path can be expressed by the width \( b_w \) rather than the full closed flux path. H may be taken as the field strength in the winding layer which is assumed to be constant along the plane of layer, thus, for first primary layer,

\[ H = \frac{I_1}{b_w} \frac{x}{h} \]
\[ (3) \]

according to the eqn.2, the energy in the total winding space can be deduced then

\[ F_{\text{energy}} = \frac{\mu_0}{2} \int w_b \cdot h \cdot dx \]
\[ (4) \]

where \( h_1 \) and \( h_2 \) are the thickness of primary and secondary respectively, \( h_3 \) is the height of insulator layers. Fig. 3, Fig. 4 and Fig. 5 show energy distribution (a) and magnetic field strength distribution (b) in non-interleaving structure, P-P-S-S-P-S-S structure and P-S-P-S-P-S-P-S structure respectively. Fig. 4 and Fig. 5 represent partial interleaving and complete interleaving winding arrangements respectively. It is obvious to see that interleaving structure provides significant advantage in reducing leakage inductance. The analytical MMF distribution (c) can be verified by magnetic field strength distribution based on FEA simulation results (b). The good matching between (b) and (c) illuminates the correctness of analytical method. Based on the above calculation, a new general formula suited for symmetrical winding arrangement (symmetrical MMF distribution) is proposed which can be expressed by,

\[ I_{\text{leakage}} = \frac{\mu_0}{b_w} \int d_x \cdot h \cdot dx \]
\[ (5) \]

where \( k_1 = \frac{N_1}{M} \), \( k_2 = \frac{N_2}{M} \),

\( N_1, N_2 \) are the number of turns on the primary and secondary respectively, \( M \) is the number of section interfaces.

**C. The error analysis**

The formula (see eqn.6) was published in the previous reference [3-5] to compute the leakage inductance for the symmetrical interleaving structure, which has been generally used to compute leakage inductance for most of designers.

\[ I_{\text{leakage}} = \frac{\mu_0}{b_w} \int d_x \cdot h \cdot dx \]
\[ (6) \]

where \( N \) is the number of turns on the winding which the leakage inductance is to be referred; \( M \) is the number of section interfaces; \( \Sigma x_A \) is the sum of all inter-section layer dimensions perpendicular to the section interfaces and \( \Sigma x_A \) is the sum of all inter-section layer thickness. It must be noted that the P-P-
S-S-S-P-P and P-S-P-S-P-S-P structures mentioned in publication [3] have same leakage energy with the P-P-S-P-P-S-P-S and P-S-P-S-P-S-P-S-P-S-P structures respectively.

However, it assumes that the magnetic field strength along the height of insulator layer between non-interleaved sections varies linearly which is shown by the blue line in the Fig.6. Actually there is no extra flux path link with the insulator layer, the MMF curve should, therefore, keep constant in the area of insulator layer (see black line in Fig.6). The correctness of the latter analytical MMF distribution can be proved by FEA 2D simulation.

As an example, a planar transformer has been built with EI 64/5/50 core, the length of each turn is 202mm, copper width is 20mm and the thickness of primary and secondary are both
0.2mm, the thickness of insulator layer is 0.3mm. The winding arrangements P-P-P-S-S-S-S, P-P-S-S-P-P-S-S and P-S-P-S-P-S-P-S will be seen as case 1, case 2 and case 3 respectively. Table I describes the error between the proposed eqn.5 and the previous eqn.6.

<table>
<thead>
<tr>
<th></th>
<th>Calculation (eqn.5)</th>
<th>Previous Calculation (eqn.6)</th>
<th>The error</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case 1</td>
<td>245 nH</td>
<td>291 nH</td>
<td>19%</td>
</tr>
<tr>
<td>Case 2</td>
<td>62.6 nH</td>
<td>82.9 nH</td>
<td>32%</td>
</tr>
<tr>
<td>Case 3</td>
<td>22 nH</td>
<td>25.8 nH</td>
<td>17%</td>
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### III. NOVEL HALF TURN STRUCTURE

The interleaving, partial interleaving and non-interleaving structures cause a significant difference in leakage inductance because of MMF distribution. From the MMF distribution curve, maximal magnetizing force in each layer determines the value of leakage inductance. Therefore half turn structure could be proposed to optimize leakage inductance further. One solution is to physically form half turn in top layer and bottom layer respectively. The other solution is to parallel the top layer with bottom layer so as to sustain half current to flow, the other layers are still in series, only one turn in each layer.

As can be seen from Fig.7, the MMF distribution has been shifted to be a symmetrical curve on the X axis. The maximal magnetizing force is reduced to half of primary current. Taken together eqn.1-3, the energy in the total winding space can be found as follows,

\[
E_{\text{energy}} = \frac{\mu_0}{2} \int_{-h_{1/2}}^{h_{1/2}} \int_{-h_{1/2}}^{h_{1/2}} \left[ \int_{-h_{1/2}}^{h_{1/2}} \frac{h_{1/2} x^2}{h_{1/2} x^2} dx \right] ^2 dx + 8 \int_{-h_{1/2}}^{h_{1/2}} \int_{-h_{1/2}}^{h_{1/2}} \left[ \int_{-h_{1/2}}^{h_{1/2}} \frac{h_{1/2} x^2}{h_{1/2} x^2} dx \right] ^2 dx + 6 \int_{-h_{1/2}}^{h_{1/2}} \int_{-h_{1/2}}^{h_{1/2}} \left[ \int_{-h_{1/2}}^{h_{1/2}} \frac{h_{1/2} x^2}{h_{1/2} x^2} dx \right] ^2 dx
\]

\[
E_{\text{energy}} = \frac{\mu_0}{2} \int_{-h_{1/2}}^{h_{1/2}} \int_{-h_{1/2}}^{h_{1/2}} \left[ \int_{-h_{1/2}}^{h_{1/2}} \frac{h_{1/2} x^2}{h_{1/2} x^2} dx \right] ^2 dx + \left( \frac{11 h_{1/2} + 4 h_{1/2}}{48} + 2 h_{1/2} \right) \int_{-h_{1/2}}^{h_{1/2}} \int_{-h_{1/2}}^{h_{1/2}} \left[ \int_{-h_{1/2}}^{h_{1/2}} \frac{h_{1/2} x^2}{h_{1/2} x^2} dx \right] ^2 dx
\]

This structure not only reduces the leakage inductance, but also benefits the winding loss caused by skin effect and proximity effect. Referring to Dowell equation [7], the quantity \( m \) represents the ratio of the MMF \( F(h) \) to the layer ampere-turns \( NI \). The value of \( m \) can directly affect proximity loss of winding [7-10]. Interleaving windings can significantly reduce the proximity loss when the primary and secondary currents are in phase. Regarding the interleaving structure, the value of \( m \) is equal to 1 for each layer. Further, the value of \( m \) also can form to 0.5 by the half turn structure which will decrease proximity loss a lot. Of course, the maximal magnetizing force can be reduced further by paralleling more layers. The MMF curve can almost be distributed into a line which overlaps with X axis if there are sufficient layers to be parallel. However, I have to mention that it doesn’t make sense because of sacrificing winding space.

### IV. IMPORTANT ISSUES FOR LEAKAGE INDUCTANCE

#### A. The thickness of copper foil

As we can see from eqn.5, leakage inductance can be influenced by the thickness of copper foil. It should be as small as possible if leakage inductance is to be reduced. Fig. 9 shows that the thicker the copper, the higher the leakage inductance will be achieved. However, the winding loss might be sacrificed if the thin copper foil is used. It is necessary to note that the ratio of ac-resistance and dc-resistance will be reduced because of the lower skin effect, although dc-resistance is increased. Therefore, there is an optimal value on the thickness of copper foil which can balance leakage inductance and winding loss.

#### B. The thickness of insulator layer

Leakage inductance can be influenced further by the thickness of insulator layer which also can be observed from the equ.5. From Fig.9, the leakage inductance decreases when the thickness of insulator layer is reduced. Considering capacitor effect between intra-windings and insulator strength, the thickness of insulator won’t be too low. The designer should find a balance between leakage inductance and
and self-capacitor. Reducing the insulation layer thickness below a certain level will result in a considerable increase of the total losses [11].

C. The number of turns

Comparing the charts (a), (b) and (c) in Fig.9, it can be seen that the number of turns provide a significant difference in leakage inductance. The more number of turns, the higher the leakage inductance will be. However, if the number of turns is increased, winding loss will be increased which is not desirable. In reverse, core loss will be reduced because of the variation of flux density is decreased. Therefore trade-off becomes an essential design property.

D. The others

As known from eqn.5, the permeability of copper foil and insulator, the length and width of conductor are also related to the leakage inductance. The relative permeability can be controlled by different materials. Therefore, a leakage layer which consists of ferrite film could be used to realize higher leakage inductance without sacrificing winding loss. This leakage layer can be used in half–bridge resonant converter and many phase-shift applications to realize ZVS.

V. EXPERIMENTAL VERIFICATION

The design and modeling of 1 kW planar transformer is built (see Fig.10). The fold technique on the planar copper winding is adopted to avoid some undesirable problem caused by the terminal connection. Furthermore, the different winding arrangements are quite flexible to be realized if the fold technique is used.

In order to verify the analytical method for leakage inductance in this paper, the results based on measurement with impedance analyzer (PSM1735+ Impedance Analysis Interface and Kelvin Fixture) is presented. Fig.11 shows good matching between calculation, FEA 2D simulation and measurement results is achieved. The proposed novel half turn structure has been seen as case 4. Obviously half turn arrangement has best result in leakage inductance. There is no doubt that small error exists between measurement and calculation because of complex magnetic flux in actual model. The tolerance of insulator thickness and short-loop in secondary side also might cause a slight error between measurement and calculation. In addition, extra connection also leads inaccuracy result.

VI. CONCLUSION

The purpose for this paper is to find a solution to acquire a desired leakage inductance. An analytical computation of leakage inductance has been introduced. Several different winding arrangements have been investigated. Computed results are in good agreement with those obtained by FEA 2D simulation. The interleaving structure provides significant advantage in reducing leakage inductance. The previous formula has been corrected. In order to optimize leakage inductance and winding loss further, a novel half turn was proposed in this paper. Computed results shows a half turn structure benefit low leakage inductance extremely. Some important issues including copper thickness, insulator thickness and number of turns were concluded to guide designer to obtain desired value. The analytical method has been experimentally validated based on a planar core transformer. Good matching is achieved between calculation, FEA simulation and measurement.
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REFERENCES


